DYNAMICS OF UNDERCUTTERS

BY

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LIST OF FREQUENTLY USED SYMBOLS

ψ = angle of soil forward failure with respect to the direction of travel of the tool.

μ = coefficient of soil frictional resistance

ϕ = angle of soil shearing resistance

μ' = coefficient of soil-metal friction

δ = soil-metal frictional angle

ρ = soil bulk volume weight (kN/m^3)

c = soil apparent cohesion (kPa)

σ = stress normal to the shear plane (kPa)

σ_1 = major principal stress on the Mohr's circle (kPa)

σ_2 = intermediate principal stress on the Mohr's circle (kPa)

σ_3 = minor principal stress on the Mohr's circle (kPa)

τ = soil shearing strength (kPa)

c_t = soil true cohesion (kPa)

σ_e = effective stress (kPa)

ϕ_t = true angle of shearing resistance

u = pore water pressure (kPa)

S_s = soil sliding stress (kPa)

Ca = adhesion (kPa)

A = area of soil forward shear failure surface (cm^2)

G = weight of soil segment (N)

B = acceleration force on soil segment (N)

2γ = nose angle of the undercutter

θ = slide angle of the undercutter

β = angle of (inclination) mounting of each wing to the horizontal plane

ϕ_w = frictional angle of weed plants on metal

$\Delta\gamma$ = correction angle for the nose angle

β_o = cutting angle of the tool

i = sharpening angle of the tool

ε = back angle of cutting or the angle of the gap

w = wing width (cm)

W = overall width of the tool (cm)

b = length of the cutting edge of each tool wing (cm)

k = pure cutting resistance of the soil (N/m)

d = depth of tool operation (cm)

v = tool velocity (m/sec. or cm/sec.)

$\vec{N}_0$ = normal force on the tool wings (N)

$\vec{N}_1$ = normal force on the soil failure surface (N)

F_x = draft force (N)

S = side draft force (N)

V = vertical force (N)

g = acceleration of gravity (m/sec^2 or cm/sec^2)

H = lift height of the tool (cm)

Chapter I

INTRODUCTION

Of the major bottlenecks in agricultral production, the problem of weed control is quite serious. In developing countries where most farms have not been completely mechanized, the problem is further compounded by the apparent lack of appropriate weed control tools. Besides, certain soil conditions require special tools for cultivation and weed control.

Loose soils are an example whereby the soil structure must be protected as weeds are being removed. The conventional methods of rotary hoeing and inter-row cultivation using small cultivator sweeps are often unsuitable for all systems of cultivation.

It is therefore not surprising that the problem of mechanical weed control in agricultural production has persistently intrigued farmers and engineers alike. The world's different systems of cultivation and soil types call for the development of relevant weed control tools adaptable to each ecological zone.

Weed control tools, like many other implements, have gone through many stages of development and modifications. The hoe is considered the earliest tool to be invented for weed control (40). The first horse drawn cultivator was invented in 1856 and tractor mounted cultivators became a reality in 1925 (46). Early cultivators were no more than pointed rods known as grubbers (3), but were quickly followed by modified forms with curved tines called scarifiers. Subsequent developments were mere improvements on the existing tools.

In order to satisfactorily accomplish the objectives of cultivation which, according to Bainer, et. al. (1), include weed control, loosening of the surface mulch and the conservation of moisture, a more suitable tool

must, of necessity, be developed for specific soil conditions. Bainer, et al also claimed that the average annual loss of crops due to weeds in the U.S.A., as estimated by USDA was in 1978 about $5 billion. About 3 billion tons of soils were eroded from the fields and pastures in 1933 and 4 billion tons in 1968, according to David, et. al. (9). Smith (41) estimated in 1968 that the annual cost of erosion control in the U.S.A. was about $4 million.

Recently, special tools that are suitable not only for inter-row cultivation but also for stubble mulch farming in loose soils have been developed. These include the undercutter cultivator sweeps. Undercutters are symmetric V-blades that operate in the soil at depths less than 25 cm. They are widely used in sandy soils of the world including the Great Plains of the U.S.A. (10). The objective of their operation is to slice through the roots of the weeds with slight lateral displacement of the soil exposing the weed roots for drying while disturbing the soil structure to a minimum. Undercutters are essentially soil cutting tools that are geometrically similar to the small arrow shaped cultivator sweeps.

Despite the increasing application of this tillage tool, a complete analysis based on its design has not been fully made. Whether the present configurations are the most effective in terms of weed control is now uncertain. Draft power requirement and minimum soil disturbance cannot be ascertained until a further study of the tool is carried out through the analysis of its geometric elements and verification with tillage experimentation.

There are, of course, inherent problems in conducting tillage research, according to Siemens (37). These include:(a) reproducing field conditions, (b) the many soil variables which often lead to complex analytical expressions if all are included in the analysis, and (c) the nature of forces on these soil working tools is not too precisely defined.

The use of artificial soils in the laboratory has, to some extent, simplified the problem of predicting the behavior of prototypes resulting from model tool designs. This is possible because of the reproducible nature of such soils. But their use has not completely eliminated the problems associated with identifying pertinent soil properties relevant to each tillage tool investigation. There is also uncertainty about how closely the use of oil, to alter the cohesive-fictional components of such soils, simulates natural soils. Despite these drawbacks, useful and reliable results have been attained with the use of artificial soils in tillage research.

Several soil properties have been identified by many authors (37,42) as being relevant to tillage tool research. These include soil cohesion, frictional angle, soil bulk density,angleofsoil-metal friction and adhesion.

The Mohr-Coulomb failure criterion or its modified form has been successfully applied to inclined and near vertical flat blades (23,37,42,47) and mathematical relationships have been developed to predict draft forces from model tool designs. The form and extent of interacting factors in these predicted relationships have, however, not been fully explained. For instance, there are inconsistencies in the soil properties identified with each tool studied. It has not been possible to establish a correlation between soil properties associated with a particular tool investigation and those needed for investigating other tools. This may be partially explained by the fact that soil is nonhomogeneous and anisotropic and its properties can therefore be easily influenced, and in fact altered, by extraneous factors. Mathematical models presuppose the inclusion of certain soil properties which need be justified or verified during experimentation.

A great deal of reliance is placed on the mechanics of tools and soils and their dynamic interactions in conducting a tillage experiment. The

use of scale models and the application of similitude techniques to the study of tillage implements under controlled environments have produced dependable results widely used in model-prototype tool predictions.

The objective of this research was to achieve better understandings of the optimum design parameters of undercutter plow sweeps through:

a) the study of the geometric elements of the tool that influence its design and application

b) identification and characterization of those soil properties pertinent to the study.

Several model tools were fabricated for this study. Emphasis was placed on the influence of soil, slide angle (θ), lift height (H), wing width (w), wing inclined angle (β), nose angle (2γ) and the overall width of the tool (W) on draft force (See Fig. 2.1 for identification of the tool parameters). Results obtained were compared with that from the mathematical model developed to see how closely the two agree.

The performance of this tool was not evaluated beyond its draft power requirement since other factors were not within the scope of this investigation. It is anticipated that future work will correlate the attained optimum design and performance characteristics with soil disturbance and weed control potentials.

Chapter II

REVIEW OF LITERATURE

2.1 Engineering Properties of Agricultural Soils

A soil subjected to compressive or tensile stress fails along definite surfaces of slip whose inclination to the principal stress are defined by the soil properties (30). This failure pattern has been applied to the study of soil engaging cultivation implements and its recognition is essential to the study and the design of agricultural implements. In the past, soil strength was related to earth dam construction and the bearing capacities for foundations, according to Tsymbal (44), but in tillage, the goal is the disruption (elastic and plastic deformations) of soils by soil engaging implements.

Osman (27), in his work on soil cutting, inferred that as a blade is moved through the soil, it compresses the soil until it reaches its maximum shear strength at which point failure occurs. This is in agreement with the Mohr-Coulomb failure criterion. According to Fountain (12), the Coulomb shear strength equation consists of two parts:

a) frictional component which is a function of the normal load,

b) cohesive component which is independent of the normal load.

These two components are vividly expressed in Coulomb's equation as follows:

$$\tau = c + \sigma \tan\phi$$

where τ = shear strength of the soil,

c = apparent cohesion, the shear strength with zero normal load,

σ = total pressure normal to the shear plane,

ϕ = angle of shearing resistance.

Fountain further stated that c and ϕ are empirical parameters of the above equation whose values hold good only under a given set of soil

and testing conditions. If a test is conducted under constant pore water pressure, the equation is modified to:

$$\tau = c_t + \sigma_e \tan \phi_t$$

where c_t = true cohesion

$\sigma_e = (\sigma - u)$ = effective pressure

ϕ_t = true angle of shearing resistance

u = pore water pressure

The normal load on the shear plane caused by the passage of any implement through the soil depends on the stress history of such soil and the size and shape of an implement.

Sineokov (39) adduced that the non-uniformity of soil structure coupled with the rapidly changing soil moisture make the study of soil strength characteristics difficult. It is known that the ultimate tensile and compressive strength of soils decrease with an increase in soil moisture content. This is particularly true for purely cohesive soils and those containing a high proportion of plant roots. The cohesion of top soils (tillage regimes) is much lower than that of subsoils of similar texture but their frictional angles are higher in magnitude.

In addition to cohesion, and the angle of shearing resistance, are the angle of soil-metal friction and adhesion. The soil-metal friction is influenced by the normal force, soil type, surface roughness and the sliding velocity of the soil along the (metal) surface (39). Gill and Vandenberg (14) explained the soil-metal friction in terms of the dynamic property of the (soil-machine) system. Sagach et. al. (34) claimed that soil-metal friction can account for about 40 to 50 percent of the total plough resistance. This value can be reduced by the presence of free water (saturation) and by the surface finish of the tool.

Soil adhesion, according to Gill and Vandenberg, is the attraction between the soil and soil engaging machine. Adhesion impairs the quality of work and increases with increases in tractive resistance, soil dispersion, contact pressure and the soil moisture (up to a limit). Soil sliding stress is computed from the soil-metal friction and adhesion as follows:

$$S_s = Ca + \sigma \tan \delta$$

where S_s = soil sliding stress

Ca = adhesion

σ = normal stress of friction surface

δ = angle of soil-metal friction

Devices used to measure soil shear properties in the field include the torsional shear box, Cohron sheargraph, cone penetrometer and annular test apparatus. The torsional shear box is commonly used for in-place topsoil strength measurements because the failure plane it induces corresponds to the surface of natural soil weakness and the shear strength is little affected by the rate of straining the soil. It is, however, not useful for determining the shear strength of soils with large stones, organic matter and roots. The Cohron sheargraph (8) is used for measuring the shear strength of the soil either in the field or in laboratory soil bins. Its action is based on the Coulomb failure theory. It is fast and dependable but it is more widely used in traction studies than in tillage research. Cone penetrometers are useful for in-place strength determinations at varying soil depths. They are being used in saturated soils subjected to compaction or traffic. Measurements are in terms of cone index or penetration resistance. They are often influenced by two factors:

i) the rate at which it penetrates the soil, generally increasing as the penetration rate is increased.

ii) The base area of the cone, high for a small cone area and low for a large cone area.

According to Schrock (36), penetration is a composite parameter whose result depends on other independent parameters such as the soil density and the soil frictional angles. In annular tests, a torque is applied to the annular sample which is strained by twisting about the principal axis of the apparatus. Its main advantage is that no change is induced in the cross sectional area of the sample during testing but it cannot be used with most agricultural soils because annular samples are difficult to attain.

The common laboratory methods for measuring soil shear strength properties, apart from those described above, are direct shear and triaxial tests. Direct shear-test apparatus has been successfully used for cohesive samples obtained from the field or on modified samples that have been given standard compaction. This method assumes failure in the horizontal plane. The triaxial test, like the direct shear test, is used for determining the soil strength properties either on cylindrical samples or on modified samples. The Mohr-Coulomb equation is the basis for shear strength determination. This compression test is achieved by making the intermediate and minor principal stresses equal ($\sigma_2 = \sigma_3$). It is also assumed that the sample is isotropic with a uniform stress distribution in all planes. Mohr stress circles can be plotted to obtain c and ϕ. Tsymbal (44) used the limiting stress approach to explain the soil failure phenomenon. The slip plane is situated at an angle $\phi/2$ to the minor principal stress. The main disadvantages of this method include, (a) the difficulty in obtaining undisturbed soil samples for the test, (b) many dry topsoils have very little strength to support them until they are loaded and stressed in the machine, and (c) the

procedure is tedious and time consuming. Siemens (37) found no significant difference between the direct shear and the triaxial shear tests and in fact recommended the direct shear test procedure due to its simplicity.

Another property used to characterize the soil is soil density. Soil density increases with soil moisture content up to a limit. An increase in bulk density has been found to increase the soil shear strength, soil frictional angles, soil cohesion and soil failure energy. Soil strength is often used to establish procedures for measuring the compaction of soils in the soil bins since there is a need to obtain uniform density with depth (37,40).

2.2 The Use of Artificial Soils in Tillage Research

Several authors (4,26,33) successfully used natural soils in their soil-machine research, but the difficulty of reproducing test conditions was serious and the rapidly changing soil moisture content often compound the problems of measuring soil properties. Bockhop (4) employed natural soil in his work with disk plows. He used colloidal properties, moisture content, organic matter composition and temperature to characterize the dynamic properties. These were found to vary widely with time. Some of the problems associated with the use of natural soils have been overcome by the use of artificial soils in laboratory soil bins.

Clark et. al. (6) identified what the characteristics of artificial soils should be:

a) strength properties should not change with time, temperature and humidity.

b) soil mix should be representative of a wide range of soil types and soil environments.

c) soil should have strength properties that can be disturbed and quickly returned to its original state without changing its properties.

d) should behave reasonably like natural soils.

The two types of artificial soils in use are the clay-sand-oil mix and the clay-sand-ethylene glycol mix. Ethylene glycol can be varied to alter the cohesive properties of the soil but it is hydroscopic (36). Spindle oil provides little change in cohesive properties but provides excellent long term stability due to slow evaporation rate.

Korayem (18) stated that the internal frictional angle generally increases with an increase in clay content but decreases with higher ethylene glycol concentrations.

The use of artificial soils is not limited to tillage-tool investigations but has been widely used for traction studies. Schrock (36) used a frictional, artificial soil consisting of 45-45-10 mix by weight of sand, clay, and mineral oil respectively. The mineral oil used is composed from Corvus mixed with Almag SAE 5-10 in ratio of 3 parts to 4 parts respectively.

2.3 Mechanics of Soil Cutting

The majority of tillage tools reported in this literature review is involved with soil cutting. Cutting is accomplished by shearing action after the soil attains maximum compressive shear strength. Plane blades, chisels, and undercutters are involved with the cutting and lifting of the soil. The failure plane established by this cutting process is referred to as the shear surface.

Designing soil cutting tools for agricultural purposes is by far one of the more complex of all engineering problems because of the variability

of soil conditions and the fact that soil is nonhomogeneous and anisotropic. Design of tillage tools is, however, based on an assumption of soil homogeneity.

Payne (30) investigated the relationships between tool geometry, speed of operation and the volume of soil upheaval using soil mechanics theory. The Mohr-Coulomb failure theory was advanced to explain soil cleavage by wide and narrow tines and he applied the passive earth pressure of Rankine to explain the soil upheaval in front of narrow tines operating at shallow depths. The failure planes he obtained for wide tines approximated straight lines whereas those for narrow tines were essentially curved. Soil-metal frictional angle was found to be independent of speed.

Kawamura (17) studied tools having various angles of inclination and operating at varying speeds and depths. He developed a mechanics theory to determine the angles of inclination corresponding to minimum draft. As his inclined tools approached the vertical plane he obtained the same result as Payne, that the shear surface was curved and that the shear angle was influenced by speed and depth of operation.

Soehne (42) studied inclined-plane blades and established an analytical procedure to determine the draft force using various soil and tool parameters. This force was made up of soil and soil-metal frictional components, shear failure, acceleration force and soil-cutting resistance respectively. Soehne inferred that for low angles of inclination (less than 40 degrees) the shear surface is not curved but a straight line, inclined at an angle of $45-\phi/2$ to the horizontal. Soehne found that frictional force due to lifting of the soil was higher than other frictional components but the force for accelerating the soil segments was negligible. Maximum cutting resistance occurred between 11 and 15 degrees of inclination angle.

McKyes, et. al. (24) used the equilibrium mechanics approach to develop a mathematical model for inclined narrow blades. This approach was based on straight-line failure planes and is a simplified and advantageous method compared with the log-spiral method for curved failure planes reported by Payne. Draft force was observed to increase with increases in rake (lift) angles, for a given depth to width ratio, in the same soil condition. Field results were in agreement with the model. Osman (27) investigated the influence of curvature of soil cutting blades on draft by using the Coulomb equation to develop his theory based on the passive earth pressure and Ohde's graphical logarithmic spiral. Dimensional analysis was used to handle the large number of variables. Osman showed that draft force increases with increases in rake angles for angles greater than 30 degrees. At low rake angles and under the same soil conditions, the draft forces for flat and curved blades were almost equal but the manner of soil movement on each blade type was different.

Luth and Wismer (23,47) continued with the work of Soehne and Kawamura. Various lift angles and widths of inclined tools were investigated in purely frictional and purely cohesive soils. Results obtained were comparable with earlier work on this tool type.

2.4 Tillage Sweep Design

Information currently obtainable on tillage sweeps deal more with their application than with their optimum design characteristics. In the past, practical knowledge of plane blades was utilized in the fabrication of this tool type but recently, the need to optimize their design to achieve better performance has necessitated further theoretical development. This, coupled with the need for effective weed control on lands prone to wind erosion, led to the design and manufacture of large sweeps called undercutters.

Sirohi (40) studied the influence of the geometric elements of several sweeps on draft. The influence of slide angle, nose angle, tool width and tool surface area on draft force were studied. The optimum slide angle was found to occur between 13 and 15 degrees for the range of speeds used. This result is in close agreement with what was obtained for plane blades (23,42,47). The nose angle was found to influence the slide angle and the surface area of each tool. The nose and slide angles investigated were within the ranges of 60 and 120 degrees and 4.5 and 31 degrees respectively. Only nose angles between 60 and 100 degrees were used to establish the functional relationships for the draft force. The overall widths of the tools varied between 102mm. and 508mm., but the lift height was fixed for all tools. The maximum velocity was about 15.84 km/hr.

Several Russian authors have researched basic design parameters for tillage sweeps. Sineokov (38) pioneered the development of design parameters for cultivator sweeps for use in soil loosening and in removal of weed plants by means of undercutting. Thedesigns of arrow-shaped undercutting sweeps were based on the nose angle (2γ), angle of mounting of the wings to the horizontal plane (β), slide angle (θ), wing width (w), and the overall width (W) of the tool (Fig. 2.1). He selected the nose angle based on the frictional angles of weed plants on metal, ϕ_w, along the cutting edge of the tool. He said that if $\gamma < (90-\phi w)$ there is undercutting of weeds but if $\gamma > (90-\phi w)$ clogging of the cutting edge would result. From his experimental work he found this frictional angle to lie between 22 and 45 degrees. This mathematical relationship was widely accepted and used by other Russian researchers.

Tsymbal (43) however argued that it is the soil-metal frictional angle, δ, and not that of weeds on metal that should be used in this

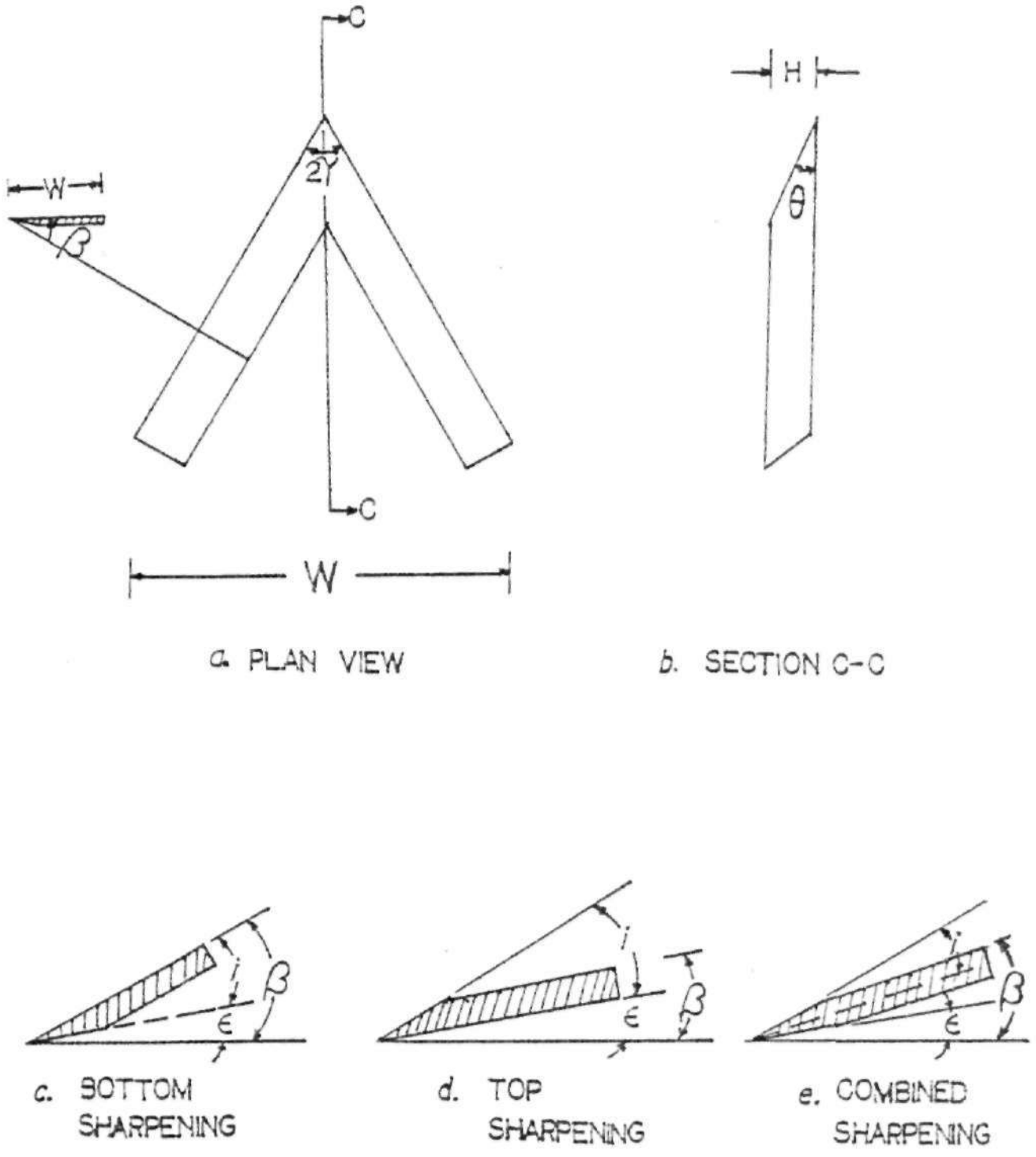


Fig. 2.1 Geometric Elements of an Undercutter

relationship. This is because of the predominance of soil in the soil mass containing weeds, and as such the coefficient of the weed stems on steel is always less than that of soil on steel. Moreover, the weeds in a soil mass cannot slide off the cutting edge earlier than the soil. He therefore modified the established relationship to:

$$2\gamma \leq 2(90 - \delta) - \Delta\gamma$$

where $\Delta\gamma$ = correction angle = 10^{o}

This modified equation guarantees the sliding of soil and weeds along the cutting edge and it is most applicable to the design for optimum nose angles of undercutter sweeps.

Another parameter investigated was the angle of mounting of the wing planes to the horizontal plane, β. For good undercutting of weeds, the angle of cutting, β_o, must be minimal. β_o is defined as:

$$\beta_o = i + \varepsilon$$

where i = the sharpening angle of the tool

ε = the back angle of cutting or the angle of the gap

Sineokov used β to determine the amount of crumbling or fragmentation caused by the sweep. He found that its selection is related to soil type and the nature of cutting edge sharpening. For β less than 15 degrees, it is recommended that the sharpening should be at the top face of the wings. Combined sharpening is recommended for β between 15 and 25 degrees, and sharpening should be on the bottom when β is greater than 25 degrees (Fig. 2.1). It has been established that the soil moves parallel to the direction of forward travel of sweeps, along the sweep's slide angle. This observation is significant to the study of the acceleration and frictional forces. The optimum combination of these tool parameters depends on the amount of soil crumbling desired and the draft force.

2.5 Application of Similitude Techniques to Tillage Research

In recent years, the similitude approach to scale-model testing for the prediction of prototype tillage tool performance has become very popular. This approach has to a great extent simplified the otherwise complex procedure of developing functional relations for model-prototype designs.

Similitude techniques, according to Freitag (13), are based on the concept of similarity between a model and a prototype. Two systems are deemed similar if they exhibit geometric, kinematic and dynamic similarities. Geometric similarity is achieved if the two systems are geometrically proportional. Dynamic similarity is achieved if the ratio of forces are the same in the two systems. If geometric and dynamic similarities are achieved then kinematic similarity is, by implication, achieved.

Forces affecting dynamic systems can be identified by constructing a set of dimensionless groups for all system variables with each having equal values in both the model and the prototype. Schafer et. al. (35) stated that for accurate prediction of a prototype tool from a model tool, all variables must be included in the prediction equation and the model design conditions must be satisfied. Failure to achieve equality in one or more design conditions would lead to a distortion of the system.

The inability of the researchers to scale soil variables often leads to distorted models in soil-machine systems. One way of minimizing this problem is by using the same soil for testing both the model and the prototype and explaining the results on the basis of this known phenomenon. The use of dimensional analysis permits the grouping of variables into dimensionless pi terms in accordance with the established

model theory (21,25). The model theory requires that the corresponding pi terms in the model and prototype be equal or scaled to achieve this equality. Schafer et al (35) proposed ways of achieving this equality analytically, experimentally or by using compensated model techniques.

Several tillage researchers have in the past applied similitude techniques to their tillage investigations. Bockhop (4) used this technique in his model-prototype study of disk plows. Other researchers (2,22,45) used distortion factors to determine the magnitude of predictive factors needed to achieve reasonable predictions of tool forces.

The wide application of this technique and its success devolve on the ability of the researchers to characterize and measure pertinent soil variables which often cause distortion.

Chapter III

DESIGN EQUATIONS FOR UNDERCUTTER BLADES

Vector mechanics has been applied in developing the design equations for the undercutter wings. For these derivations, it was assumed that two of the geometric elements ($\gamma, \theta, \beta, \alpha$) are known while the others were developed in terms of these two. It makes no difference which two design parameters were selected for starting as each parameter has a functional relationship with the other.

Due to the symmetry of undercutter-sweeps, one wing can be used to establish the design equations. The angle between the wing of the tool and the xy (horizontal) plane, defined by β, can be redefined in terms of γ and θ, thus:

a) $\beta = f_1(\gamma, \theta)$

From Fig. 3.1(a), the vectors A and B and be defined as:

$$\bar{A} = \begin{Bmatrix} -\cos\gamma \\ \sin\gamma \\ 0 \end{Bmatrix} \quad \text{and} \quad \bar{B} = \begin{Bmatrix} -\cos\theta \\ 0 \\ \sin\theta \end{Bmatrix}$$

The cross product between $\bar{A}$ and $\bar{B}$ ($\bar{A} \times \bar{B}$) is perpendicular to the plane of the wing as shown in Fig. 3.1(b). The components of vector C in the x, y and z directions are:

$$\bar{C} = \bar{A} \times \bar{B} = \begin{Bmatrix} \hat{i} & \hat{j} & \hat{k} \\ -\cos\gamma & \sin\gamma & 0 \\ -\cos\theta & 0 & \sin\theta \end{Bmatrix} = \begin{Bmatrix} \sin\gamma\sin\theta \\ \cos\gamma\sin\theta \\ \sin\gamma\cos\theta \end{Bmatrix} \quad \begin{Bmatrix} x \\ y \\ z \end{Bmatrix}$$

$\cos\beta$ is the z component of $\bar{C}$ divided by the magnitude of $\bar{C}$:

$$\cos\beta = \frac{\bar{C}_z}{|\bar{C}|} = \frac{\sin\gamma\cos\theta}{(\sin^2\theta + \sin^2\gamma + \cos^2\theta)^{1/2}}$$

and

$$\beta = \cos^{-1}\left\{ \frac{\sin\gamma\cos\theta}{(\sin^2\theta + \sin^2\gamma + \cos^2\theta)^{1/2}} \right\} \qquad \text{(i)}$$

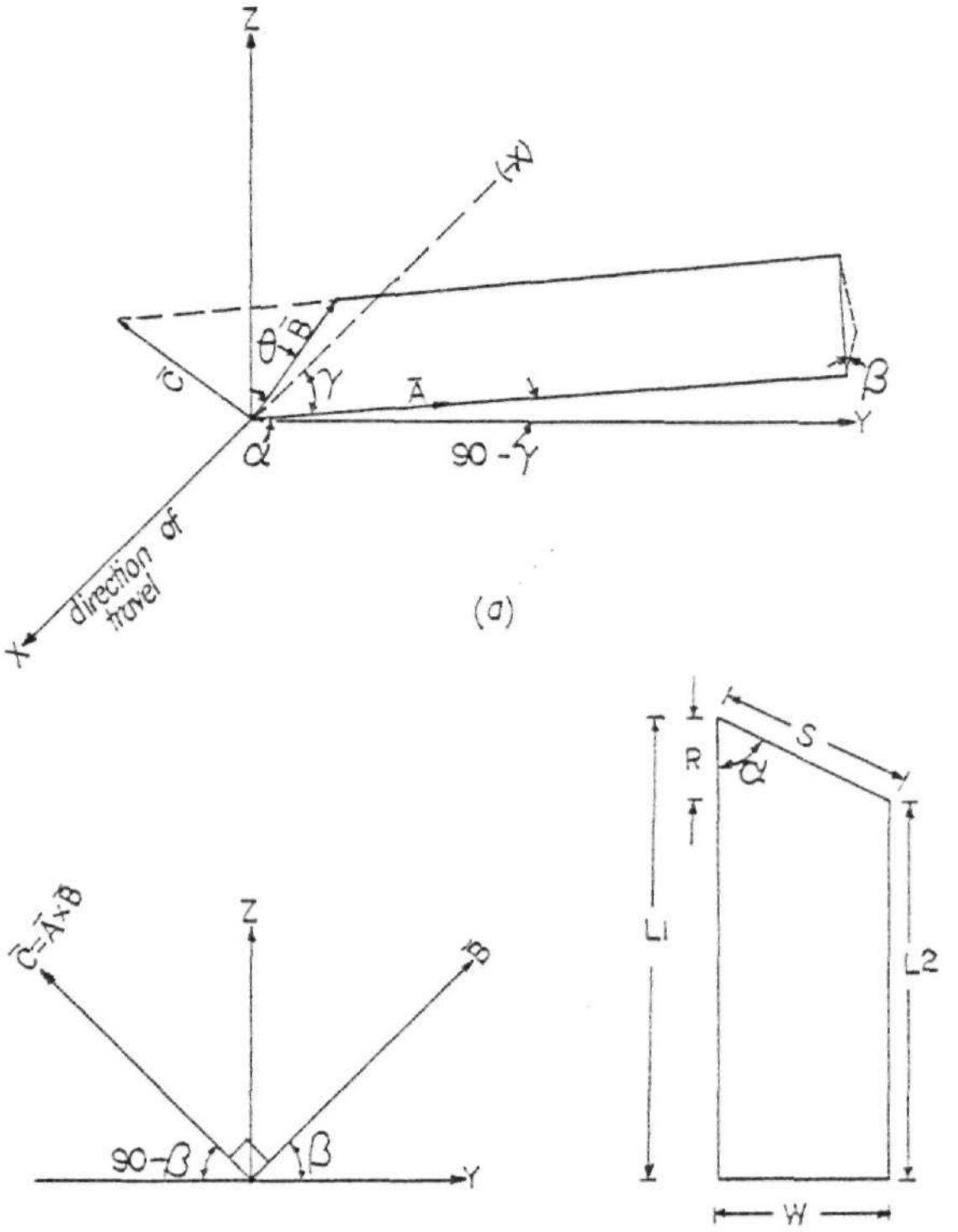


Fig. 3.1 Design Parameters of an Undercutter Wing

Similarly, $\sin\alpha$ is the magnitude of $\bar{C}$:

$$\sin\ \alpha = (\sin^2\gamma\sin^2\theta+\cos^2\gamma\sin^2\theta+\sin^2\gamma\cos^2\theta)^{1/2}$$

$$\alpha = \sin^{-1}(\sin^2\theta+\sin^2\gamma\cos^2\theta)^{1/2} \qquad \text{(ii)}$$

b) $\alpha = f_2\ (\gamma,\beta)$

A shown above,

$$\sin\alpha = (\sin^2\theta+\sin^2\gamma\cos^2\theta)^{1/2}$$

$$\alpha = \sin^{-1}(1-\cos^2\gamma\cos^2\theta)^{1/2} \qquad \text{(iii)}$$

and

$$\cos\beta = \frac{\sin\gamma\cos\theta}{(1-\cos^2\gamma\cos^2\theta)^{1/2}}$$

$$\cos^2\beta = \frac{\sin^2\gamma\cos^2\theta}{1-\cos^2\gamma\cos^2\theta}$$

hence

$$\cos^2\theta = \frac{\cos^2\beta}{(\cos^2\beta\cos^2\gamma+\sin^2\gamma)} \qquad \text{(iv)}$$

Substituting (iv) into (iii) yields:

$$\alpha = \sin^{-1}\left\{\frac{\cos^2\beta\cos^2\gamma+\sin^2\gamma-\cos^2\gamma\cos^2\beta}{\cos^2\beta\cos^2\gamma+\sin^2\gamma}\right\}^{1/2}$$

$$\alpha = \sin^{-1}\left\{\frac{\sin\gamma}{(\cos^2\beta\cos^2\gamma+\sin^2\gamma)^{1/2}}\right\}$$

or $$\alpha = \sin^{-1}\left\{\frac{\tan\gamma}{(\cos^2\beta+\tan^2\gamma)^{1/2}}\right\}$$

Using the above relationships and Figures 2.1 and 3.1 respectively, other pertinent relationships can be established as shown below:

Given the lift height of the tool, H, and the tool width, W:

the wing width, $w = H/\sin\beta$

the slide length, $S = w/\sin\alpha$

the major length, $L_1 = W/2.\sin\gamma$

the minor length, $L_2 = L_1 - w/\tan\alpha = L_1 - R$

the surface area of the wing,

$$Aw = 1/2\ \{(L_1 + L_2)w\}$$

and

the total surface area, $A_t = 2Aw$

where $R = w/\tan\alpha = S\cos\alpha$

The above derivations are those that are required for designing an undercutter with the geometric shape illustrated. As the geometry of the tool changes, the pertinent equations would need to be adjusted accordingly.

The geometric elements of each model tool designed were taken into consideration in designing for its sharpening angle and its back clearance angle as shown in Fig. 2.1. The design criterion was such that the optimum back clearance angle, ε, was maintained ($\varepsilon \geq 10^{o}$). A minimum thickness of 1.25 mm was maintained for the cutting edge of each wing.

Chapter IV

MATHEMATICAL MODEL

The development of a theoretical model for predicting draft forces on undercutters is based on the symmetry of the tool. The theory of mechanics of equilibrium has been applied by many authors to the development of equilibrium equations for predicting forces on soil cutting tools and the results obtained were in most cases in close agreement with the experimental results. This procedure assumes a prior knowledge of the type of failure surface on the soil segments being sheared. The draft force on a soil segment is usually determined from an equilibrium analysis involving the angle of inclination of the soil shear surface, ψ, and such relevant soil properties as the frictional angles (soil on soil and soil on metal), soil cohesion and soil bulk volume weight. The geometric elements of the tillage tool and the location of the forces acting on the tool are important for establishing the equations. Vector algebra was employed by Clark, et. al. (7) in developing mathematical analysis for plan undercutting blades. This approach greatly simplified the complexity of the analytical procedure.

As a soil cutting tool moves through the soil, the soil compresses until failure results according to the Coulomb equation. The failure plane is situated at an angle of $(90 - \phi)$ to the minor principal stress plane along a path of least resistance (Fig. 4.3b). This failure angle is $(45 - \phi/2)$ to the minor principal stress plane on the soil segment.

The equilibrium equations for the undercutter can be established by applying vector algebra to the three dimensional analysis of the forces on the tool and the soil segment respectively.

4.1 Forces on the Tool

If the soil is assumed to slide parallel to the direction of travel, along the slide angle, θ, then the force components are those shown below as illustrated in Figure 4.1.

Horizontal force components: $-kb\cos\gamma$, $-\mu'\vec{N}_0\cos\theta$

Side force components: $-kb\sin\gamma$, $kb\sin\theta$

Vertical force component: $\mu'\vec{N}_0\sin\theta$

and the equilibrium force equations are:

Horizontal force: $$F_x = \frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} + \vec{N}_0\cos\theta + kb\cos\gamma \qquad (1a)$$

Side force: $$S = \frac{\vec{N}_0\tan\gamma}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} + kb\sin\gamma \qquad (2a)$$

Vertical force: $$V = \frac{\vec{N}\cot\theta}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} - \mu'\vec{N}_0\sin\theta \qquad (3a)$$

4.2 Forces on the Soil Segment

The force components on the soil segment can be obtained from Fig. 4.2 and by writing the equilibrium equations as follows:

Horizontal force: $$F_x = \frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} + B\cos\psi + \mu\vec{N}_1\cos\psi + cA\cos\psi \qquad (1b)$$

Side force: $$S = \frac{\vec{N}_1\tan\gamma}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} + kb\sin\gamma \qquad (2b)$$

Vertical force: $$V = G + B\sin\psi + \mu\vec{N}_1\sin\psi + cA\sin\psi - \frac{\vec{N}_1\cot\psi}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} \qquad (3b)$$

The cutting resistance components can be obtained from equations (2a) and (2b) as follows:

$$kb\sin\gamma = \tan\gamma\left\{\frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} - \frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}\right\}$$

and

$$kb\cos = \left\{\frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} - \frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}\right\} \qquad (4)$$

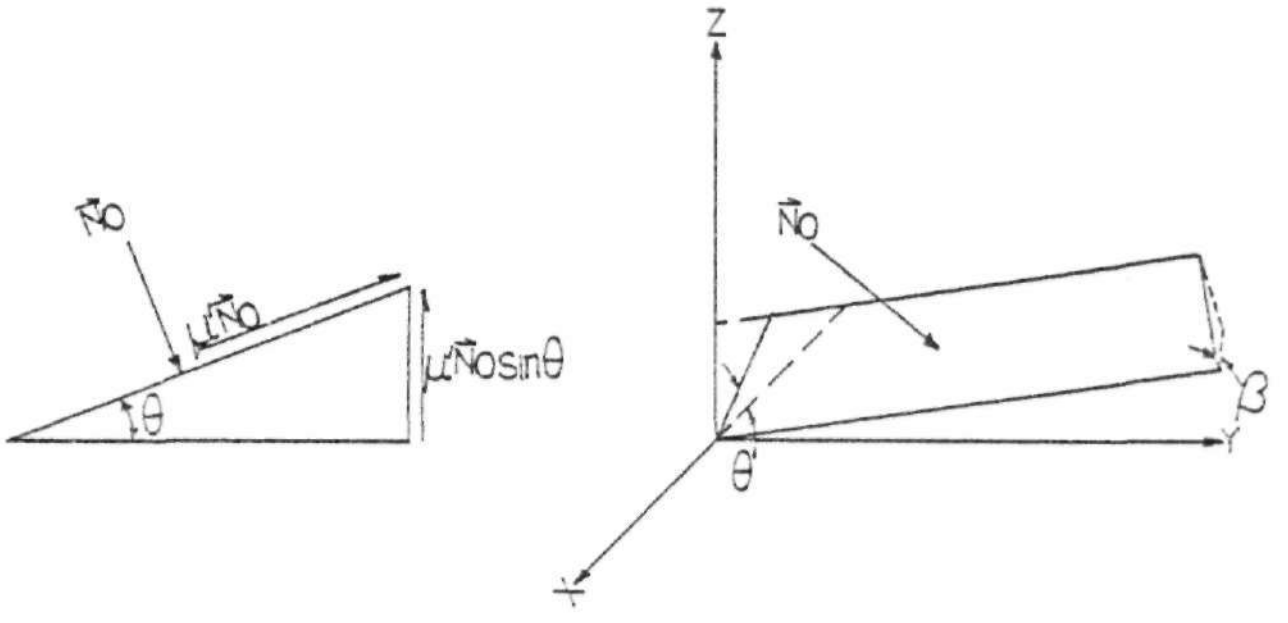


Fig. 4.1 Forces Acting on the Tool

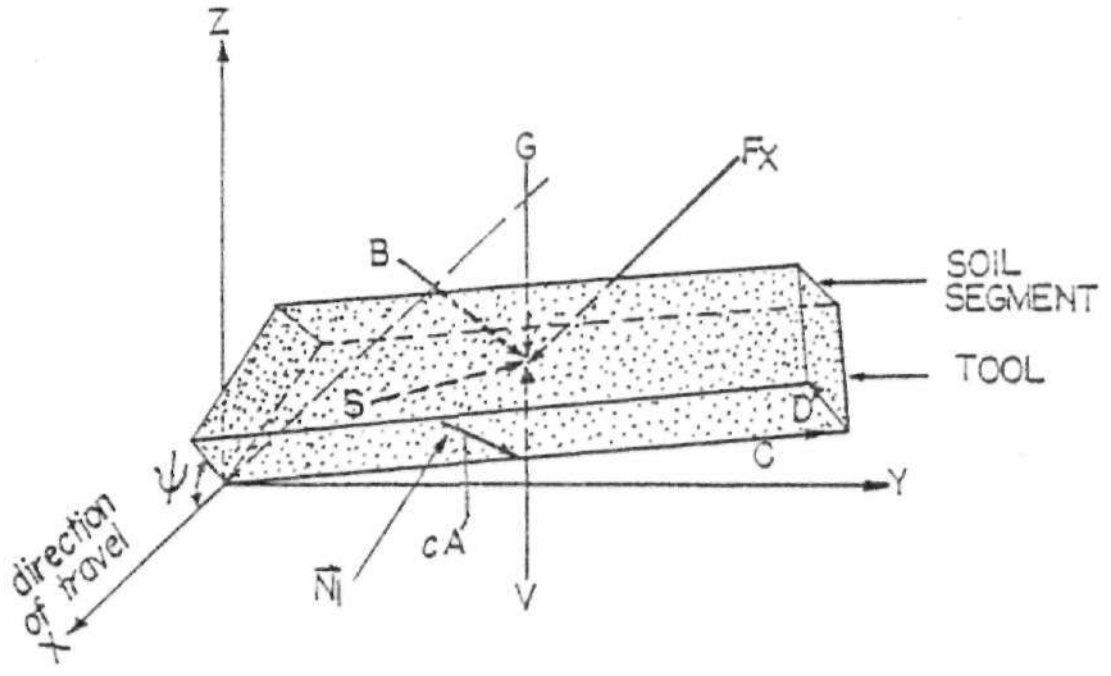


Fig. 4.2 Forces Acting on the Soil Segment

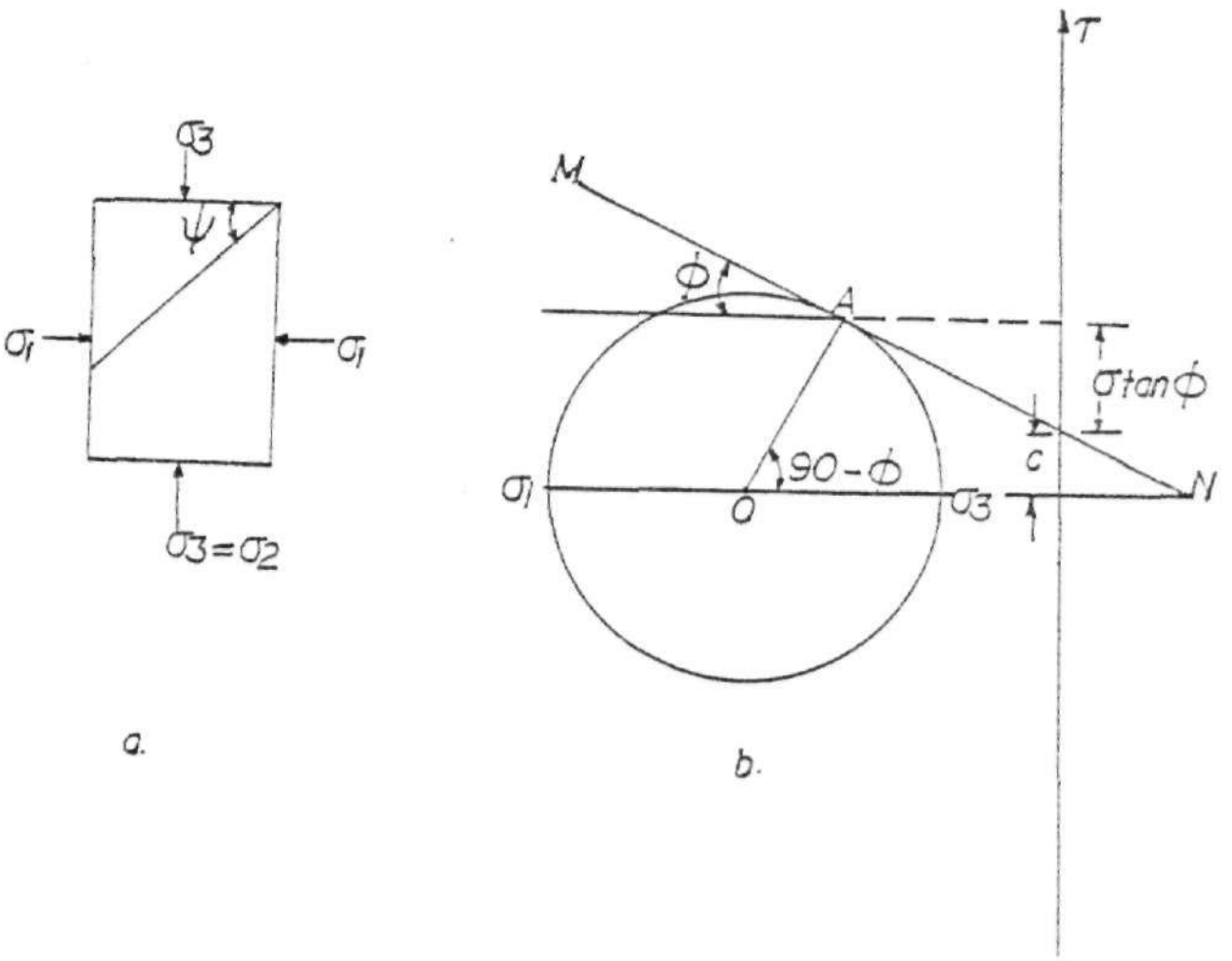


Fig. 4.3 Mohr-Coulomb Failure Diagram

The normal force on the tool, $\vec{N}_0$, can be solved for from equations (1a) and (4) as follows:

$$\vec{N}_0 = \frac{1}{\mu' \cos\theta} \left\{ F_x - \frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} \right\}$$

The normal force on the soil segment is again obtained by rearranging equation (1b):

$$\vec{N}_1 = F_x - \frac{(B + cA)\cos\psi}{\frac{1}{1+\tan^2\gamma+\cot^2\psi)^{1/2}} + \mu\cos\psi} \qquad (6)$$

4.2 Draft Force

From the above equations, the final expression for the draft force can be obtained as given below:

$$F_x = \frac{2}{Z} \left\{ G + (B + cA)\cos\psi \left\{ \tan\psi - \frac{\cot\theta - \mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{(\mu'\cos\theta+\mu'\cos\theta\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}(1+\tan^2\gamma+\cot^2\theta)^{1/2})} + \frac{\cot\psi - \mu\sin\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}}{\mu'\cos\theta(1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2})} \right\} \right\} \qquad (7)$$

where

$$Z = \left\{ \frac{\cot\theta - \mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}} + \left\{ \frac{\cot\psi - \mu\sin\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}}{\mu'\cos\theta(1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2})} \right\} - \frac{\cot\theta - \mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}\ (\mu'\cos\theta+\mu'\cos\theta\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}} \right\}$$

The approach described by Soehne (42) was used for obtaining the weight of the soil segment and the acceleration force on the soil segment respectively as follows:

Weight of the soil segment;

$$G = \rho b \frac{d\sin(\psi+\theta)}{\sin\psi} \left\{ w + d/2 \left\{ \frac{\cos(\psi+\theta)}{\sin\psi} + \frac{\sin(\psi+\theta)\tan\theta}{\sin\psi} \right\} \right\}$$

The failure surface area,

$$A = \frac{bd}{\sin\psi}$$

and

acceleration force;

$$B = \rho/g \; b \; d \; v^2 \; \frac{\sin\theta}{\sin(\psi+\theta)}$$

Details of this mathematical model are given in the appendix. Equation (7) was verified experimentally to see how closely the theoretical model predicted draft force on the undercutters designed.

Chapter V

EQUIPMENT DESIGN

The soil bin facility employed for this investigation consists of the following

1. The test (artificial) soil
2. The soil trough (container)
3. The soil processing carriage
4. The test tool dynamometer carriage
5. The test tools

The test soil is an artificial soil consisting of a mixture of "#520 Oregon Silica" sand, "fire" clay supplied by Hill & Griffith Co., Chicago, IL, and mineral oil (a mixture of "Corvus" and "Almag") in the ratio of 45-45-10 by weight as reported by Schrock (36).

The soil trough was constructed of concrete. It is 15.2 meters long, 114 cm. wide and 60 cm deep. Soil depth is about 40 cm.

The soil processing carriage consists of a rotarytiller, a strike-off blade and a surface roller. The raising and lowering of each component is by a hydraulic cylinder. The rotarytiller is a modified Howard Rotovator powered by a 15 kW., three phase electric motor. Its depth of operation can be varied by means of a hydraulic cylinder. The strike-off blade is mounted between the rotarytiller and the surface roller and serves to level the soil after rotarytilling. Its action is also controlled by a hydraulic cylinder. The surface roller consists of a cylindrical drum which compacts the soil by rolling over it repeatedly. This liquid tight drum is 91 cm in diameter and 110 cm long with an effective weight of 415 kg.

The carriage is pulled by a cable by a hydraulic-motor-driven winch. The winch motor is powered by a pressure compensated pump.

The speed of the motor is controlled by a flow control valve which allows for the selection of speeds between 70 cm/sec and 150 cm/sec. The initial drive cable was 5 mm. (3/16") in diameter but had to be replaced with a 6.35 mm. (1/4") diameter cable due to wear and tear.

The test wheel carriage reported by Schrock (36) was modified to carry the test tool dynamometer. It consists of

a) The rectangular steel tubing frames

b) The dynamometer

c) The tool holder

The rectangular steel tubing frames consist of the base frame which rests on the rails of the soil bin track and is pulled along these rails by the cable drive system. This base frame is provided with solid nylon tire rollers that run at the top, the side and the underside of the rails to provide for the stability and constraint of the carriage.

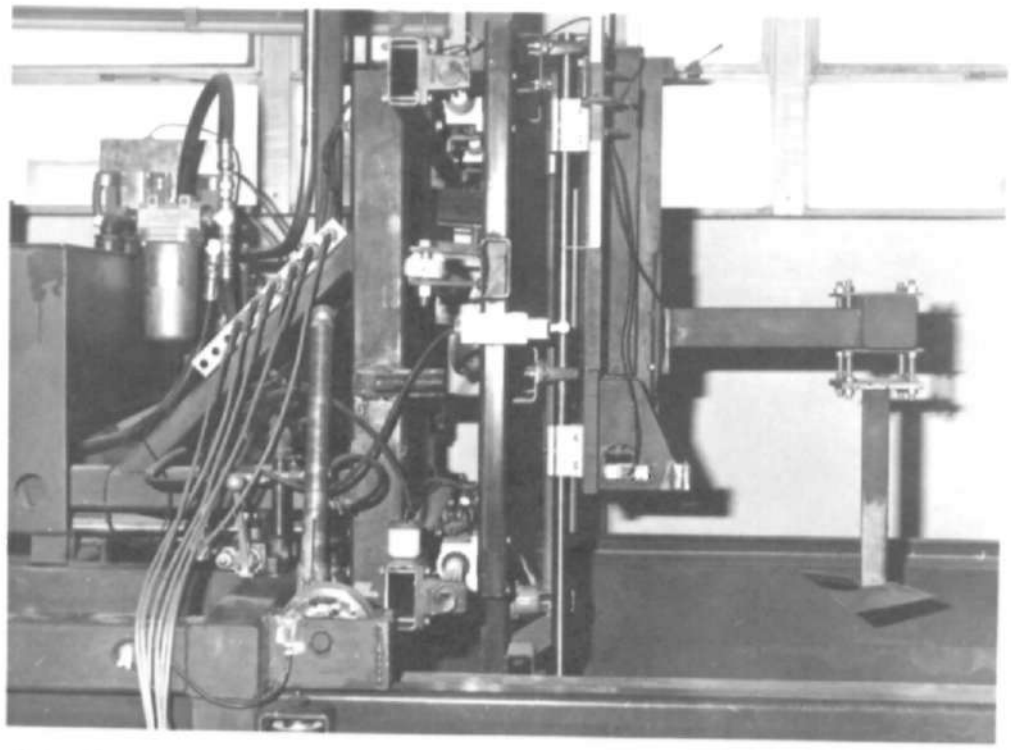
The vertical frame that supports the dynamometer is supported by a pair of Thompson 1060 stainless steel shafts and linear bearing blocks that are bolted on to the base frame. Also bolted to the vertical frame are 32 mm (I.D.) SB-20 shaft support blocks which in turn support two 1060 stainless steel solid shafts. Each shaft is 152 cm long and 32 mm in diameter. These two shafts run across the width of the soil bin and carry the dynamometer through two rectangular tubing frames that are attached to these shafts by means of adjustable ball bushing pillow blocks.

These horizontal shafts also permit lateral movement of the dynamometer across the soil bin. This lateral movement is provided by a CMM-2710 Duff-Norton maxi-pac machine screw type mechanical actuator. Attached to the dynamometer frame through another set of shaft support blocks are two 122 cm solid shafts. These vertical shafts carry the dynamometer which can be lowered into or raised from the soil along these solid shafts by means of a Duff-Norton mini-pac mechanical actuator.

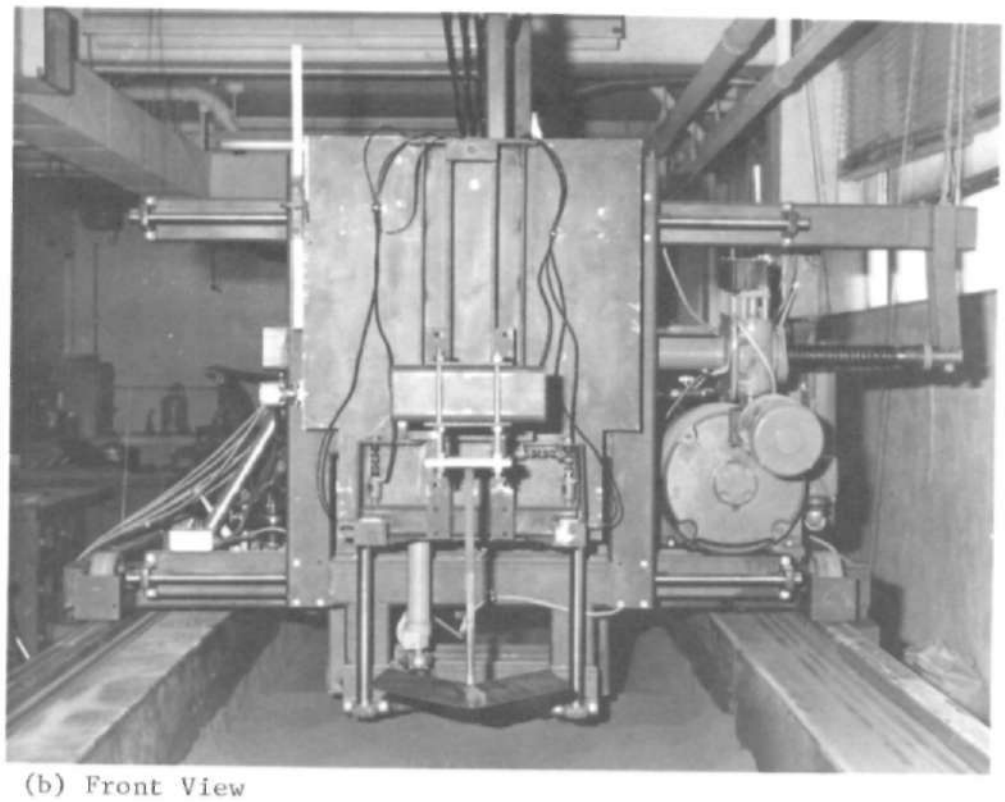
The dynamometer back plate is 2.54 cm thick aluminum. The dynamometer outer (inverted T) frame is bolted to this back plate. Along the vertical face of the inner (inverted T) frame are provisions for bolting the tool holder to the dynamometer. Mounted between the inner and outer (inverted T) frames are the six load cells and their flexures. Three of the load cells are oriented in the horizontal plane, two in the vertical plane and one in the side plane. Four of the load cells were obtained from Transducers Inc. One of these Model 182 tension load cells is rated at 4450 newtons (N) while the remaining three are each rated at 2225 N in capacity. The remaining two load cells were obtained from GSE Inc. These Model 5350 cells are each rated at 4450 N capacity. The entire arrangement is similar to that which exists in the Deere and Company soil bin.

The test tools were constructed from 3.2 mm (1/8") thick cold rolled steel. There is a universal standard which can be bolted to each undercutter tool platform by means of two 4.8 mm. (3/16") bolts. The standard is bolted to the dynamometer tool holder as shown in Fig.5.1.

The method of welding the platform to the underside of the upper junction of the wings of each tool and supported by cross braces as reported by Sirohi (40) was found to be unsatisfactory because of its effect on soil sliding friction. This was particularly true for those tools with small slide angles. This problem was resolved by using a triangular platform. Each model tool has its own platform spot-welded between the two wings and recessed about a quarter of the width of the wing from the upper edges of the wings. This reduces contact between the soil surface and the underside of the platforms and hence minimizes any soil-metal friction and adhesion which would otherwise result.



(a) Side View



(b) Front View

Fig. 5.1 Views of Tillage Tool Dynamometer

The surface area of each platform was minimized but sufficient to position the base of the standard. Two 14.3 mm. (9/16") holes were drilled into each platform parallel to the midrib of each tool. These holes were for bolting the standard to the model tool. The overburden pressure resulting from the accumulation of soil on the platform around the standard could not be completely eliminated without unduely weakening this support and hence is thought to have contributed in some way to the observed draft forces. This was particularly true for those tools with large nose angles and those operating at greater depths.

Chapter VI

EXPERIMENTAL PROCEDURE

6.1 Soil Preparation:

Before any experimental data could be collected on the designed model tools, it was necessary to establish a consistent soil testing procedure and environment. This was achieved by processing the soil in such a way that minimum variation in soil density existed within the bin and within the range of soil depths of interest. Schrock (36) observed some density variations across the soil bin but noted that the variation along the bin was very small. Preliminary investigations confirmed these claims, hence attempts were made to establish a testing procedure that would further minimize the variations across the bin.

The soil was rotary tilled to a depth of 27 cm. The surface was leveled with a levelling blade and rotarytilled a second time to the same depth. The second rotarytilling was followed by the levelling blade. The soil density was then measured at three locations across the bin, 30 cm apart, and along the bin at six locations, 60 cm apart. The Standard Test Method for Density of Soil in Place by the Drive Cylinder Method (ANSI/ASTM D 2937-71) was adopted. A set of cylinders were constructed to remove soil cores from the surface down to a depth of 15 cm in 2.5 cm increments. The soil processing was subsequently repeated and followed by roller passes ranging from one pass to five passes with the soil density measurement taken for each level of compaction. The results of the soil density tests are shown in Fig. 6.1.

6.2 Soil Strength Properties:

Soil strength properties are important to this study from the standpoint of the theoretical analysis where cohesion, coefficient of soil

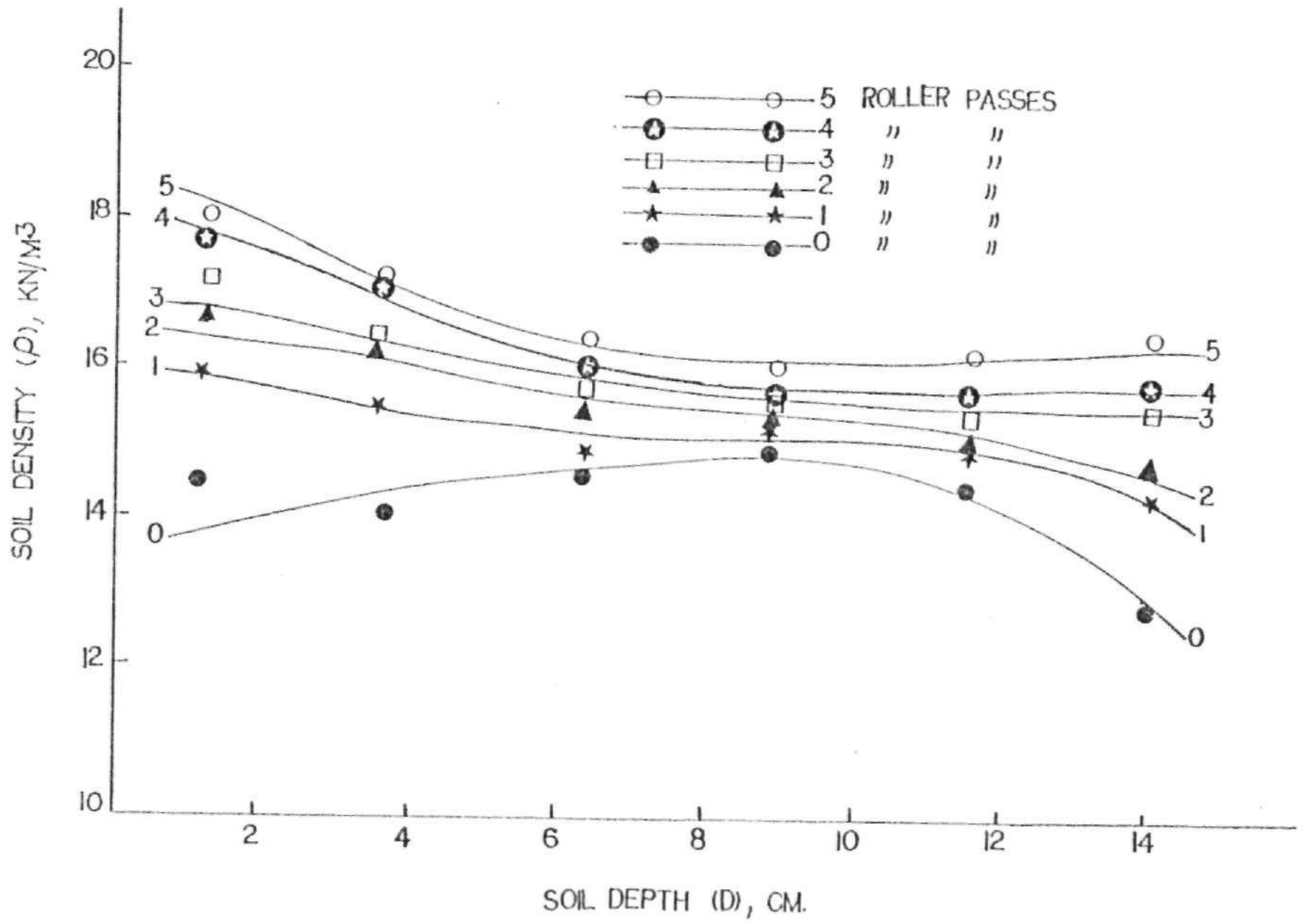


Fig. 6.1 Soil Density Variation with Depth in the Soil Bin

TABLE 6.1

Results of the Periodic Soil Property Tests
Each Value is the Average of Three Readings.

Test Conducted Prior to Test Run No.	Penetrometer Pressures (kPa) Soil, Depth, cm			Soil Cohesion c(kPa)	Soil Frictional Angle (Ø)
10	554.27	765.18	774.01	6.25	29.40
29	557.21	776.95	776.95	6.60	27.96
60	570.94	766.16	788.72	6.65	27.25
86	568.00	765.18	769.10	6.62	28.0
100	561.13	757.33	793.63	6.74	26.95
150	567.02	753.41	783.82	6.75	27.05
172	570.94	760.28	784.80	6.44	28.05

TABLE 6.2

The Central Composite Statistical Design for the Investigation.

	Variable		Levels				
			-2	-1	0	+1	+2
i	Slide angle	(θ,degrees)	10	15	20	25	30
ii	Nose angle	(2γ, degrees)	62.5	75	86.5	100	112.5
iii	Lift height	(H, cm)	1.66	2.30	2.94	3.58	4.22
iv	Soil depth	(D, cm)	1.27	2.54	3.81	5.08	6.35
v	Speed	(V, cm/sec.)	83.0	97.0	111.0	125.0	139.0

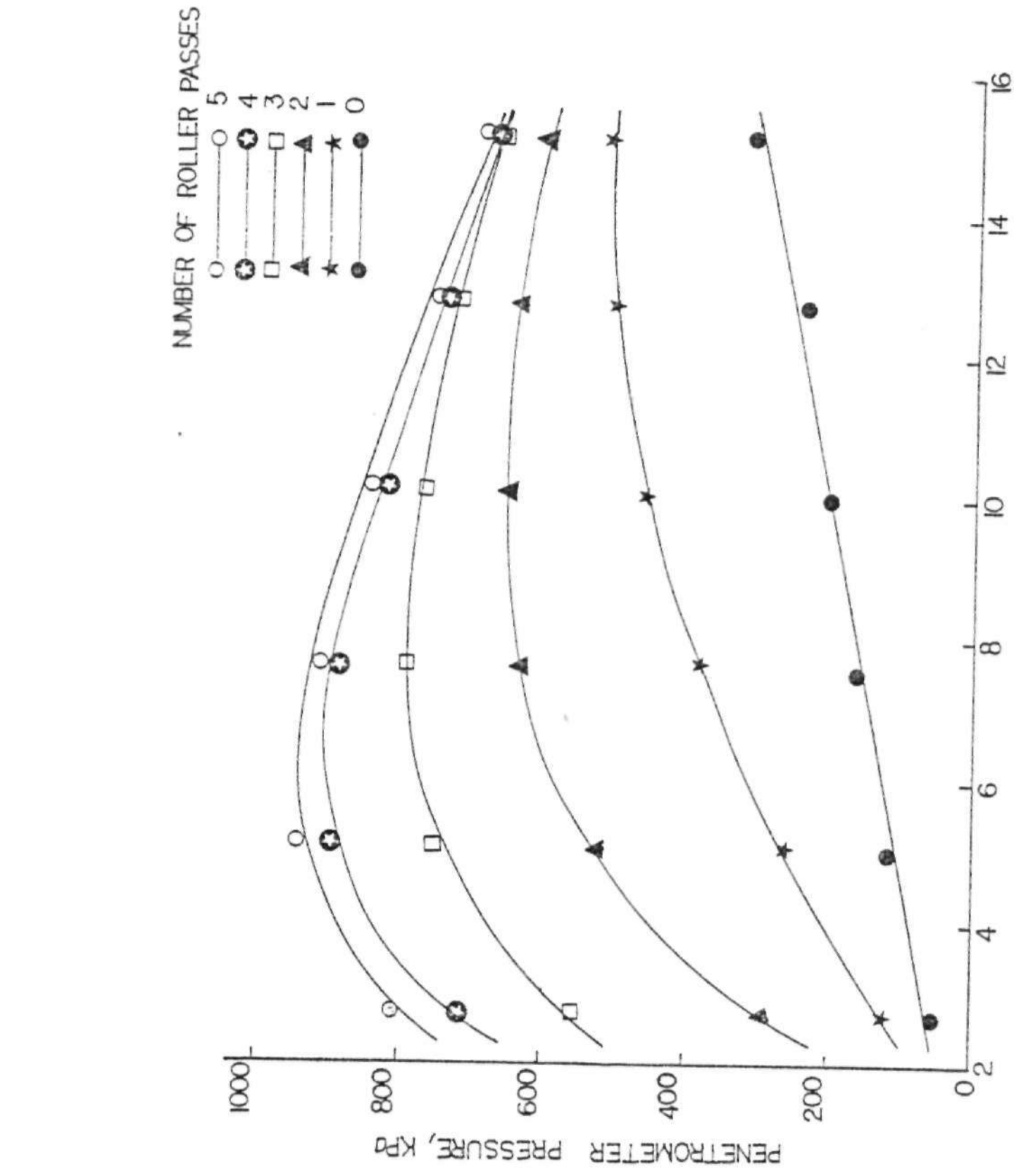


Fig. 6.2 Penetrometer Pressure Variation with Depth in the Soil Bin

shearing resistance, and the coefficient of soil-metal friction are important parameters of the model equations. The methods adopted for investigating these properties are the direct shear test and the insitu test with the Cohron shear graph.

For the direct shear test, the amount of soil sample used was determined from the known soil density and the volume of the direct shear apparatus, excluding the heights of the top and bottom porous plates. The shear machine was calibrated for normal pressures of 96kPa, 192kPa, 288kPa, 384kPa and 480kPa respectively. The corresponding gage pressures were 24kPa, 48kPa, 72kPa, 96kPa and 120 kPa respectively. The prepared sample was fixed in place in the shear unit and the vertical and horizontal dial gages positioned on the machine. The vertical dial gage measured the vertical displacement while the horizontal dial gage measured the horizontal displacement. The shear force corresponding to each normal force was recorded on a chart recorder which continuously plotted the shear force as the test progressed. The shear stress for each test was computed and the peak stress obtained was used for plotting the shear stress normal stress graph as shown in Fig. 6.3. The maximum obtainable strain rate for this machine without excessive vibration was 0.90 mm per minute. Even though this may be low compared to the rate at which a soil is strained during the passage of any tool, the result obtained is not at great variance from that obtained using the Cohron shear graph.

The Cohron shear graph was placed on the surface of the prepared soil and its metal head (cup) introduced into the soil vertically at slow rate. This metal head is equipped with internal vanes to ensure soil-soil shearing action. The shear tests were conducted along the test path at four locations and the results averaged.

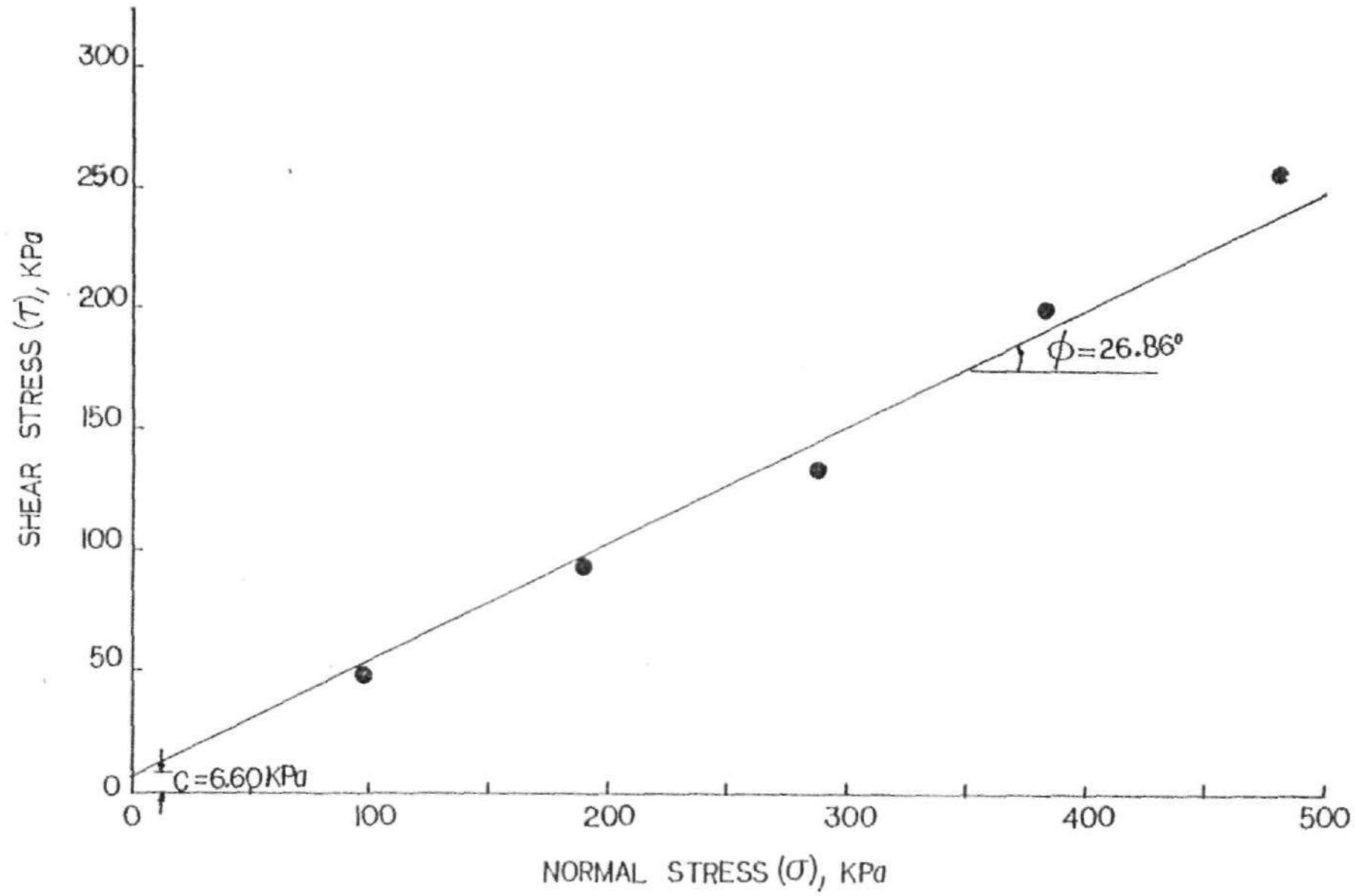


Fig. 6.3 Shear Stress vs Normal Stress Curve for Direct Shear Test on Artificial Soil

The angle of soil-metal friction was also measured directly on the surface of the prepared soil. A metal slider with a surface area of 232 sq. cm was prepared from the 3.2 mm thick cold-rolled steel, the same material used for fabricating the model tools. This plate was loaded with varying known weights and pulled along the soil surface with a calibrated spring type dynamometer. The value of the tangential force corresponding to each normal force was used in computing the tangential stress versus normal stress from which the soil-metal frictional angle and hence the coefficient of soil-metal friction were obtained. The assumption made in the mathematical model that the force of adhesion is negligibly small was confirmed in this test as shown in Fig. 6.4.

The strength distribution in the soil profile was further checked using a hand held cone penetrometer. A 30^{o} cone penetrometer with a 3.20 cm base area was used for the test. With the cone tip placed on the soil and the stem held vertically, the tip was introduced into the soil at a slow rate. Observations were made for cone depths of 0 to 15 cm in 2.54 cm increments, and the results of average penetrometer pressure versus soil depth was plotted as shown in Fig. 6.2. The soil strength consistency was periodically checked with this equipment throughout the conduct of the experiment as presented in Table 6.1.

6.3 Experimental Design:

The primary objective of this study was to investigate how the geometric designs of undercutters, operational speeds and the soil operating depths influence draft performance. A central composite statistical design was found to be best suited for this study. Five levels of tool lift height, nose angle, slide angle, soil depth and operational speed were selected as shown in Table 6.2. The width of 38 cm was used for this study. The range of soil depths and tool speeds were scaled in

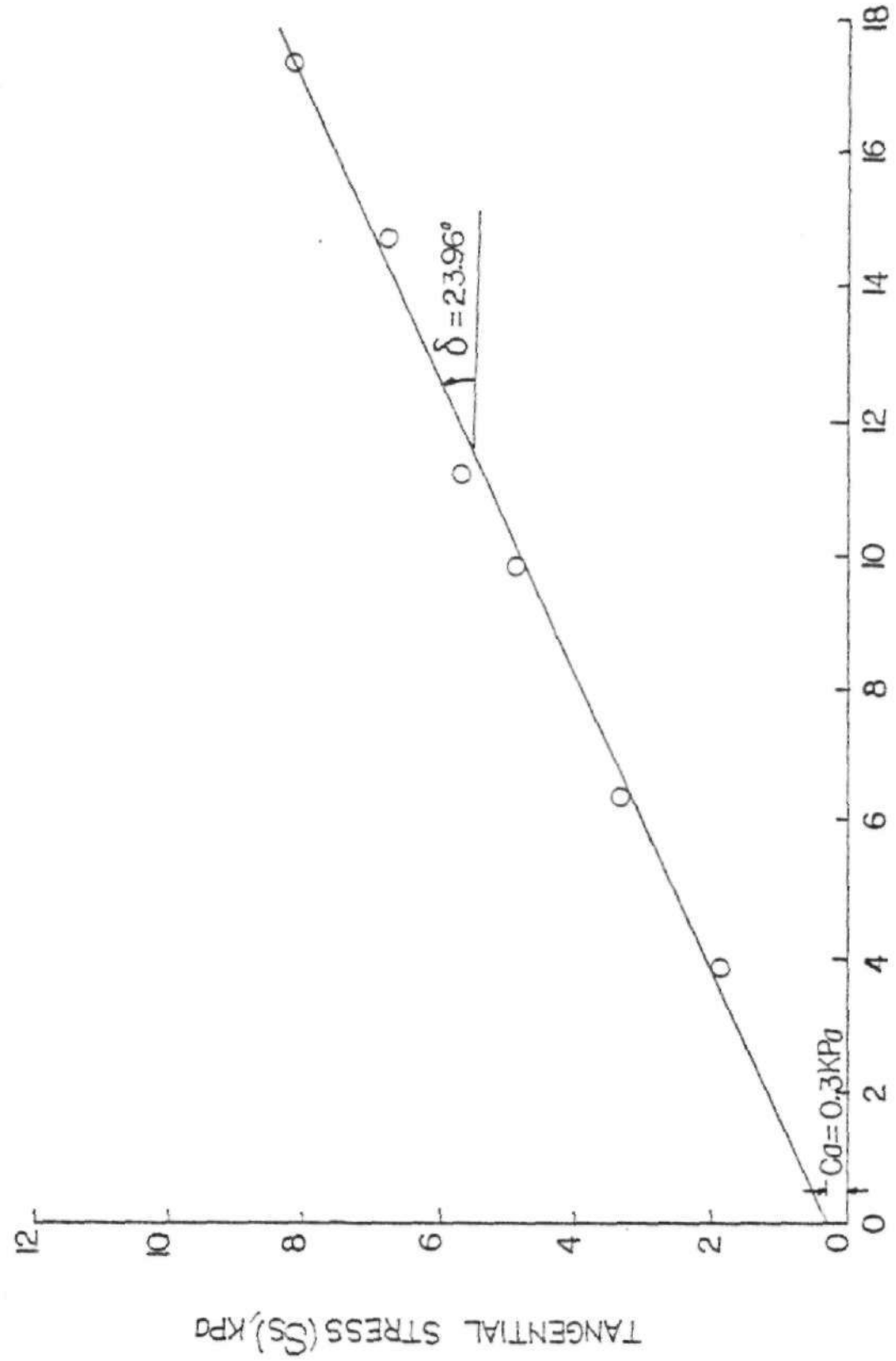


Fig. 6.4 Tangential Stress vs. Normal Stress Curve for Determination of Soil-metal Interface Properties in the Soil Bin

accordance with the scale of model to prototype (true size) used. The speeds were selected by calibrating the flow rate of the hydraulic motor which drives the carriages. The calibration curve is shown in Fig. 6.5. A total of twenty-nine model tools were constructed for this study as shown in Table 6.3 and in Figures 6.6(a)and 6.6(b)respectively.

6.4 Data Acquisition and Reduction:

A SYM-1 microcomputer, manufactured by Synertek Systems Corporation, was used in conjunction with the multichannel recorder for the data acquisition as shown in Fig. 6.7. Each load cell was calibrated prior to its installation by hanging known weights on it and monitoring the corresponding force response with the microcomputer via the recorder. Since there are six load cells, only six channels on the recorder were utilized. The appropriate gain and balance were selected on the recorder and the calibration constant read from the digital display on the microcomputer. The span on the recorder was adjusted to give a voltage reading of 5v to 10v. The zero balance was rechecked after removing the dead weights and the process repeated until consistent values were obtained. The calibration constants were checked periodically during the conduct of the experiment. This single board, 28 key microcomputer was programmed to sample 20 data points per second for five seconds. The test length of the bin is 5 meters. One test run was made for each soil preparation. Prior to each test run, a hole was dug and the model tool lowered to the prescribed depth. The flow rate of the hydraulic motor was then selected and the calibration constants on the microcomputer checked. Data generated from each test run was stored on a cassette tape. This information is in hexadecimal form. It was later transferred into the departmental Digital Equipment Corporation minicomputer via the

TABLE 6.3

Geometric Elements Used for Designing Model Tools

Tool No.	Lift Height H	Slide Angle θ	Nose Angle γ	Tool Width W	Incline Angle β	Bevel Angle α	Wing Width w	Slide Length S	Wing Major Length L1	Minor Length L2	Surface Wing Aw	Area Total At
1	2.30	15.00	37.50	38.10	23.76	39.98	5.71	8.89	31.29	24.48	159.22	318.44
2	2.30	15.00	50.00	38.10	19.28	51.62	6.97	8.89	24.87	19.35	154.02	308.03
3	2.30	25.00	37.50	38.10	37.45	44.03	3.78	5.44	31.29	27.38	110.96	221.92
4	3.58	15.00	37.50	38.10	23.76	39.98	8.89	13.83	31.29	20.69	230.99	461.98
5	2.30	25.00	50.00	38.10	31.33	54.37	4.42	5.44	24.87	21.70	102.99	205.98
6	3.58	15.00	50.00	38.10	19.28	51.62	10.84	13.83	24.87	16.28	223.08	446.17
7	3.58	25.00	37.50	38.10	37.45	44.03	5.89	8.47	31.29	25.20	166.30	332.60
8	3.58	25.00	50.00	38.10	31.22	54.37	6.89	8.47	24.87	19.93	154.23	308.46
9	3.58	20.00	43.75	38.10	27.76	47.25	7.69	10.47	27.55	20.44	184.44	368.88
10	2.30	20.00	43.75	38.10	27.76	47.25	4.94	6.72	27.55	22.98	124.77	249.53
11	2.94	25.00	43.75	38.10	33.99	49.10	5.26	6.96	27.55	22.99	132.89	265.78
12	2.94	15.00	43.75	38.10	21.18	45.75	8.14	11.36	27.55	19.62	191.92	383.83
13	2.94	20.00	50.00	38.10	25.41	52.84	6.85	8.60	24.87	19.68	152.58	305.16
14	2.94	20.00	37.50	38.10	30.87	41.80	5.73	8.60	31.29	24.88	160.93	321.85
15	2.94	20.00	43.75	38.10	27.76	47.25	6.31	8.60	27.55	21.71	155.40	310.95
16	1.66	10.00	31.25	38.10	18.77	32.66	5.16	9.56	36.72	28.67	168.66	337.32
17	1.66	10.00	56.25	38.10	11.97	56.83	8.00	9.56	22.91	17.68	162.41	324.81
18	1.66	30.00	31.25	38.10	48.06	42.24	2.23	3.32	36.72	34.26	79.21	158.41
19	4.22	10.00	31.25	38.10	18.77	32.66	13.11	24.30	36.72	16.26	347.38	694.77
20	1.66	30.00	56.25	38.10	34.78	61.24	2.91	3.32	22.91	21.31	64.36	128.72
21	4.22	10.00	56.25	38.10	11.97	56.83	20.34	24.30	22.91	9.61	330.82	661.64
22	4.22	30.00	31.25	38.10	48.06	42.24	5.67	8.44	36.72	30.47	190.61	381.21
23	4.22	30.00	56.25	38.10	34.78	61.24	7.40	8.44	22.91	18.85	154.49	308.99
24	4.22	20.00	43.75	38.10	27.76	47.25	9.06	12.34	27.55	19.17	211.66	423.31
25	1.66	20.00	43.75	38.10	27.76	47.25	3.56	4.85	27.55	24.25	92.31	184.62
26	2.94	30.00	43.75	38.10	39.86	51.27	4.59	5.88	27.55	23.87	117.94	235.87
27	2.94	10.00	43.75	38.10	14.30	44.65	11.90	16.93	27.55	15.50	256.14	512.27
28	2.94	20.00	31.25	38.10	35.05	36.55	5.12	8.60	36.72	29.82	170.30	340.60
29	2.94	20.00	56.25	38.10	23.64	58.53	7.33	8.60	22.91	18.42	151.52	303.05

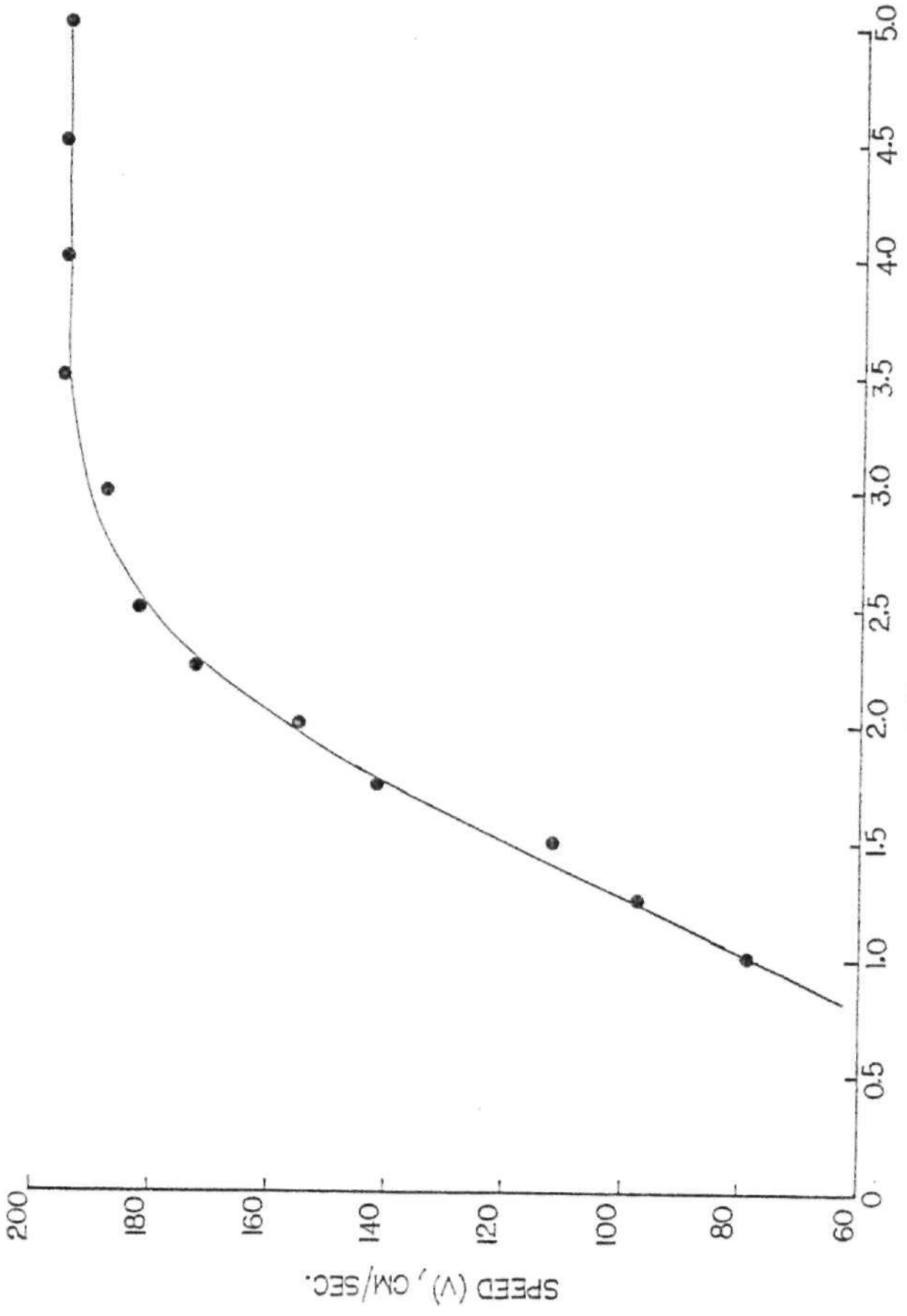
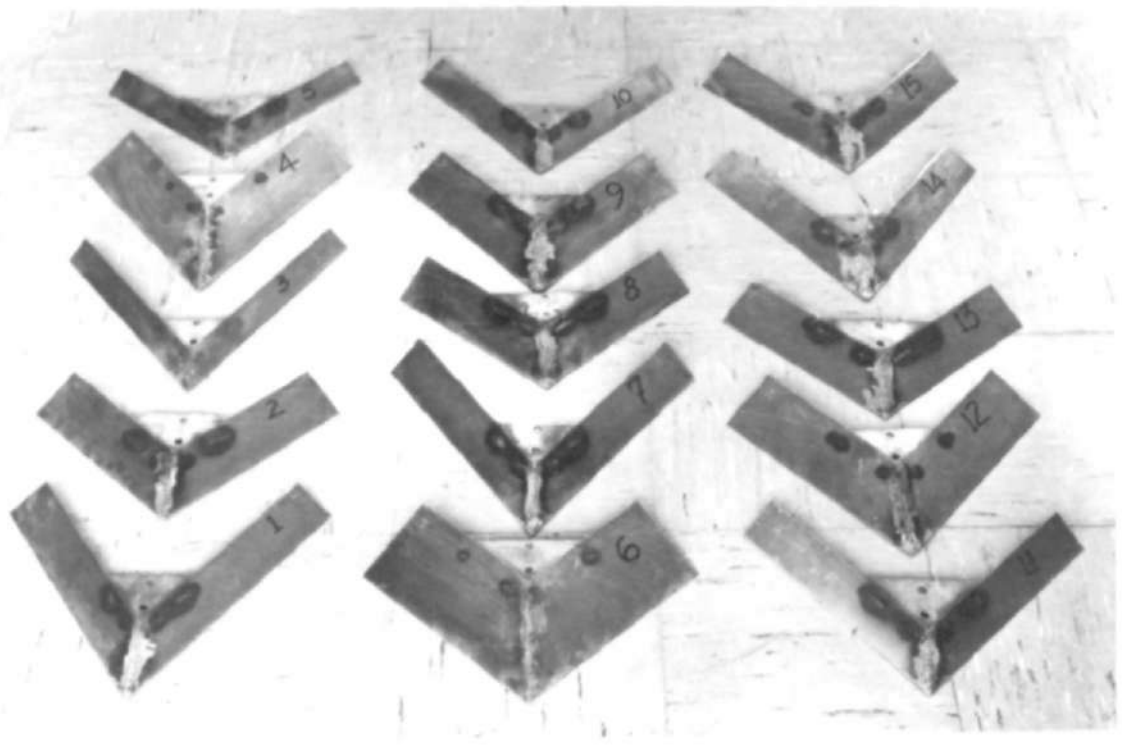
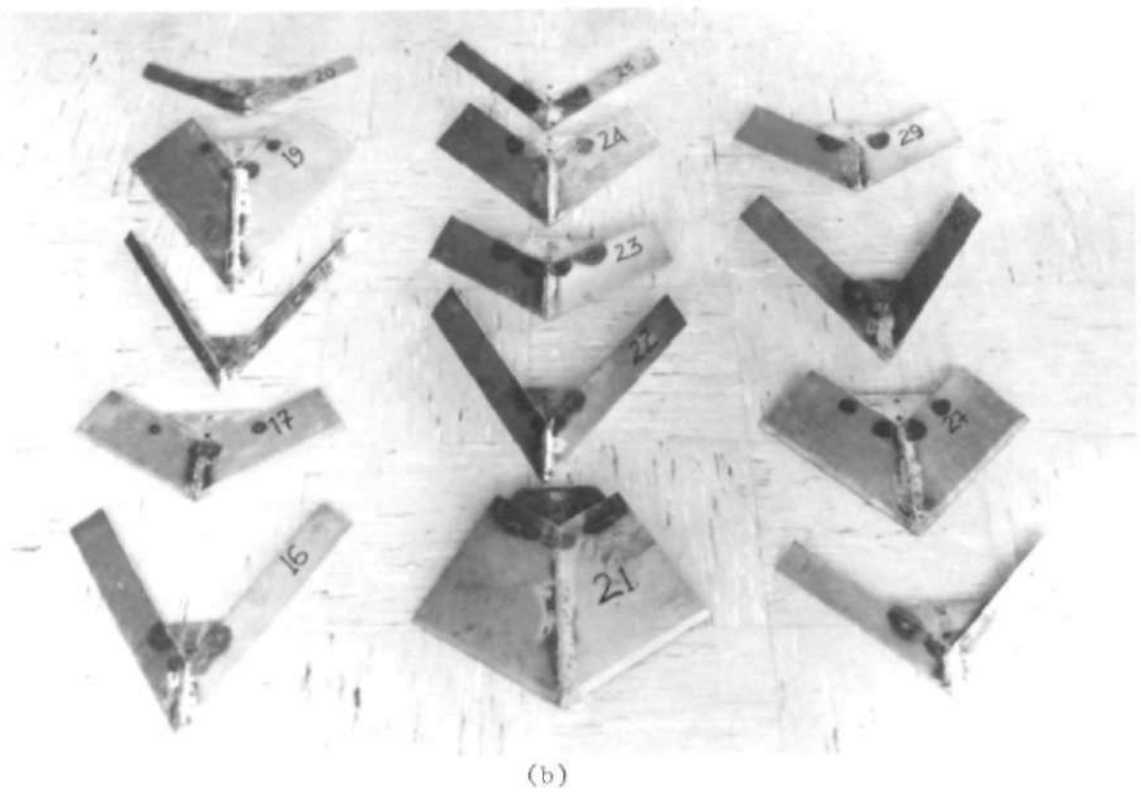


Fig. 6.5 Calibration Curve for the Hydraulic Motor Pump on the Soil Bin



(a)



(b)

Fig. 6.6 Twenty-nine Model Tools Designed for this Investigation

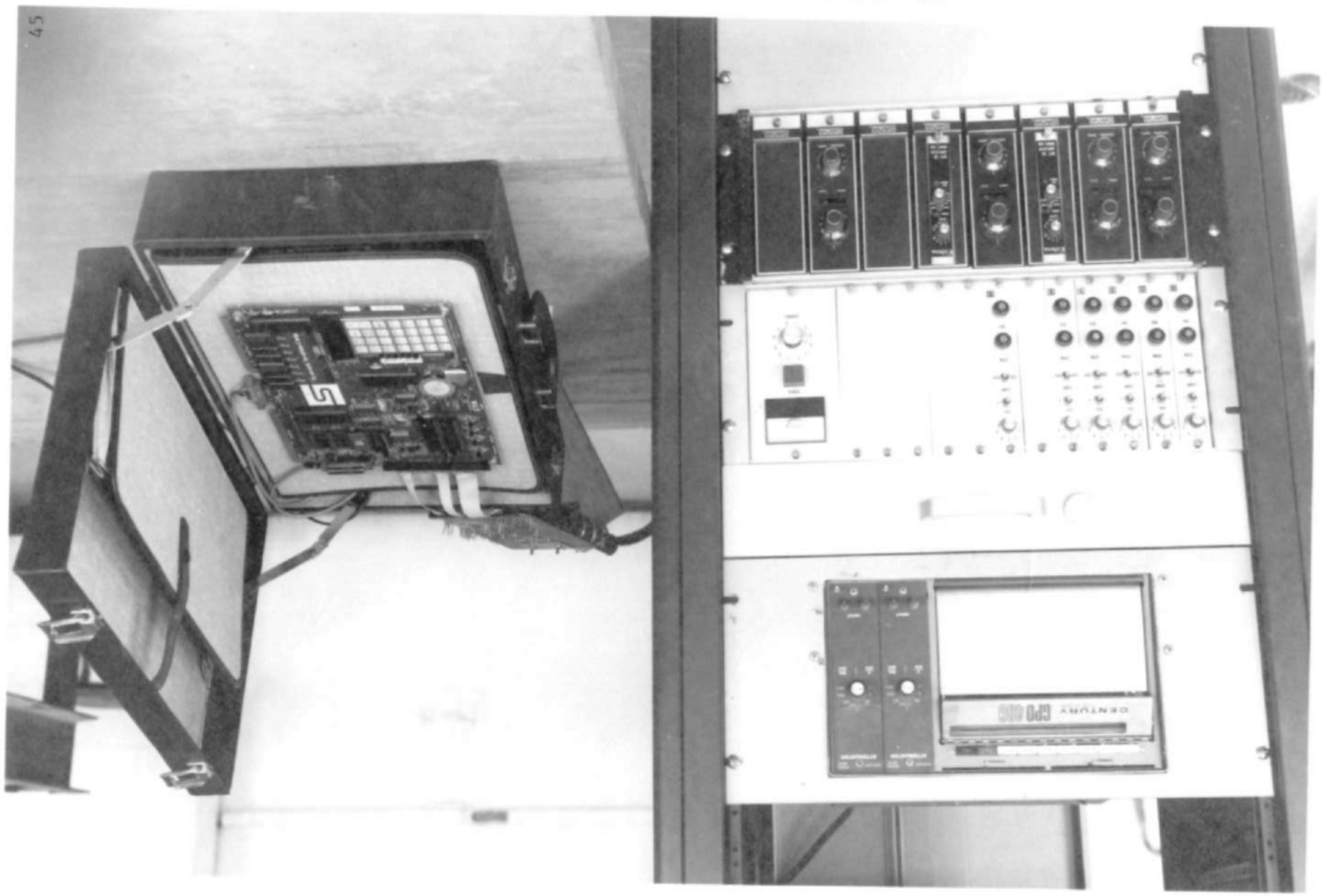


Fig. 6.7 Laboratory Data Acquisition System

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CRT terminal. Data reductions were performed once data were put on the minicomputer. The schematics of the data aquisition system is shown in Fig. 6.8.

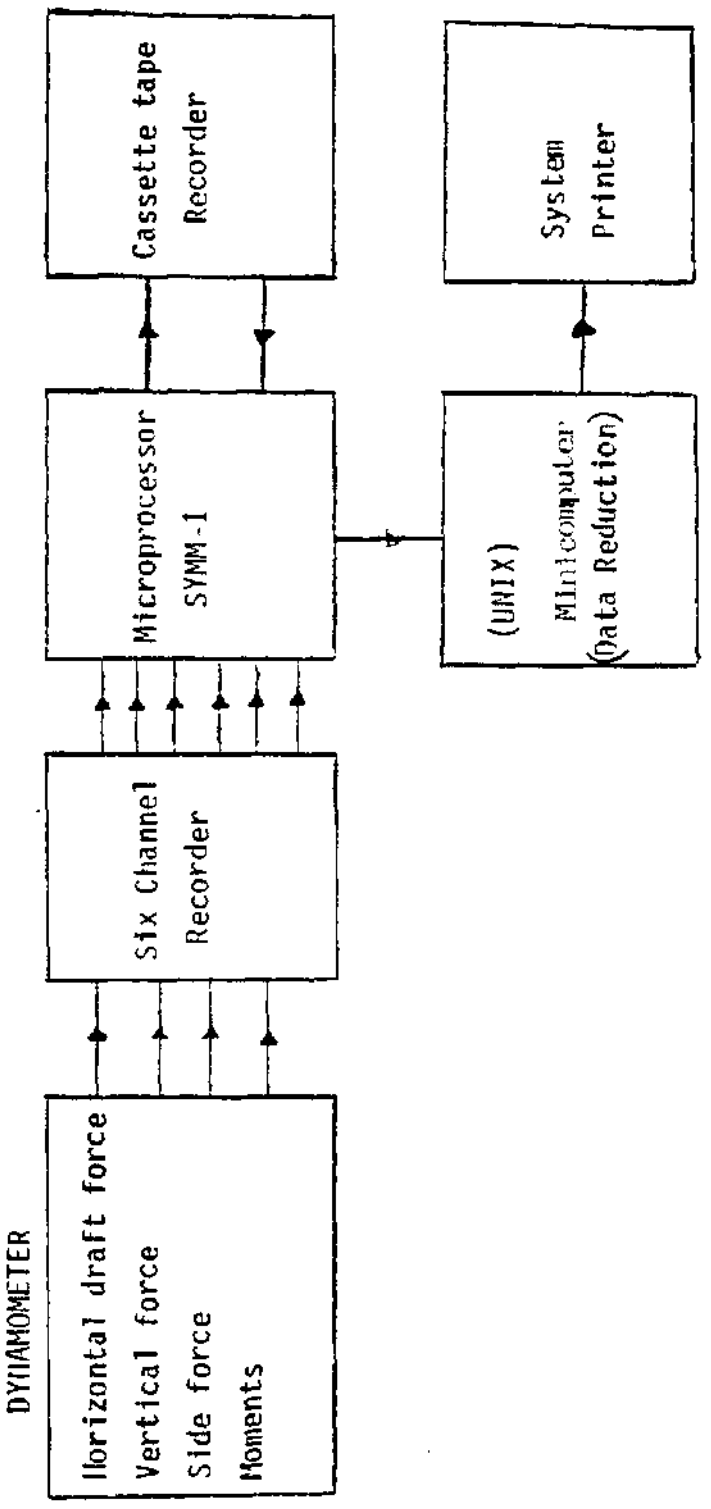


Fig. 6.8 Schematics of Data Acquisition System

Chapter VII

RESULTS AND DISCUSSIONS

The objectives of this dissertation included:

1. Experimental study of the various tool and soil parameters that influence the design and application of undercutters based on their draft power requirement.
2. The verification of an analytical model to predict draft force on this tool type.

7.1 Experimental Study

Prior to the conduct of this experiment, a consistent method of processing the soil was established. Soil density tests were performed to determine variation of soil density with soil depth. Three roller passes provided the least variation with depth. However, greater soil compaction existed at the surface of the prepared soil and an attempt to completely eliminate this was unsuccessful. A direct shear test and cohron shear graph test were employed for the determination of pertinent soil strength parameters.

The average soil density value, obtained for three roller passes, was 15.50kN/m^3. This soil density value was used for the determination of soil strength properties using the direct shear apparatus. The resulting values of soil cohesion and the angle of soil shearing resistance were 6.60kPa and 26.86 degrees respectively. The angle of soil-metal friction was determined on the surface of the prepared soil. Its value was 24 degrees.

Each of the twenty-nine model tools discussed in Chapters V and VI were experimentally tested based on the statistical design for this

investigation. The observed soil failure pattern depended, to a large extent, on the depth of operation and the tool geometry and apparently was influenced little by the range of velocities used. The surface of the soil after running tool No. 15 at 1.27 cm deep and 3.81 cm deep respectively are shown in Figures 7.1 and 7.2. The velocity of operation in both cases was 97 cm/sec. A contrasting appearance of the soil surface was also observed between tool No. 21 and tool No. 22. At shallow depth (1.27 cm) there was little typical soil cutting with tool No. 21 as the tool essentially bulldozed the soil. A smooth even surface was observed for tool No. 22 at this depth. However at greater depth (6.35 cm) a fairly even surface was observed for tool No. 21. while a trough was left in the middle of the worked surface by tool No. 22. It is not exactly clear which of the soil and tool factors were responsible for these conditions but the effects were quite noticeable. The bulldozing effect at shallow depth by some of these tools accounted for the unreasonably high draft forces observed for some of these model tools. A close study of Table 6.3 and Appendix C.7.1 will reveal variations in observed results for the geometric design of each tool. The bulldozing effect of tool No. 21 is shown in Fig. 7.3.

7.2 Analytical Study

The mechanics of equilibrium and vector algebra were employed in establishing the mathematical model equation used to predict draft forces on the model tools. By comparing the resulting draft forces shown in Appendix C (C.7.4 and C.7.5), it can be seen that predicted draft result is, in most cases, lower than observed forces, and the difference is more extreme for some of the model tools at shallow depths. This is possibly due to the observed variations in soil density with depth and the fact that the model results were not subjected to extraneous

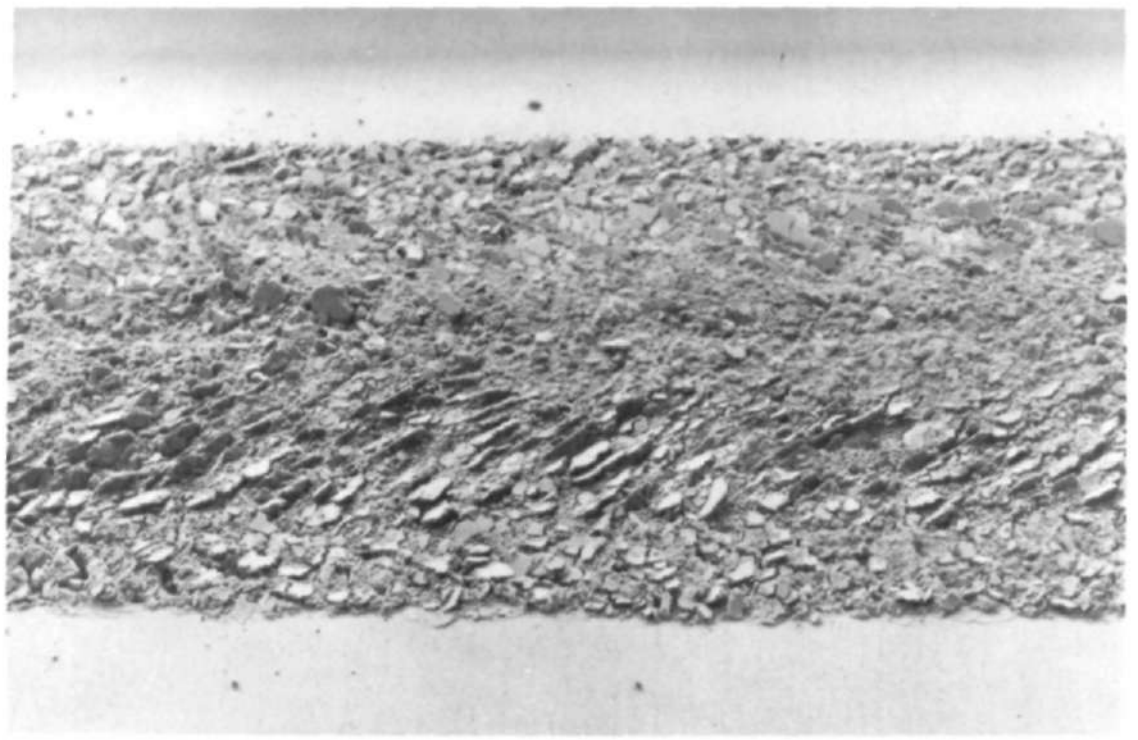


Fig. 7.1 Soil Surface Profile for Model Tool No. 15
Operated at a Soil Depth of 1.27 cm (V = 97 cm/sec.)

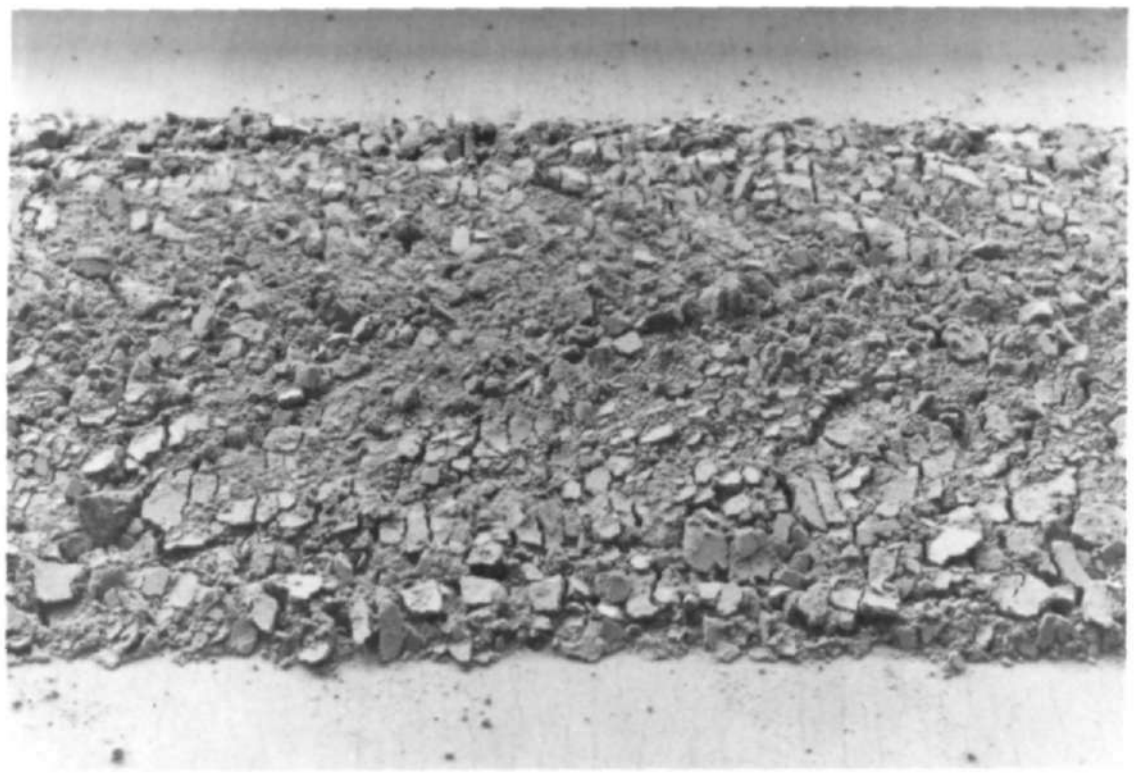


Fig. 7.2 Soil Surface Profile for Model Tool No. 15
Operated at a Soil Depth of 3.81 cm (V = 97 cm/sec.)

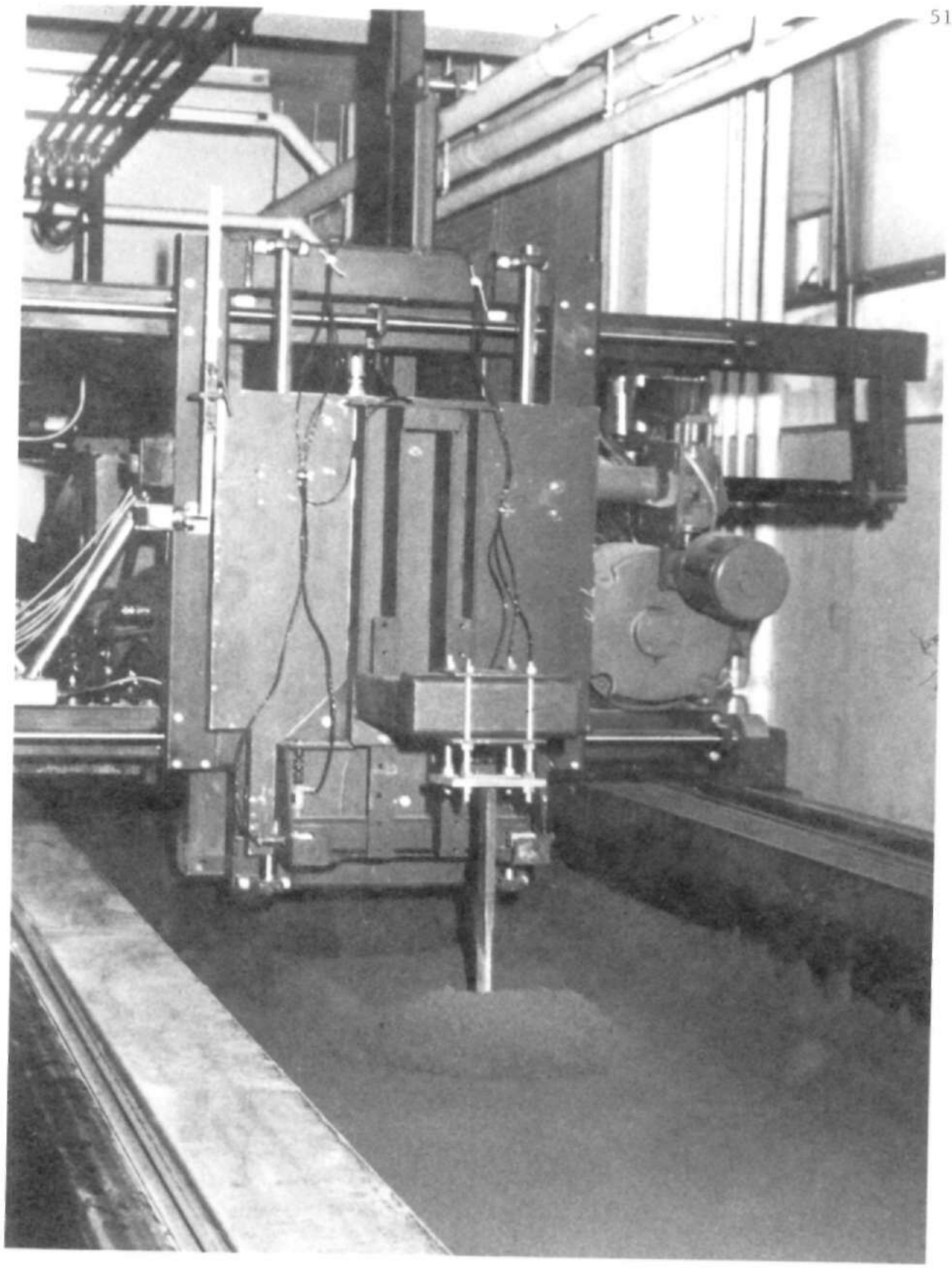


Fig. 7.3 Bulldozing Effect of Tool No. 21 at a Shallow Depth
(D = 1.27 cm V = 83 cm/sec.)

factors to which the experimental model tools were subjected. Since soil shearing resistance is influenced by soil density and soil depth is shown to influence soil density, it is highly probable that soil shearing resistance changed with soil depth. This was assumed to be constant in the mathematical model. The difficulty in modeling soil stress conditions can be advanced to explain the differences in the experimental and theoretical results.

7.3 Statistical Analysis of the Data

The statistical design of this investigation is to provide information on the influence of each of the factors on draft. These factors are soil depth (D), tool velocity (v), tool slide angle (θ), tool lift height (H) and the tool nose angle of the tool (2γ). The central composite design adopted enabled one to study the variations in draft with levels of one factor at selected levels of the other factors. The preliminary statistical analysis of the data using general linear model building techniques showed that the draft force varies exponentially with the factors as revealed by the parabolic form of the preliminary graphs. This suggests that no single factor can be investigated in the absence of other factors.

A model building technique that would include all the first second and third order terms and their interactions was thought best for analyzing these data. This was done through the use of the statistical packages (SAS79) that are available at KSU Computing Center.

A backward elimination procedure was employed for each set of data. The results of these analyses are presented in Tables 7.1 and 7.2. Data shown in Appendix C.7.1 were used in this analysis and a statistical model was developed from the draft (experimental) and

Table 7.1. Backward Elimination Procedure For Experimental Model-Draft

R^2 =0.96774 C(P)=7.05154

	DF	SUM OF SQUARES	MEAN SQUARE	F	PROB>F
REGRESSION	15	1582969.63911	105531.309274	311.96	0.0001
ERROR	156	52772.61526	338.285995		
TOTAL	171	1635742.25437			

	B VALUE	STD. ERROR	TYPE II SS	F	PROB>F
INTERCEPT	82.94588				
D	21.622142	4.872609	6661.287914	19.69	0.0001
Hθ	-1.523795	0.173265	26164.708047	77.34	0.0001
HY	2.018007	0.589905	3958.822879	11.70	0.0008
Dθ	0.364065	0.087685	5831.652206	17.24	0.0001
DY	-0.226995	0.702430	3532.730488	10.44	0.0015
θY	0.269411	0.037031	17904.856956	52.93	0.0001
V^2	0.001018	0.000568	1086.309831	3.21	0.0751
Y^2	-0.262142	0.060524	6346.077436	18.76	0.0001
H^2	0.934627	0.374823	2103.340833	6.22	0.0137
Y^3	0.003527	0.000805	6490.461715	19.19	0.0001
HD^2	2.554007	0.315162	22215.778963	65.67	0.0001
H^2D	-2.646502	0.420004	13431.408620	39.70	0.0001
H^2V	0.018832	0.010476	1093.340997	3.23	0.0741
θY^2	-0.003826	0.000558	15886.743735	46.96	0.0001
HY^2	0.266329	0.106717	2106.936437	6.23	0.0136

Table 7.2. Backward Elimination Procedure For Analytical Model-Pdraft

$R^2 = 0.99966$ C(P)=15.80250

	DF	SUM OF SQUARES	MEAN SQUARE	F	PROB>F
REGRESSION	21	1516344.885533	72206.899311	21107.46	0.0001
ERROR	150	513.137719	3.420918995		
TOTAL	171	1516858.023252			

	B VALUE	STD. ERROR	TYPE II SS	F	PROB>F
INTERCEPT	59.384452				
H	95.969535	5.167248	1180.024095	344.94	0.0001
D	73.057588	1.137782	14079.753740	4115.78	0.0001
Y	-9.226946	2.236396	58.242341	17.03	0.0001
HD	-21.691233	0.849060	2232.722602	652.67	0.0001
HV	-0.077977	0.027066	28.393085	8.30	0.0045
Hθ	-0.184857	0.017489	382.214050	111.73	0.0001
DV	0.045543	0.003131	724.047351	211.65	0.0001
Dθ	0.986968	0.008823	42806.431655	12513.14	0.0001
DY	-0.647564	0.007064	28744.977122	8402.71	0.0001
Vθ	0.009918	0.000786	544.659396	159.21	0.0001
VY	-0.002419	0.000615	52.994927	15.49	0.0001
θY	-0.314296	0.052661	121.856795	35.62	0.0001
H^2	-15.404114	0.888021	1029.365516	300.90	0.0001
θ^2	0.218767	0.058385	48.029697	14.04	0.0003
Y^3	0.212634	0.046796	70.628636	20.65	0.0001
θ^3	-0.002201	0.000991	16.878145	4.93	0.0278
Y^3	-0.001500	0.000342	65.635814	19.19	0.0001
HD^2	0.205670	0.035177	116.943440	34.18	0.0001
H^2D	3.713766	0.136510	2531.875191	740.12	0.0001
H^2V	0.013299	0.004958	24.616250	7.20	0.0081
θY^2	0.003474	0.000602	114.054433	33.34	0.0001

predicted draft data respectively. For the experimental data, the resulting model is:

$$\begin{aligned}\text{Experimental Model, Draft} = {} & 82.946+21.622D-1.524H\theta+2.018HY+0.364D\theta \\ & -0.227DY+0.269\theta Y+0.001V^2-0.262Y^2+0.935H^3 \\ & +0.004Y^3+2.554HD^2-2.647H^2D+0.019H^2V \\ & -0.004\theta Y^2-0.266H^2Y\end{aligned}$$

The R^2 value is 0.96774. This value represents the percentage of total data variation that is explained by the model. Depth is the only single factor in the model which further explains the dorminant role of tillage depth in this investigation. The error mean square for this model is 388.3 and is an indication of the magnitude of extraneous or environmental factors.

The resulting statistically developed model for the predicted (analytical) draft (Pdraft) data is as follows:

$$\begin{aligned}\text{Analytical Model, Pdraft} = {} & 59.384+95.970H+73.058D-9.227Y-21.691HD \\ & -0.078HV-0.185H\theta+0.0455DV+0.987D\theta-0.648DY \\ & +0.010V\theta-0.002VY-0.314\theta Y-15.404H^2+0.219\theta^2 \\ & +0.213Y^2-0.002\theta^3-0.002Y^3+0.206HD^2+3.714H^2D \\ & +0.0133H^2V+0.004\theta Y^2\end{aligned}$$

The R^2 value is 0.99966. This means there is less variation in the total data as explained by the model. This is expected because these data were not collected under the same environment as for the experimental data. The error mean square of 3.4209 confirmed this belief. It should, however, be observed that there are more single factors in the analytical model (Pdraft) equation than in the experimental model Draft equation. This does not make the latter less accurate because these single factors may be significantly present in the interactions.

7.4 Discussion of the Results

The statistically developed model equations were used to generate data presented in Tables 7.3 and 7.4 and those in the Appendix C.7.4 to C.7.5. Data in Tables 7.3 and 7.4 were used in plotting the graphs shown in Figures 7.4 and 7.5 respectively. The main advantage to this is that the equations provide a smoothing of the curves thereby making their interpretations easier. The Figures were for experimental model (Draft) and the analytical model (Pdraft) which represent the observed analytical results respectively.

7.4.1 Influence of Soil Depth on Draft

Figure 7.4 shows the influence of depth of operation on draft for model Draft and model Pdraft respectively. In both cases, increasing the depth of tool operation brings about an increase in draft for given levels of tool lift height, slide angle and nose angle. The range of velocity used to generate the data was 75 cm/sec. to 135 cm/sec. The relationship of depth with draft is parabolic and is represented by the upward shifts in the graphs. The contribution of soil depth to the overall draft is obvious from this figure and from the tables in the Appendix C.7.4 to C.7.5. The draft increase with depth is due to the increase in the weight of soil segment passing over the surface of the tool. This increase in the weight of soil segment results in an increase in the force needed to accelerate and lift the soil segment. Undercutters are usually operated at shallow depths (6-10 cm) aimed at causing minimum disturbance to the wind erosion-prone soils. The importance of depth to these models is further reflected in Tables 7.1 and 7.2 where direct and interactive effects are shown. Depth is, infact, the most dominant single factor in the models.

Table 7.3. Experimental Model(Draft) and Analytical Model(Pdraft) Data
For Different Soil Depths

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
2	15	75	75	92.12	125.64	169.38	223.33	287.50	72.11	112.63	153.96	196.14	239.12
			90	95.77	129.30	173.03	226.99	291.16	72.81	114.01	156.04	198.88	242.55
			105	99.89	133.41	177.15	231.10	295.27	73.51	115.39	158.10	201.63	245.98
			120	104.46	137.98	181.72	235.67	299.84	74.21	116.78	160.17	204.38	249.42
			135	109.49	143.01	186.95	240.70	304.86	74.91	118.16	162.23	207.13	252.85
2	25	75	75	115.94	153.10	200.48	258.07	325.88	87.50	137.89	189.10	241.14	294.00
			90	119.59	156.75	204.13	261.72	329.53	89.69	140.76	192.65	245.37	298.91
			105	123.70	160.86	208.24	265.83	333.64	91.87	143.63	196.20	249.60	303.83
			120	128.27	165.43	212.81	270.40	338.21	94.06	146.50	199.75	253.84	308.74
			135	133.30	170.46	217.84	275.43	343.24	96.24	149.36	203.31	258.07	313.66
3	15	100	75	99.74	129.96	175.51	236.37	312.56	70.85	101.18	132.74	165.54	199.58
			90	104.81	135.03	180.57	241.44	317.63	70.92	101.94	134.19	167.67	202.38
			105	110.33	140.55	186.09	246.96	323.15	71.00	102.70	135.63	169.79	205.19
			120	116.31	146.53	192.07	253.94	329.13	71.08	103.46	137.01	171.92	208.00
			135	122.75	152.97	198.51	259.38	335.57	71.16	104.22	138.51	174.04	210.81
3	25	100	75	100.05	133.91	183.10	247.60	327.43	83.38	123.59	165.02	207.69	251.59
			90	105.12	138.98	188.16	252.67	332.50	84.95	125.83	167.95	211.30	255.89
			105	110.64	144.50	193.68	258.19	338.12	86.51	128.08	170.88	214.91	260.18
			120	116.62	150.48	199.66	264.17	344.00	88.07	130.32	173.80	218.52	264.47
			135	123.06	156.92	206.10	270.61	350.44	89.64	132.57	176.73	222.13	268.77

Table 7.3. Experimental Model(Draft) and Analytical Model(Pdraft) Data For Different Soil Depths (cont.)

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
4	30	110	75	85.13	113.91	163.13	232.78	322.86	91.69	138.93	187.80	238.33	294.50
			90	92.16	120.95	170.16	239.81	329.89	94.05	141.96	191.52	242.73	295.58
			105	99.66	128.44	177.66	247.31	337.39	96.40	145.00	195.24	247.13	300.66
			120	107.61	136.40	185.61	255.26	345.34	98.75	148.03	198.96	251.53	305.74
			135	116.03	144.81	194.03	263.68	354.76	101.10	151.06	202.67	255.93	310.82

TABLE 7.4. Experimental Model(Draft) and Analytical Model(Pdraft) Data
For Different Tool Slide Angles

				DRAFT					PDRAFT				
				SLIDE ANGLE, θ (DEGREES)					SLIDE ANGLE, θ (DEGREES)				
D	H	2Y	V	10	15	20	25	30	10	15	20	25	30
3	2	60	75	135.75	149.09	162.42	175.76	189.09	130.10	137.50	150.89	168.62	189.04
			90	139.40	152.74	166.07	179.41	192.74	131.02	139.16	153.29	171.78	192.92
			105	143.52	156.86	170.19	183.52	196.86	131.93	140.81	159.68	174.90	196.80
			120	148.09	161.42	174.76	188.09	201.43	132.84	142.46	158.08	178.03	200.68
			135	152.12	153.12	179.79	193.12	206.46	133.75	144.12	160.47	181.17	204.56
3	2	75	75	111.92	125.64	139.37	153.10	166.83	108.16	112.63	123.09	137.89	155.38
			90	115.57	129.30	143.02	156.75	170.48	108.80	114.01	125.21	140.76	158.99
			105	119.68	133.41	147.14	160.86	174.59	109.44	115.39	127.34	143.63	162.60
			120	124.25	137.98	151.71	165.43	179.16	110.08	116.79	129.47	146.49	166.21
			135	129.28	143.01	156.74	170.46	184.19	110.72	118.16	131.59	149.36	169.82
3	2	100	75	100.81	110.40	120.00	129.59	139.19	89.41	93.38	103.34	117.64	134.62
			90	104.46	114.06	123.65	133.25	142.84	89.60	94.31	105.01	120.05	137.79
			105	108.57	187.17	127.76	137.36	146.95	89.79	95.25	106.69	122.47	140.95
			120	113.14	122.74	132.33	141.93	151.52	89.98	96.18	108.36	124.89	144.11
			135	118.17	127.77	137.36	146.96	156.55	90.17	97.11	110.04	127.31	147.27

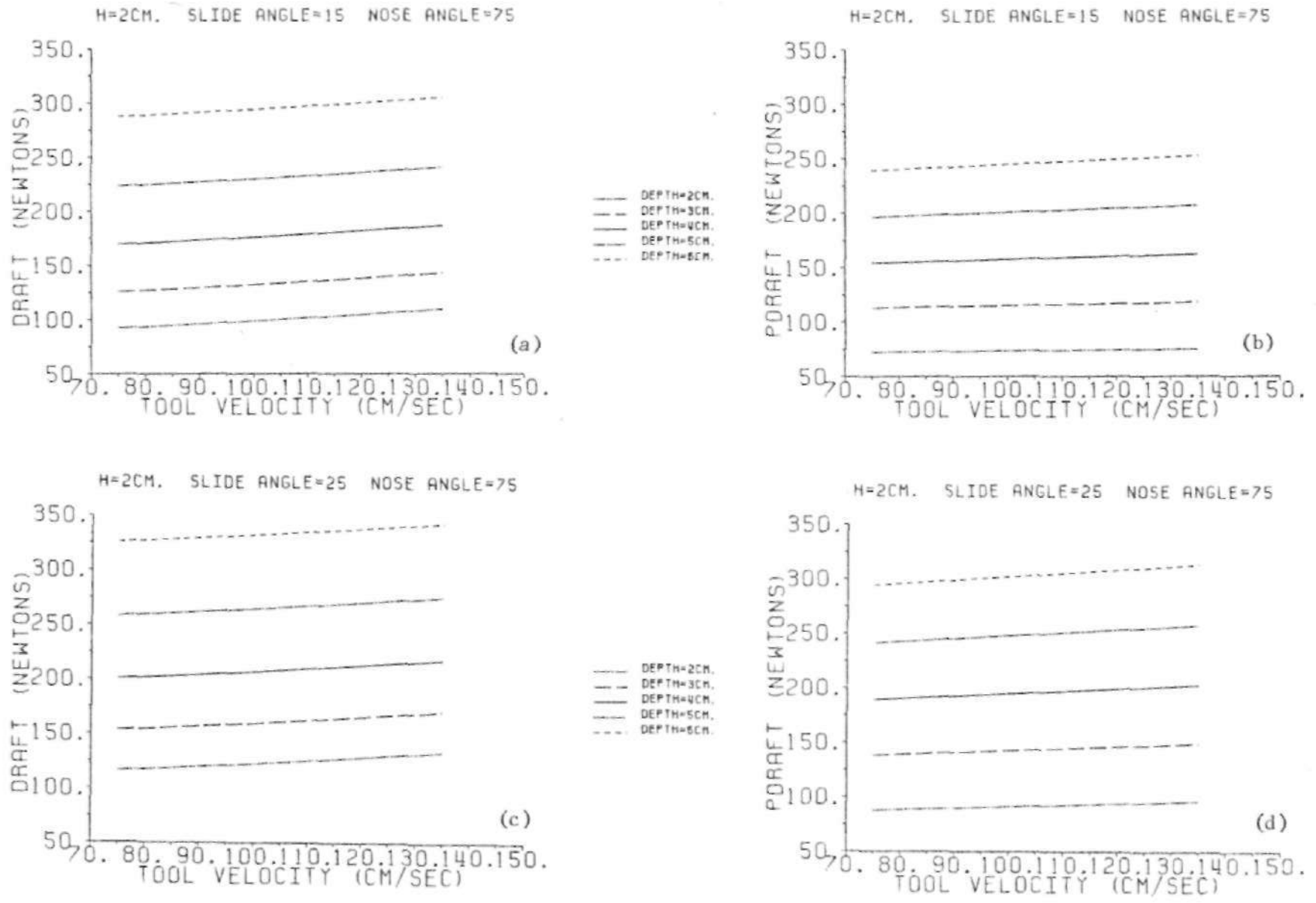


Fig. 7.4 Draft and Pdraft vs Velocity for Levels of Soil Depth

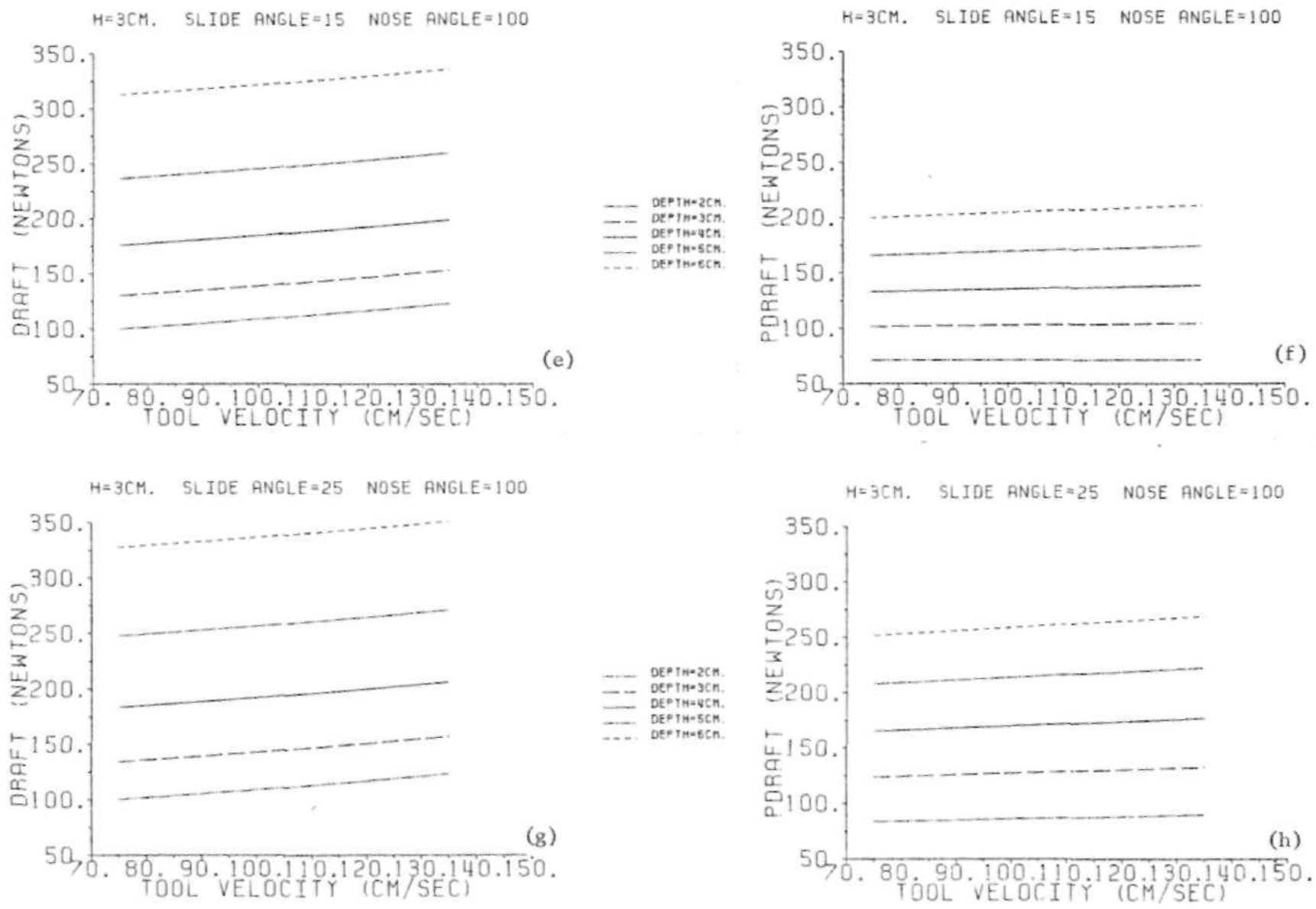

H=3CM. SLIDE ANGLE=15 NOSE ANGLE=100
DRAFT (NEWTONS)
350.
300.
250.
200.
150.
100.
50.
70. 80. 90. 100. 110. 120. 130. 140. 150.
TOOL VELOCITY (CM/SEC)
(e)
DEPTH=2CM.
DEPTH=3CM.
DEPTH=4CM.
DEPTH=5CM.
DEPTH=6CM.
H=3CM. SLIDE ANGLE=15 NOSE ANGLE=100
PDRAFT (NEWTONS)
350.
300.
250.
200.
150.
100.
50.
70. 80. 90. 100. 110. 120. 130. 140. 150.
TOOL VELOCITY (CM/SEC)
(f)
H=3CM. SLIDE ANGLE=25 NOSE ANGLE=100
DRAFT (NEWTONS)
350.
300.
250.
200.
150.
100.
50.
70. 80. 90. 100. 110. 120. 130. 140. 150.
TOOL VELOCITY (CM/SEC)
(g)
DEPTH=2CM.
DEPTH=3CM.
DEPTH=4CM.
DEPTH=5CM.
DEPTH=6CM.
H=3CM. SLIDE ANGLE=25 NOSE ANGLE=100
PDRAFT (NEWTONS)
350.
300.
250.
200.
150.
100.
50.
70. 80. 90. 100. 110. 120. 130. 140. 150.
TOOL VELOCITY (CM/SEC)
(h)

Fig. 7.4 (cont.)

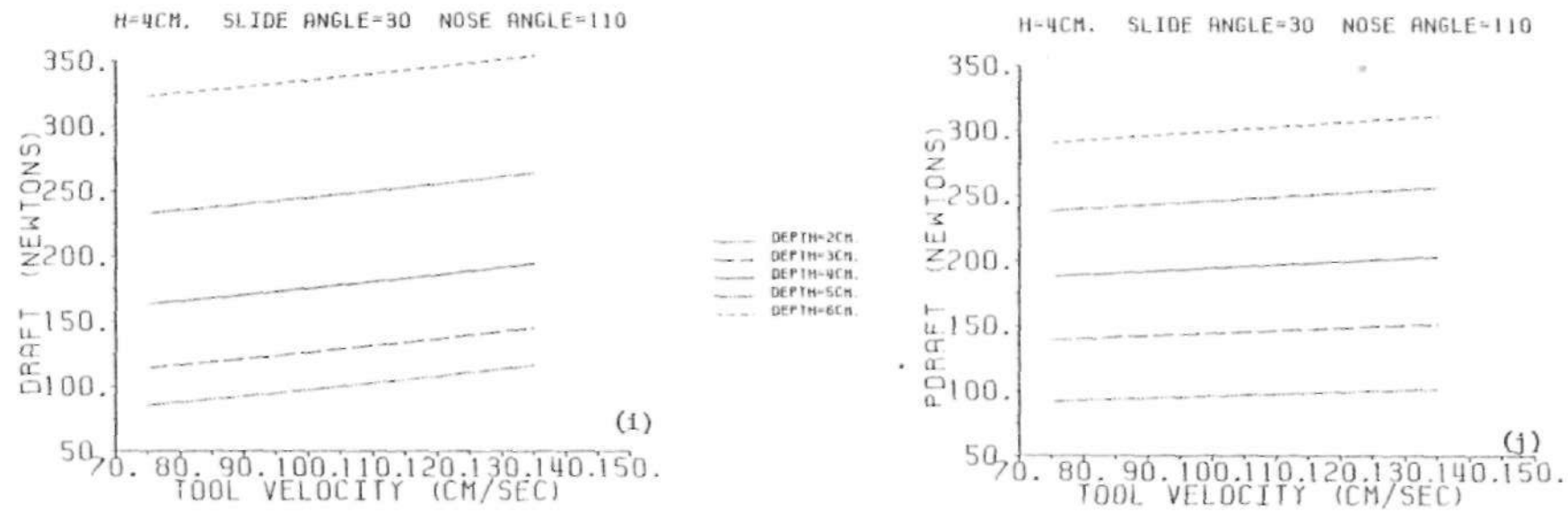

H=4CM. SLIDE ANGLE=30 NOSE ANGLE=110
DRAFT (NEWTONS)
350.
300.
250.
200.
150.
100.
50
(i)
70. 80. 90. 100. 110. 120. 130. 140. 150.
TOOL VELOCITY (CM/SEC)
DEPTH=2CM.
DEPTH=3CM.
DEPTH=4CM.
DEPTH=5CM.
DEPTH=6CM.
H=4CM. SLIDE ANGLE=30 NOSE ANGLE=110
DRAFT (NEWTONS)
350.
300.
250.
200.
150.
100.
50
(j)
70. 80. 90. 100. 110. 120. 130. 140. 150.
TOOL VELOCITY (CM/SEC)

Fig. 7.4 (cont.)

7.4.2 *Influence of Tool Velocity on Draft*

Velocity factor entered into the two model equations by interacting with other factors and as a square term. This implies that the velocity has an ordered and parabolic relationship with draft force. Draft force increases as the velocity increases for the given levels of other factors. Except at shallow depths where the influence of speed is not appreciable for Pdraft, an increase in the level of any of the factors accompanied by an increase in velocity also increases draft. This is due to the significance of velocity in interactions with other factors of the models. This is quite apparent in Figures 7.4 to 7.5. An increase in tool velocity brings about an increase in the force needed to accelerate the sheared soil segment.

7.4.3 *Influence of Nose Angle (2Y) on Draft*

The nose angle is one of the design parameters of this tool type. Its contribution to the model equations is mainly in the form of interaction with other factors. A close examination of Tables 7.1 to 7.2 and the tables in Appendix C (C.7.4 to C.7.5) would reveal a decrease in draft as nose angle is increased up to 100 degrees for given levels of soil depth, tool lift height and slide angle respectively. This is attributable to a decrease in the acceleration force and the weight of soil segment with an increase in nose angle. This is obvious from the analytical results presented in Appendix C.7.3. From this experiment, a minimum draft is observed for nose angle of 100 degrees for given levels of H, θ and depth. Below or above this, draft tends to increase with velocity at those levels of other factors.

7.4.4 *Influence of Slide Angle (θ) on Draft*

Figure 7.5 shows an ordered increase in draft as the slide angle is increased. The resulting increase in draft is mainly due to the

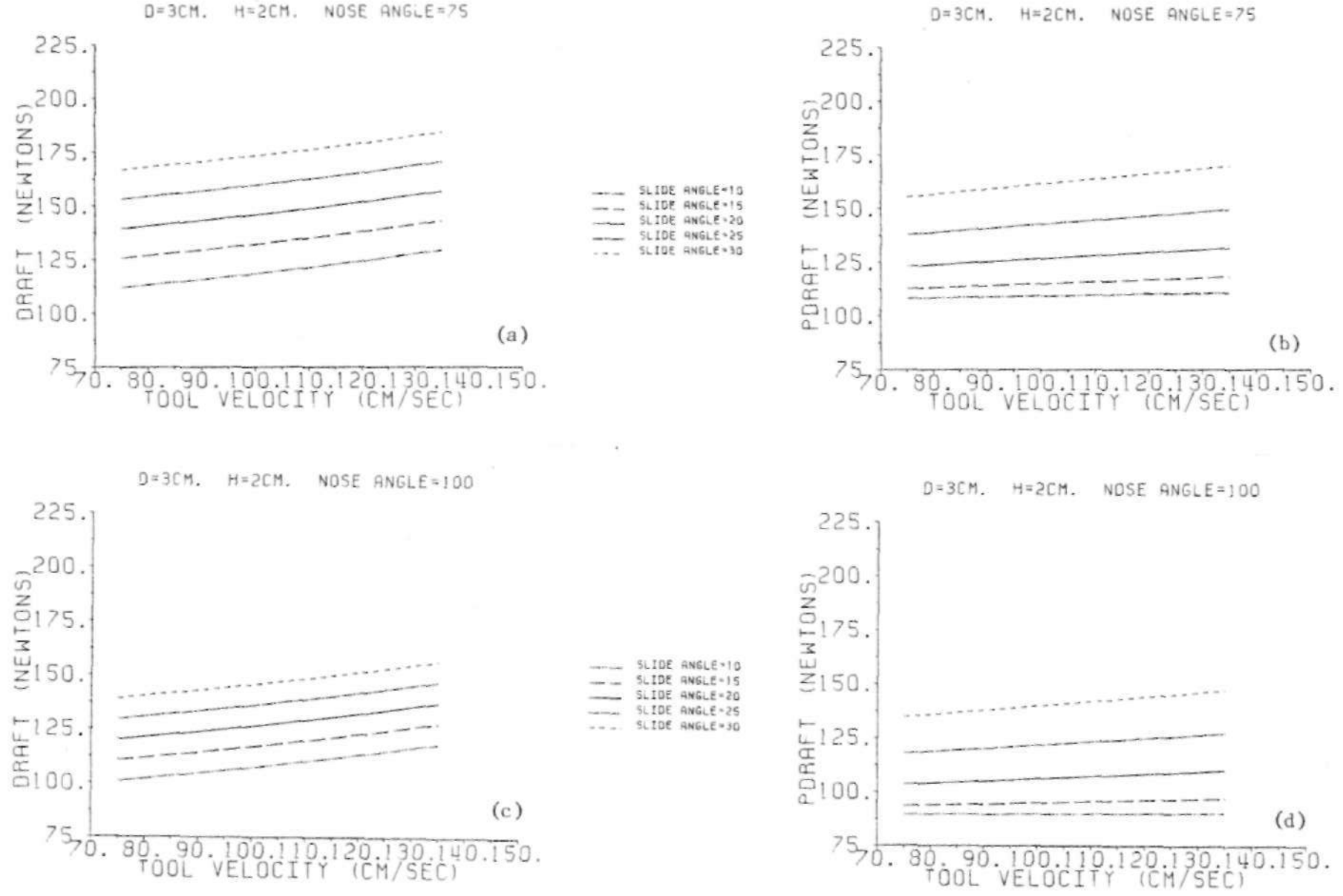
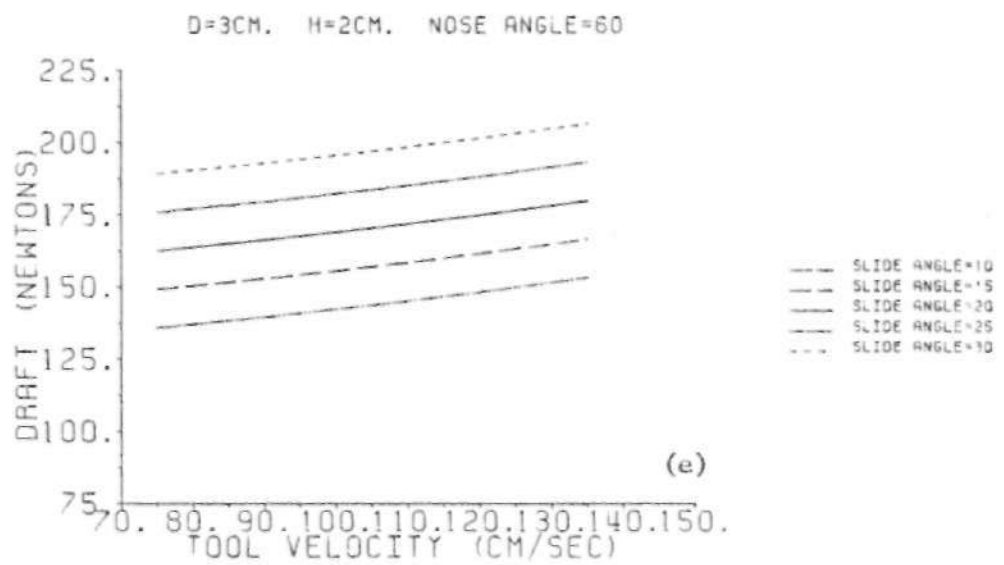


Fig. 7.5 Draft and Pdraft vs Velocity for Levels of Slide Angle



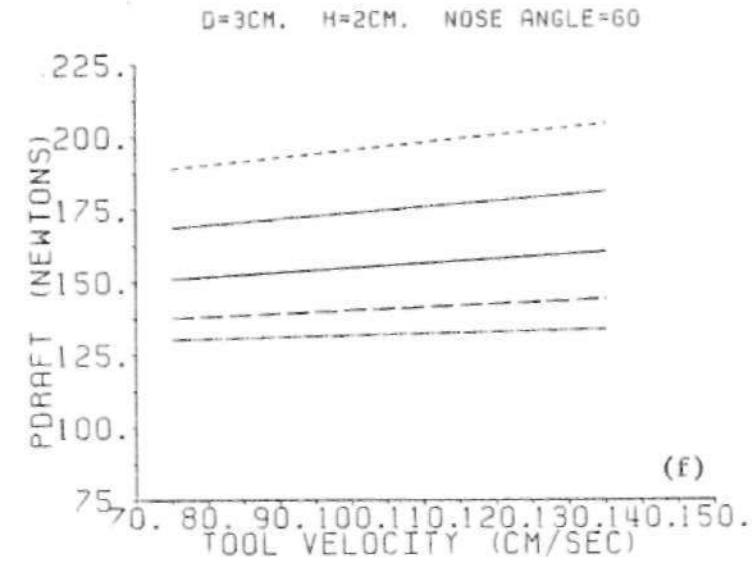


Fig. 7.5 continued

increase in the acceleration force on the soil segment. Also, since the slide angle varies proportionately with the slide length, there is an increase in the frictional force. This result further confirms the assumption that the soil segment flows along the slide length parallel to the direction of travel of the tool.

It will be observed from the tables of generated data that there is little agreement between model drafts and model Pdraft at slide angle of 10 degrees.

7.4.5 Influence of Lift Height (H) on Draft

The results of this analysis shows that an increase in the tool lift height increases draft force. This is due to the increase in the acceleration force. Beyond a lift height of 3 cm there is poorer agreement between the experimental model, Draft, and the analytical model, Pdraft. However, seldom do lift heights exceed 3 cm which translates to 12 cm for the prototype tools. The increase in draft with lift height, particularly for large slide angles, is due to an increase in the force required to lift the soil before it flows over the tool. Such tools have the tendency to disturb the soil surface more than those with smaller lifts.

7.5 Optimum Combination of Factors

The optimum level for each of the five factors can be selected from Figures 7.4 and 7.5, Tables 7.3 and 7.4 and the Tables in Appendix C. Though not readily observable from the graphs, minimum draft is obtained at a nose angle of 100 degrees for given levels of other factors. Figure 7.5 shows that increasing the slide angle, θ , increases draft force. The poor correlation between experimental model, Draft, and the analytical model, Pdraft, at low slide angles is further illustrated in Fig. 7.5(a) and (b) and in Table 7.5. Hence, a slide angle of 20 degrees is considered optimum for this study. Increasing the tool lift height increases draft

force for given levels of other factors. A selection of a lift height of 2 cm is considered reasonable for this investigation. A depth of 2 cm is ideal for weed control while 5 cm is considered optimum for deep tillage. These translate to depths of 8 cm. and 20 cm respectively for the prototype (true size).

Figures 7.6 and 7.7 show that there is a closer correlation between experimental model (Draft) and the analytical model (Pdraft) at a depth of 5 cm than at a depth of 2 cm. This is possibly due to the high compaction at the soil surface as observed during the conduct of this experiment.

Figures 7.6 and Table 7.6 show the influence of different levels of velocity on Draft and Pdraft as soil depth is increased for the optimum levels of nose angle, slide angle and lift height. There is closer agreement between the two models at high velocity and greater depth as mentioned above.

It is difficult to arbitrarily select an optimum velocity for this tool type since this depends on the farming practices at each locality. Some farmers would prefer to operate at high velocity while others may prefer low velocity at varying depths. Besides, velocity was not varied enough to specify an optimum. The plotted graphs only illustrate the trends as each of the factors is varied.

Table 7.7 is a comparison between the results for the experimental model (Draft) and the analytical model (Pdraft) at depths of 2 cm. and 5 cm. for low and high velocities (80 cm/sec. and 140 cm/sec.) respectively.

TABLE 7.5. Influence of Tool Slide Angle on Draft and Pdraft For Varying Levels of Velocity

				DRAFT					PDRAFT				
				VELOCITY (CM/SEC)					VELOCITY (CM/SEC)				
H	D	2Y	θ	80	100	120	140	160	80	100	120	140	160
2	2	100	10	73.11	78.29	84.28	91.09	98.71	61.76	61.10	60.45	59.79	59.13
			15	80.89	86.06	92.05	98.86	106.49	61.04	61.37	61.71	62.04	62.37
			20	88.66	93.84	99.83	106.64	114.26	66.31	67.63	68.96	70.28	71.61
			25	96.44	101.61	107.60	114.41	122.04	75.92	78.23	80.55	82.86	85.18
			30	104.21	109.39	115.38	122.19	129.81	88.22	91.53	94.83	98.13	101.44
2	5	100	10	190.35	195.53	201.52	208.33	215.95	147.38	149.45	151.53	153.60	155.67
			15	203.59	208.76	214.76	221.56	229.19	161.46	164.53	167.59	170.66	173.72
			20	216.82	222.00	227.99	234.80	242.42	181.54	185.59	189.65	193.70	197.76
			25	230.06	235.23	241.22	248.03	255.66	205.96	211.00	216.04	221.09	226.13
			30	243.29	248.47	254.46	261.27	268.89	233.06	239.10	245.13	251.16	257.20

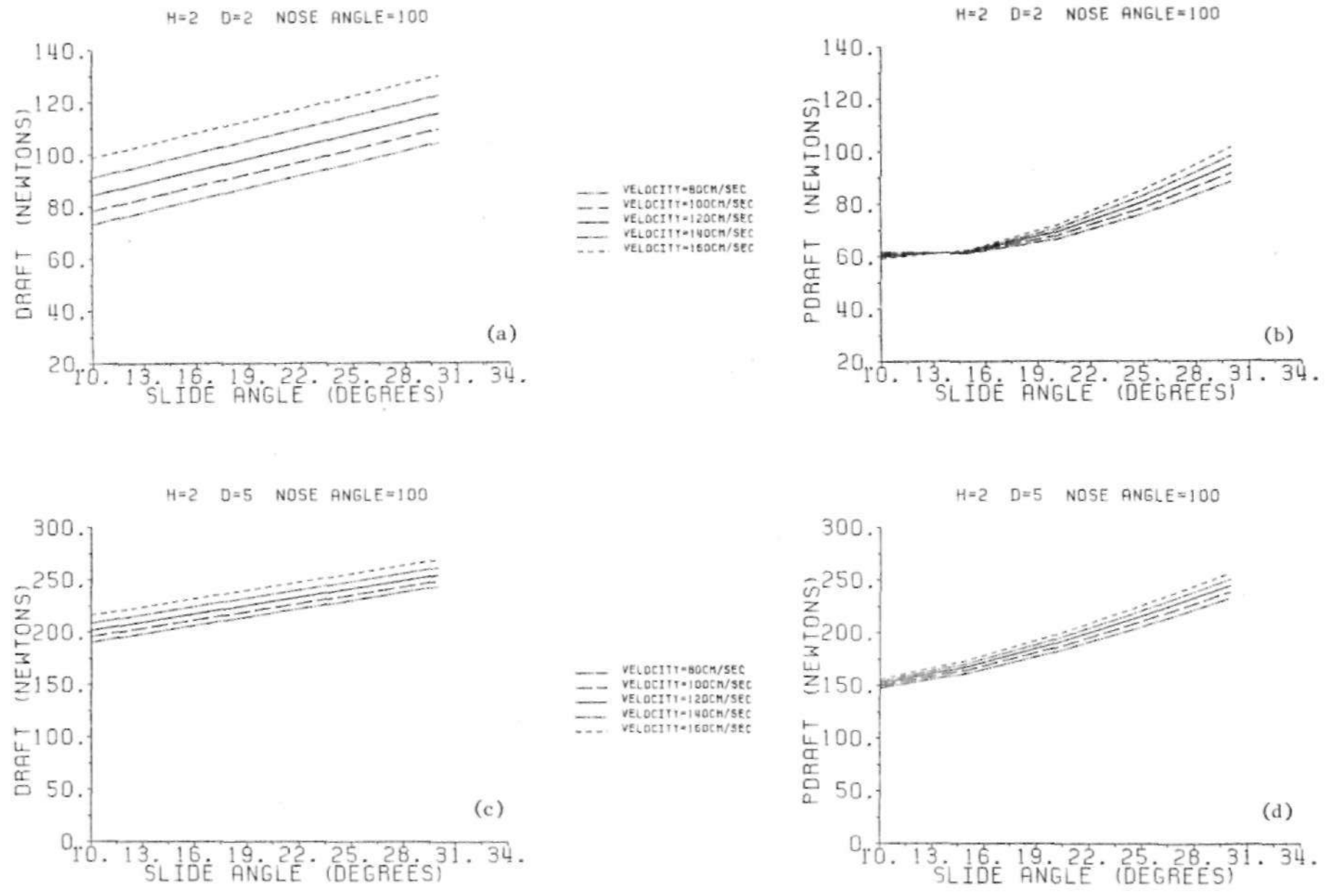


Fig. 7.6 Draft and Pdraft vs Slide Angle for Levels of Velocity

TABLE 7.6. Influence of Soil Depth on Draft and Pdraft
For Varying Levels of Velocity

				DRAFT					PDRAFT				
				VELOCITY (CM/SEC)					VELOCITY (CM/SEC)				
H	0	2Y	D	80	100	120	140	160	80	100	120	140	160
2	20	100	2	88.66	93.84	99.83	106.64	114.26	66.31	67.63	69.00	70.28	71.61
			3	121.16	126.34	132.33	139.14	146.76	103.90	106.13	108.36	110.60	112.83
			4	163.88	169.06	175.05	181.86	189.48	142.31	145.45	148.59	151.74	154.88
			5	216.82	222.00	227.99	234.80	242.42	181.54	185.59	189.65	193.70	197.76
			6	279.97	285.15	291.14	297.95	305.57	221.60	226.60	231.52	236.49	241.45

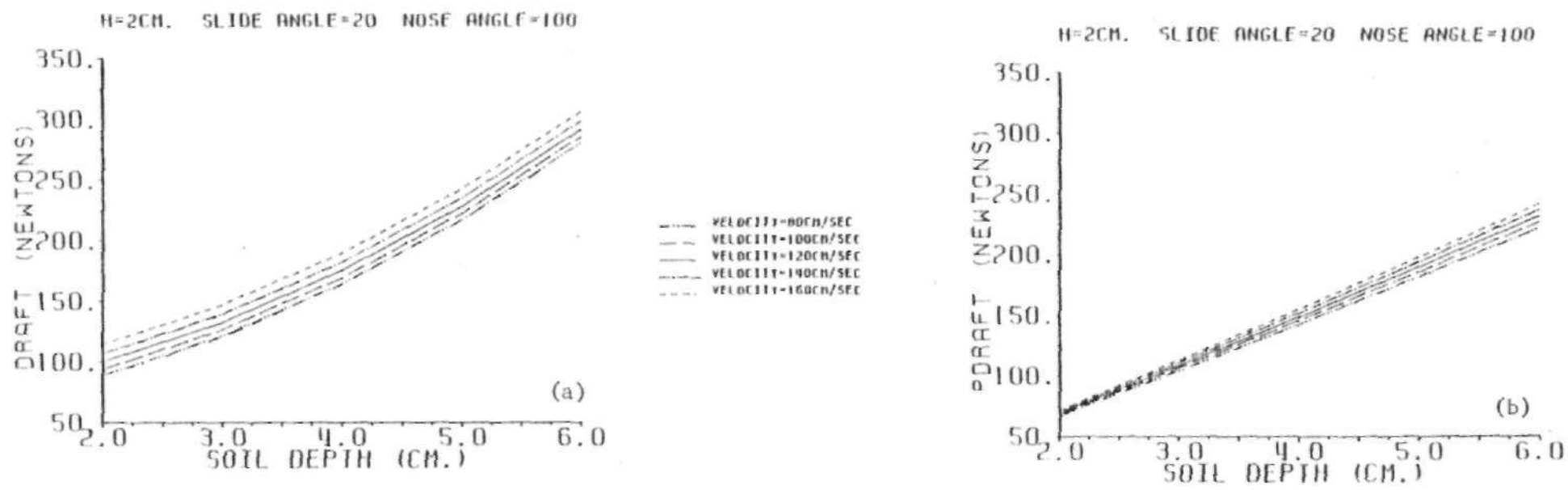


Fig. 7.7 Draft and Pdraft vs Soil Depth for Levels of Velocity

Table 7.7 Draft and Pdraft results for the Optimum combination of factors

H=2cm	θ =20°	2Y=100°	
speed(cm/sec)	Draft(N)	Pdraft(N)	Difference(N)
	(a) DEPTH=2cm		
80	88.66	66.31	22.35
140	106.64	70.28	36.36
	(b) DEPTH=5cm		
80	216.82	181.54	35.28
140	234.80	193.70	41.10

A soil surface similar to that shown in Fig. 7.1 is anticipated for the above tool at a depth of 2 cm while that shown in Fig. 7.2 is anticipated for this tool type operating at a depth of 5 cm. Using the above result as the average for this investigation, the factors shown below establish a correspondence between experimental model and the analytical model:

For D = 2 cm: V = 80 cm/sec Draft = 1.34 Pdraft

V = 140 cm/sec Draft = 1.52 Pdraft

For D = 5 cm: V = 80 cm/sec Draft = 1.20 Pdraft

V = 140 cm/sec Draft = 1.21 Pdraft.

These factors are sufficiently reasonable and can be applied for predicting draft forces in the artifical soil, on this tool type. Closer agreement is expected as the prediction equations for the analytical model are improved.

7.6 Model Selection

The analytical model, Pdraft, was statistically developed from the results of the analytical study. This was by using mathematical equations were used for combining the various tool parameters and soil properties to predict draft forces on this tool type. It is a means of predicting the amount of energy needed for the specified soil conditions. Certain assumptions were made in the mathematical model. These include the pattern of soil failure in front of the tillage tool with varying soil depths and operating velocities, the relationship between soil shearing strength and soil depth, direction of flow of sheared soil segment along the surface of the tool and the influence of tool velocity on the acceleration force of soil segments being sheared.

The experimental model, Draft, was also statistically developed from the observed results of operating the twenty-nine model tools in the soil bin. These results were influenced by the method of soil preparation and the variation in the tool geometry. Influences of soil resistance to cutting and the weight of soil segment as soil depth and operating speed were increased are also reflected in the results.

At shallow depth, the problem of surface compaction by the soil processing equipment and the bulldozing of soil by some tools constituted the source of poor correlation between the experimental model and the analytical model. The variation in soil density with soil depth also contributed to this poor agreement, particularly at greater depth.

It is therefore impossible to conclude that one model is superior to the other.

However, the analytical model, though it generally underpredicted draft forces for some of these tools, may be preferred over the experimental model for the following reasons:

1. It is not specific for any soil environment.
2. It gave a comparable trend with the experimental model and hence shows good promise with further refinement of the prediction equations.
3. It provides a general basis for predicting the energy requirement for this tool type.

The levels of tool paramenters contributing to minimum and maximum draft force for this investigation are as shown below:

a) Parameters causing minimum draft at a depth of 2 cm:

	Model Draft			Model Pdraft		
Velocity	H	θ	2γ	H	θ	2γ
80 cm/sec	2	10	100	2	10	100
140 cm/sec	2	10	100	2	10	100

b) Parameters causing minimum draft at a depth of 5 cm:

	Model Draft			Model Pdraft		
Velocity	H	θ	2Y	H	θ	2Y
80 cm/sec	2	10	100	2	10	110
140 cm/sec	2	10	100	2	10	110

c) Parameters causing maximum draft at a depth of 5 cm:

	Model Draft			Model Pdraft		
Velocity	H	θ	2Y	H	θ	2Y
80 cm/sec	3	30	60	3	30	60
140 cm/sec	3	30	60	3	30	60

The above levels of factors are only relevant to this investigation as they do not reflect the optimum combination of factors as previously discussed.

Chapter VIII

SUMMARY AND CONCLUSIONS

8.1 Summary

The objectives of this investigation included (a) development of an analytical model which predicts the horizontal draft force on undercutters, and (b) verification of the validity of the model experimentally.

Vector algebra and the mechanics of equilibrium were employed for the design of each of the model tools and in the establishment of the prediction equations.

Twenty-nine model tools were designed and a central composite statistical design was followed in the conduct of the experiment, aimed at providing information on the contributions of soil depth (D), tool lift height (H), tool slide angle (θ), tool nose angle (2γ) and the tool velocity (V) to the horizontal draft force on the tools. There were five levels to each of the factors.

The soil properties used in the draft prediction model study are the soil density (ρ), soil cohesion (c), angle of soil shearing resistance (ϕ) and the angle of soil-metal friction (δ). Experimental work was carried out in the K.S.U. soil bin where a standard soil preparation was established on the artifical soil used. Each of the factors was varied in accordance with the statistical design during the conduct of the experiment.

The instrumentation employed for this study included a tillage tool dynamometer, a recorder with signal conditioning capability, a microprocessor (SYM-1) and a Digital Corporation minicomputer. The results of the experimental study and the analytical study were analyzed statistically and the resulting statistical models were used

to generate data for plotting the graphs in Figures 7.4 to 7.7.

8.2 Conclusions

1. The results of this investigation showed that it is possible to predict the draft force on undercutters by using a model based on the equilibrium of soil forces passing over the surface of the tool.

2. The analytical model predicted lower draft force for some of the tools at shallow depths and at greater depths. This was due to the limitations imposed by the design of the tools and the problems of scaling and preparing the soil for the experiment. The high compaction at the soil surface could not be completely eliminated further adding to the discrepancy between the deserved and the experimental draft results.

3. For given levels of lift height, slide angle and soil depth, there was a decrease in draft with increasing nose angle (up to nose angle of 100 degrees for model Draft).

4. Soil depth was the most dominant single factor in the two models and was highly significant in the interacting factors.

5. The establishment of statistically developed model equations permitted a closer study of the various combination of factors within limits imposed by the design of the experiment.

6. Beyond tool lift height of 3 cm, there is a poor correlation between the analytical model (Pdraft) and the experimental model (Draft).

8.3 Suggestion for Future Work

1. Further refinement of the analytical (mathematical) model is needed. Account should be taken of soil parameters entering into this development, particularly the contribution of soil density to the model and a more precise method of determining this property.

2. Analysis of the forces along the cutting edge of the tool in relation to the forces along the soil failure surface should be studied. This may significantly improve the estimation of forces on the tool and soil segments.

3. Since the high compaction at the soil surface was a persistent problem for this study, particularly at shallow depths, an improved method of soil processing should be investigated for this soil bin.

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APPENDICES

APPENDIX A.4

Force Analysis on an Undercutter

The normal force $\vec{N}_0$ on the undercutter wing can be represented vectorially by unit vectors n_1, n_2 and n_3 such that

$$\vec{N}_0 = |\vec{N}_0| \ (n_1\hat{i}+n_2\hat{j}+n_3\hat{k})$$

The plane of the undercutter wing is similarly defined by vectors $\vec{A}$ and $\vec{B}$ as shown in Fig. 4.6, where

$$\vec{A} = |\vec{A}| \ (\cos\gamma\hat{i}+\sin\gamma\hat{j}+0\hat{k})$$

and

$$\vec{B} = |\vec{B}| \ (\cos\theta\hat{i}+0\hat{j}+\sin\theta\hat{k})$$

Since $\vec{N}_0$ is perpendicular to vectors $\vec{A}$ and $\vec{B}$, their dot products are given as:

$$\vec{N}_0\cdot\vec{A} = 0 \ : \ -n_1\sin\gamma+n_2\cos\gamma+0 = 0 \ ; \ n_2 = n_1\tan\gamma$$

$$\vec{N}_0\cdot\vec{B} = 0 \ : \ -n_1\cos\theta+0+n_3\sin\theta = 0 \ ; \ n_3 = n_1\cot\theta$$

But $n_1^2+n_2^2+n_3^2 = 1$

Hence $n_1^2 + n_1^2(\tan^2\gamma)+n_1^2(\cot^2\theta) = 1$

$$n_1 = \pm \frac{1}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}$$

$$n_2 = \pm \frac{\tan\gamma}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}$$

and $$n_3 = \pm \frac{\cot\theta}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}$$

Considering the orientation of $\vec{N}_0$ on the plane defined by $\vec{A}$ and $\vec{B}$ (Fig. 4.6), the negative sign is correct. Therefore the compoenents of $\vec{N}_0$ in the x, y and z directions are:

$$\vec{N}_{0-x} = -\frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}$$

$$\vec{N}_{0-y} = -\frac{\vec{N}_0\tan\gamma}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}$$

and

$$\vec{N}_{0-z} = - \frac{\vec{N}_0 \cot\theta}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}$$

Forces acting on the Tool:

If the soil segments are assumed to slide parallel to the direction of travel along the slide angle, θ, then the forces acting on the wings are:

Horizontal force components: $-kb\cos\gamma, -\mu'\vec{N}_0\cos\theta$

Side force components: $-kb\sin\gamma, \quad kb\sin\theta$

Vertical force component: $\mu'\vec{N}_0\sin\theta$

The equilibrium equations for the forces acting on the tool can be written as:

Horizontal forces: $$F_x = \frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} + \mu'\vec{N}_0\cos\theta + kb\sin\gamma \qquad (1a)$$

Side forces: $$S = \frac{\vec{N}_0\tan\gamma}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} + kb\sin\gamma \qquad (2a)$$

Vertical forces: $$V = \frac{\vec{N}_0\cot\theta}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} - \mu'\vec{N}_0\sin\theta \qquad (3a)$$

Forces Acting On the Soil Segment:

From Fig. 4.2, $\vec{N}_1$ acts on the shear failure surface defined by vectors $\vec{C}$ and $\vec{D}$. This can be resolved vectorially as:

$\vec{N}_1 \cdot \vec{C} = 0$: $n_1\sin\gamma+n_2\cos\gamma+0=0$; $n_2 = n_1\tan\gamma$

$\vec{N}_1 \cdot \vec{D} = 0$: $n_1\cos\psi+0+n_3\sin\psi=0$; $n_3 = n_1\cot\psi$

Using the relationship: $n_1^2+n_2^2+n_3^2 = 1$

then

$$n_1 = - \frac{1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}}$$

$$n_2 = - \frac{\tan\gamma}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}}$$

$$n_3 = - \frac{\cot\psi}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}}$$

The equilibrium equations on the soil segment are obtained from Fig. 4.2 as:

Horizontal forces: $$F_x = \frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} + B\cos\psi + \mu\vec{N}_1\cos\psi + cA\cos\psi \quad (1b)$$

Side forces: $$S = \frac{\vec{N}_1\tan\gamma}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} + kb\sin\gamma \quad (2b)$$

Vertical forces: $$V = G+B\sin\psi+\mu\vec{N}_1\sin\psi+cA\sin\psi- \frac{\vec{N}_1\cot\psi}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} \quad (3b)$$

The cutting resistance components can be obtained from equations (2a) and (2b) as follows:

$$kb\sin\gamma = \tan\gamma\left[\frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} - \frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}\right]$$

and

$$kb\cos\gamma = \left[\frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} \quad \frac{\vec{N}_0}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}}\right] \quad (4)$$

The normal force on the tool, N_0 can be obtained from equations (1a) and (4) as follows:

$$N_0 = \frac{1}{\mu'\cos\theta}\left[F_x - \frac{\vec{N}_1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}}\right] \quad (5)$$

The normal force on the soil failure surface, $\vec{N}_1$ is again obtained from equation (1b) as follows:

$$\vec{N}_1 = F_x - \frac{(B+cA)\cos\psi}{\frac{1}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} + \mu\cos\psi} \quad (6)$$

The vertical force, V can be eliminated by combining equations (3a) and (3b):

$$\frac{\vec{N}_0\cot\theta}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} - \mu'\vec{N}_0\sin\theta = G+B\sin\psi+\mu\vec{N}_1\sin\psi+cA\sin\psi- \frac{\vec{N}_1\cot\psi}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}}$$

$$G - \vec{N}_0\left[\frac{\cot\theta}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}} - \mu'\sin\right] - \vec{N}_1\left[\frac{\cot\psi}{(1+\tan^2\gamma+\cot^2\psi)^{1/2}} - \mu\sin\psi\right] +(B+cA)\sin\psi = 0$$

By substituting for $\vec{N}_0$ and $\vec{N}_1$

$$F_x\left[\frac{\cot\theta-\tan\theta\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}} - \frac{\cot\theta-\mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}\{1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}\}} + \frac{\cot\psi-\mu'\sin\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}}{\mu'\cos\theta\{1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}\}}\right] =$$

$$G +(B+cA)\cos\psi\left\{\tan\psi - \frac{\cot\theta-\mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}\{1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\theta)^{1/2}\}} + \frac{\cot\psi-\mu'\sin\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}}{\mu'\cos\theta\{1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}\}}\right\}$$

This represents an expression for half of the draft force on the tool (one wing). The total draft force on the tool is:

$$F_x = \frac{2}{Z}\left[G+(B+cA)\cos\psi\left[\tan\psi - \frac{\cot\theta-\mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}\{1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}\}} + \frac{\cot\psi-\mu'\sin\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}}{\mu'\cos\theta(1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2})}\right]\right]$$

where:

$$Z = \left[\frac{\cot\theta - \mu'\sin\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{\mu'\cos\theta(1+\tan^2\gamma+\cot^2\theta)^{1/2}} + \right.$$

$$\frac{\cot\psi - \mu'\sin\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}}{\mu'\cos\theta\{1+\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2}\}} -$$

$$\left. \frac{\cot\theta - \mu'\sin\psi(1+\tan^2\gamma+\cot^2\theta)^{1/2}}{(1+\tan^2\gamma+\cot^2\theta)^{1/2}(\mu'\cos\theta+\mu'\cos\theta\mu\cos\psi(1+\tan^2\gamma+\cot^2\psi)^{1/2})} \right]$$

Weight of Soil Segment, G:

The weight of soil segment supported by the tool is obtained from the volume of soil supported and the soil density as proposed by Soehne (41), from Fig. A .4.1,

$$d' = \rho\sin(\psi+\theta)$$

$$l_1 = d'\cot(\psi+\theta)$$

$$d = \rho\sin\psi$$

$$\frac{d'}{d} = \frac{\sin(\psi+\theta)}{\sin\psi} \quad \text{or} \quad d' = \frac{d(\sin\psi+\theta)}{\sin\psi}$$

where d = depth of the operation of the tool in the soil

d'= height of sheared soil segment on the tool

and

l_0, l_1, and l_2 can be approximated by the width of the wing.

hence,

$$G = \rho b \frac{d\sin(\psi+\theta)}{\sin\psi} \left[w + d/2 \left[\frac{\cos(\psi+\theta)}{\sin\psi} + \frac{\sin(\psi+\theta)\tan\theta}{\sin\psi} \right] \right]$$

where ρ = the soil bulk volume weight

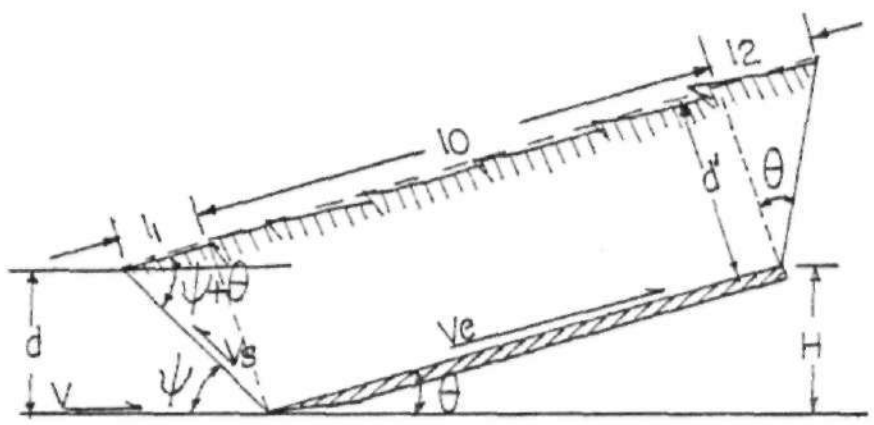
w = width of the wing

b = effective length of the cutting edge

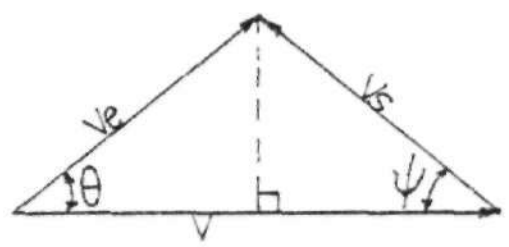
Acceleration force, B:

From Newton's second law of motion, acceleration force, B is:

$$B = m \frac{dv}{dt}$$



(a) SOIL SEGMENT ON THE TOOL



(b) VELOCITY POLYGON

Fig. A.4.1 Geometric Elements of a Soil Segment

where m = mass of soil segment being accelerated

v = velocity of soil segment being accelerated

t = time.

If the soil is assumed to be in equilibrium at t =0 with a velocity, v_e, then the mass of soil accelerated,

$$m = \frac{\rho}{g} bd\,t$$

The relative velocity, v, is defined as:

$$v = v_s\cos\psi + v_e\cos\theta$$

where v = relative velocity of soil on the tool

v_s = relative velocity of the soil along failure surface

v_e = relative velocity of the soil along the inclined shear.

From the velocity polygon shown in Fig. A.4.1.

$$v_e = \frac{v_s\sin\psi}{\sin\theta}$$

Substituting v_e into v gives:

$$v\sin\theta = v_s\sin\theta\cos\psi + v_s\sin\psi\cos\theta$$

and

$$v_s = \frac{v\sin\theta}{\sin(\psi+\theta)}$$

At a given point in time,

$$B = \frac{mv_s}{t} = \frac{mv}{t}\,\frac{\sin\theta}{\sin(\psi+\theta)}$$

Substituting for m in B gives:

$$B = \frac{\rho bd}{g} v^2\,\frac{\sin\theta}{\sin(\psi+\theta)}$$

where g = acceleration of gravity.

APPENDIX B.6.1

Soil Density Data For Varying Soil Depth

DEPTH(CM)	SOIL DENSITY (KN/M^3) NUMBER OF ROLLER PASSES					
	0	1	2	3	4	5
1.27	14.71	16.17	16.95	17.44	17.74	18.05
3.81	13.54	15.69	16.82	17.23	17.54	17.75
6.35	14.51	14.62	15.40	15.59	15.79	15.89
8.89	14.91	15.20	15.50	15.50	15.69	16.08
11.43	14.42	14.71	15.01	15.30	15.50	16.28
13.97	12.75	14.32	14.81	15.69	16.08	16.48

Appendix B.6.2. Computer Program for Designing Undercutter Blades

```
c fortran program for the design of model tools
c   ht      = lift height of the tool in cm.
c   theta   = slide angle of the soil in degrees
c   gamma   = half of the tool nose(approach) angle in degrees
c   beta    = angle of inclination of the wings in horizontal plane in degrees
c   alpha   = bevel angle on each wing in horizontal plane in degrees
c   W       = overall width of the tool in cm.
c   ww      = width of each wing in cm.
c   S       = slide length of the tool along soil slide path in cm.
c   hw      = half of the tool overall width in cm. = W/2
c   L1      = major length of each wing in cm.
c   L2      = minor length of each wing in cm.
c   Aw      = surface area of each wing in cm2
c   At      = total surface area of the tool in cm2
c   td      = theta in degrees
c   tr      = theta in radians
c   gd      = gamma in degrees
c   gr      = gamma in radians
c   betad   = beta in degrees
c   betar   = beta in radians
c   alphad = alpha in degrees
c   alphar = alpha in radians
    real L1,L2
    n=29
 10 format(4f6.2)
 20 format(14(2x,f6.2))
    write(6,30)
 30 format(//,5x'ht',4x,'theta',3x,'gamma',5x,'W',5x,'beta',4x,'alpha'
&   5x,'ww',6x,'s',6x,'W/2',5x,'L1',6x,'L2',6x,'Aw',5x,'At')
    if(ierror(104).ne.0)go to 70
    pi=3.141593
    do 60 i=1,n
    read(5,10)ht,td,gd,W
    tr=td*pi/180.
    gr=gd*pi/180.
    a1=sin(tr)
    a2=cos(tr)
    c=cos(gr)
    f=sin(gr)
    x=a1/a2
    y=f/c
    betar=atan(x/f)
    alphar=atan(y/cos(betar))
    ww=ht/sin(betar)
    S=ww/sin(alphar)
    hw=W/2.
    L1=hw/f
    L2=L1-S*cos(alphar)
    Aw=(L1+L2)/2.*ww
    At=Aw*2
    alphad=alphar*180./pi
    betad=betar*180./pi
    write(6,20)ht,td,gd,W,betad,alphad,ww,S,hw,L1,L2,Aw,At
 60 continue
 70 stop
    end
```

Appendix C.7.1.

Observed and Predicted Results

TOOL NO.	TESTRUNI	TESTRUNII	AVE. DRAFT	PREDIC. DRAFT
1.1	116.90	112.00	114.45	98.443
1.2	127.40	124.60	126.00	100.725
1.3	256.20	240.80	248.50	203.995
1.4	256.90	261.80	259.35	208.560
2.1	113.40	108.50	110.95	80.745
2.2	103.60	105.70	104.65	82.566
2.3	212.10	204.40	208.25	167.407
2.4	299.20	297.50	298.35	171.048
3.1	130.00	128.10	129.05	120.353
3.2	137.80	133.70	135.75	124.421
3.3	252.30	263.20	257.75	249.502
3.4	279.90	294.00	286.95	257.638
4.1	112.90	119.70	116.30	103.815
4.2	133.80	121.80	127.80	106.098
4.3	284.50	296.80	290.65	214.740
4.4	310.80	312.90	311.85	219.305
5.1	147.70	161.00	154.35	102.189
5.2	154.70	150.50	152.60	105.603
5.3	240.10	245.70	242.90	211.863
5.4	246.40	240.10	243.25	218.690
6.1	100.60	107.10	103.85	86.186
6.2	114.30	107.80	111.05	88.007
6.3	211.40	234.50	222.95	178.289
6.4	262.10	254.10	258.10	181.930
7.1	138.60	133.70	136.15	124.491
7.2	149.70	147.70	148.70	128.559
7.3	268.10	265.30	266.70	257.778
7.4	275.10	273.00	274.05	265.915
8.1	132.30	130.90	131.60	106.311
8.2	136.50	140.00	138.25	109.725
8.3	238.70	232.40	235.55	220.106
8.4	258.30	264.60	261.45	226.933
9.1	218.40	224.70	221.55	157.545
10.1	163.10	157.50	160.30	150.725
11.1	223.30	218.40	220.85	172.115
12.1	165.20	158.20	161.70	139.791
13.1	186.20	175.70	180.95	143.232
14.1	205.10	201.60	203.35	171.089

Appendix C.7.1.

Observed and Predicted Results (cont.)

TOOL NO.	TESTRUNI	TESTRUNII	AVE. DRAFT	PREDIC. DRAFT
15.1	270.20	272.30	271.25	209.072
15.2	134.34	156.80	145.57	100.960
15.3	175.00	189.70	182.35	156.344
15.4	191.10	203.70	197.40	152.164
15.5	176.40	173.60	175.00	154.122
16.1	67.90	61.90	64.75	49.931
16.2	95.90	98.00	96.95	51.709
16.3	290.50	284.20	287.35	267.952
16.4	301.70	302.40	302.05	276.845
17.1	52.50	49.00	50.75	31.900
17.2	98.00	93.80	95.90	32.960
17.3	279.00	275.80	277.40	171.885
17.4	246.90	259.00	252.95	177.184
18.1	154.70	161.00	157.85	73.099
18.2	121.10	126.70	123.90	78.977
18.3	369.90	394.10	395.50	393.256
18.4	403.90	407.40	405.65	422.647
19.1	125.60	123.20	124.40	56.980
19.2	158.30	168.00	163.15	58.758
19.3	382.90	401.10	392.00	303.198
19.4	427.00	419.30	423.15	312.091
20.1	70.70	74.90	72.80	54.153
20.2	93.80	87.50	90.65	58.455
20.3	294.00	287.00	290.50	291.420
20.4	316.40	338.10	327.25	312.933
21.1	123.90	119.00	121.45	39.306
21.2	198.10	194.60	196.35	40.365
21.3	404.40	396.20	400.30	208.913
21.4	379.10	382.90	381.00	214.212
22.1	83.30	88.20	85.75	77.168
22.2	130.20	123.90	127.05	83.046
22.3	388.50	372.40	380.45	413.602
22.4	448.70	443.80	446.25	442.993
23.1	92.40	86.10	89.25	58.105
23.2	98.00	95.90	96.95	62.407
23.3	384.20	385.00	384.60	311.181
23.4	393.00	392.70	392.85	332.693

Appendix C.7.1.

Observed and Predicted Results (cont.)

TOOL NO.	TESTRUNI	TESTRUNII	AVE. DRAFT	PREDIC. DRAFT
24.1	165.30	161.70	163.50	160.945
25.1	161.00	151.20	156.10	147.302
26.1	203.70	196.70	200.20	193.053
27.1	188.70	172.60	180.65	130.926
28.1	194.60	195.30	194.95	196.991
29.1	196.90	202.30	199.60	137.285
15.1*	364.00	352.80	358.40	265.810
15.2*	85.40	83.80	84.35	49.586
15.3*	188.30	193.20	190.75	158.830
15.4*	171.50	174.30	172.90	150.469
15.5*	180.60	184.10	182.35	154.122

Appendix C.7.2. Computer Program for the Analytical Model using minicomputer.

```
c     program for the mathematical modelling of undercutters
c     td    =theta in degrees is the slide angle of the tool
c     betd=angle of forward failure of the soil
c     gd    =gamma in degrees is one half of the nose angle of the tool
c     phid =soil frictional angle in degrees
c     deltd=soil-metal frictional angle in degrees
c     rho   =soil bulk volume weight in N/cm3
c     gv    =acceleration of gravity in cm/sec2
c     b     =length of the cutting edge of each wing
c     w     =width of the tool wing in cm.
c     G     =weight of the soil segment in Newtons(N)
c     B     =acceleration force in N
c     v     =tool velocity in cm./sec.
c     ch    =soil cohesion in N/cm2
c     A     =area of forward failure surface of soil segment in cm2
c     d     =depth of operation of the tool in cm.
c     Fx     =predicted tool draft force in N
      Tn    =Tool No.
      n=86
  100 format(2x,i3,6f8.2)
  110 format(' ',5x,i3,5f8.2,f10.3,f8.3,f10.3,f8.3,2f10.3,f8.2)
      if(ierror(104).ne.0)go to 20
      pi=3.141593
      gv=981.0
    betd=32.0
     phid=27.0
    deltd=24.0
      rho=0.0155
      ch=0.660
      write(6,120)
  120 format(///,5x,120('-'))
      write(6,130)
  130 format(//,21x,'WING',4x,'WING',12x,'SOIL',3x,'FAILURE',3x,'ACCEL',
     &    3x,'WT. SOIL',21x,'PREDIC.',2x,'TOOL'/6x,'THETA',x,'GAMMA',4x,'WIDTH'
     &    ,2x,'LENGTH',3x,'VEL',5x,'DEPTH',2x,'SURFACE',3x,'FORCE',4x,'SEGMENT'
     &    ,4x'Z',9x,'C',6x,'DRAFT'5x,'NO.')
      write(6,140)
  140 format(/,5x,120('-'))
      do 10 i=1,n
      read(5,100)td,gd,w,b,v,d,Tn
      tr=td*pi/180.
      gr=gd*pi/180.
     betr=betd*pi/180.
     phir=phid*pi/180.
    deltr=deltd*pi/180.
      x1=sin(tr)
      x2=sin(betr)
      x3=cos(tr)
      x4=cos(betr)
      x5=x1/x3
      x6=sin(tr+betr)
      x7=cos(tr+betr)
```

Appendix C.7.2. continued

```
      a1=x2/x4
      a2=1./x5
      h1=sin(deltr)
      h2=cos(deltr)
      h3=sin(gr)
      h4=cos(gr)
      h5=sin(phir)
      h6=cos(phir)
      a3=h1/h2
      a4=h3/h4
      a5=(a4)**2
      a6=(a2)**2
      a7=h5/h6
      a8=1./a1
      a9=(a8)**2
      f1=(1.+a5+a6)**0.5
      f2=(1.+a5+a9)**0.5
      r1=(a2-a3*x1*f1)
      r2=(a3*x3+a3*x3*a7*x4*f2)*f1
      r3=(a8-a3*x2*f2)
      r4=(1.+a7*x4*f2)*a3*x3
      p1=(a2-x5*a7*x3*f1)
      p2=(a7*x3*f1)
      p3=(a2-a3*x1*f1)
      p4=(a3*x3+(a3*x3*a7*x4*f2))*f1
      p5=(a8-a3*x2*f2)
      p6=(1.+a7*x4*f2)*a3*x3
      e1=p1/p2
      e2=p3/p4
      e3=p5/p6
      e4=r1/r2
      e5=r3/r4
   velsq=v*v
       A=d*b/x2
       B=rho/gv*b*velsq*d*(x1/x6)
       C=a1-e4+e5
      e8=(x6*x5)/x2
       G=(rho*b*(d*x6/x2)*(w+(d/2.*x7/x2)+(d/2.*e8)))
       Z=e1-e2+e3
       W=2*(G+(B+ch*A)*x4*C)/Z
      td=tr*180./pi
    betd=betr*180./pi
      gd=gr*180./pi
    phid=phir*180./pi
   deltd=deltr*180./pi
      write(6,110)td,gd,w,b,v,d,A,B,G,Z,C,Fx,Tn
10 continue
20 stop
      end
```

Appendix C.7.3. Printout for the Analytical (math) model using a minicomputer

THETA θ	GAMMA γ	WING WIDTH ww	WING LENGTH b	VEL v	SOIL DEPTH d	FAILURE SURFACE A	ACCEL FORCE B	WT. SOIL SEGMENT G	z	c	PREDIC. DRAFT Fx	TOOL NO.
15	37.50	5.71	31.29	97.00	2.54	149.979	4.181	13.285	2.013	0.980	98.443	1.1
15	37.50	5.71	31.29	125.00	2.54	149.979	6.944	13.285	2.013	0.980	100.725	1.2
15	37.50	5.71	31.29	97.00	5.08	299.957	8.363	33.725	2.013	0.980	203.995	1.3
15	37.50	5.71	31.29	125.00	5.08	299.957	13.887	33.725	2.013	0.980	208.560	1.4
15	50.00	6.97	24.87	97.00	2.54	119.206	3.323	12.262	1.922	0.940	80.745	2.1
15	50.00	6.97	24.87	125.00	2.54	119.206	5.519	12.262	1.922	0.940	82.566	2.2
15	50.00	6.97	24.87	97.00	5.08	238.413	6.647	30.211	1.922	0.940	167.407	2.3
15	50.00	6.97	24.87	125.00	5.08	238.413	11.038	30.211	1.922	0.940	171.048	2.4
25	37.50	3.78	31.29	97.00	2.54	149.979	5.954	11.742	1.988	1.212	120.353	3.1
25	37.50	3.78	31.29	125.00	2.54	149.979	9.887	11.742	1.988	1.212	124.421	3.2
25	37.50	3.78	31.29	97.00	5.08	299.957	11.908	32.228	1.988	1.212	249.502	3.3
25	37.50	3.78	31.29	125.00	5.08	299.957	19.775	32.228	1.988	1.212	257.638	3.4
15	37.50	8.89	31.29	97.00	2.54	149.979	4.181	18.692	2.013	0.980	103.815	4.1
15	37.50	8.89	31.29	125.00	2.54	149.979	6.944	18.692	2.013	0.980	106.098	4.2
15	37.50	8.89	31.29	97.00	5.08	299.957	8.363	44.538	2.013	0.980	214.740	4.3
15	37.50	8.89	31.29	125.00	5.08	299.957	13.887	44.538	2.013	0.980	219.305	4.4
25	50.00	4.42	24.87	97.00	2.54	119.206	4.732	10.324	1.857	1.196	102.189	5.1
25	50.00	4.42	24.87	125.00	2.54	119.206	7.859	10.324	1.857	1.196	105.603	5.2
25	50.00	4.42	24.87	97.00	5.08	238.413	9.465	27.599	1.857	1.196	211.863	5.3
25	50.00	4.42	24.87	125.00	5.08	238.413	15.717	27.599	1.857	1.196	218.690	5.4
15	50.00	10.84	24.87	97.00	2.54	119.206	3.323	17.492	1.922	0.940	86.186	6.1
15	50.00	10.84	24.87	125.00	2.54	119.206	5.519	17.492	1.922	0.940	88.007	6.2
15	50.00	10.84	24.87	97.00	5.08	238.413	6.647	40.670	1.922	0.940	178.289	6.3
15	50.00	10.84	24.87	125.00	5.08	238.413	11.038	40.670	1.922	0.940	181.930	6.4
25	37.50	5.89	31.29	97.00	2.54	149.979	5.954	15.855	1.988	1.212	124.491	7.1
25	37.50	5.89	31.29	125.00	2.54	149.979	9.887	15.855	1.988	1.212	128.559	7.2
25	37.50	5.89	31.29	97.00	5.08	299.957	11.908	40.455	1.988	1.212	257.778	7.3
25	37.50	5.89	31.29	125.00	5.08	299.957	19.775	40.455	1.988	1.212	265.915	7.4
25	50.00	6.89	24.87	97.00	2.54	119.206	4.732	14.152	1.857	1.196	106.311	8.1
25	50.00	6.89	24.87	125.00	2.54	119.206	7.859	14.152	1.857	1.196	109.725	8.2
25	50.00	6.89	24.87	97.00	5.08	238.413	9.465	35.254	1.857	1.196	220.106	8.3
25	50.00	6.89	24.87	125.00	5.08	238.413	15.717	35.254	1.857	1.196	226.933	8.4
20	43.75	7.69	27.55	111.00	3.81	198.078	8.869	26.454	1.951	1.075	157.545	9.1
20	43.75	4.94	27.55	111.00	3.81	198.078	8.869	19.801	1.951	1.075	150.725	10.1
25	43.75	5.26	27.55	111.00	3.81	198.078	10.297	22.205	1.934	1.206	172.115	11.1
15	43.75	8.14	27.55	111.00	3.81	198.078	7.231	25.365	1.976	0.963	139.791	12.1
20	50.00	6.85	24.87	111.00	3.81	178.810	8.006	22.046	1.886	1.058	143.232	13.1
20	37.50	5.71	31.29	111.00	3.81	224.968	10.073	24.660	1.996	1.086	171.089	14.1
20	43.75	6.31	27.55	111.00	5.08	264.104	11.825	34.309	1.951	1.075	209.072	15.1
20	43.75	6.31	27.55	111.00	2.54	132.052	5.913	13.666	1.951	1.075	100.960	15.2
20	43.75	6.31	27.55	125.00	3.81	198.078	11.247	23.115	1.951	1.075	156.344	15.3
20	43.75	6.31	27.55	97.00	3.81	198.078	6.773	23.115	1.951	1.075	152.164	15.4
20	43.75	6.31	27.55	111.00	3.81	198.078	8.869	23.115	1.951	1.075	154.122	15.5
10	31.25	5.16	36.72	83.00	1.27	88.003	1.317	5.651	2.059	0.908	49.931	16.1
10	31.25	5.16	36.72	139.00	1.27	88.003	3.695	5.651	2.059	0.908	51.709	16.2
10	31.25	5.16	36.72	83.00	6.35	440.014	6.586	47.094	2.059	0.908	267.952	16.3
10	31.25	5.16	36.72	139.00	6.35	440.014	18.473	47.094	2.059	0.908	276.845	16.4

Appendix C.7.3. continued

10	56.25	8.00	22.91	83.00	1.27	54.906	0.822	5.143	1.898	0.799	31.900	17.1
10	56.25	8.00	22.91	139.00	1.27	54.906	2.305	5.143	1.898	0.799	32.960	17.2
10	56.25	8.00	22.91	83.00	6.35	274.530	4.109	37.469	1.898	0.799	171.885	17.3
10	56.25	8.00	22.91	139.00	6.35	274.530	11.525	37.469	1.898	0.799	177.184	17.4
30	31.25	2.23	36.72	83.00	1.27	88.003	2.874	4.099	2.036	1.360	73.099	18.1
30	31.25	2.23	36.72	139.00	1.27	88.003	8.062	4.099	2.036	1.360	78.977	18.2
30	31.25	2.23	36.72	83.00	6.35	440.014	14.372	48.760	2.036	1.360	393.256	18.3
30	31.25	2.23	36.72	139.00	6.35	440.014	40.309	48.760	2.036	1.360	422.647	18.4
10	31.25	13.11	36.72	83.00	1.27	88.003	3.317	12.908	2.059	0.908	56.980	19.1
10	31.25	13.11	36.72	139.00	1.27	88.003	3.695	12.908	2.059	0.908	58.758	19.2
10	31.25	13.11	36.72	83.00	6.35	440.014	6.586	83.375	2.059	0.908	303.198	19.3
10	31.25	13.11	36.72	139.00	6.35	440.014	18.473	83.375	2.059	0.908	312.091	19.4
30	56.25	2.91	22.91	83.00	1.27	54.906	1.793	3.068	1.707	1.338	54.153	20.1
30	56.25	2.91	22.91	139.00	1.27	54.906	5.030	3.068	1.707	1.338	58.455	20.2
30	56.25	2.91	22.91	83.00	6.35	274.530	8.967	32.977	1.707	1.338	291.420	20.3
30	56.25	2.91	22.91	139.00	6.35	274.530	25.149	32.977	1.707	1.338	312.933	20.4
10	56.25	20.34	22.91	83.00	1.27	54.906	0.822	12.170	1.898	0.799	39.306	21.1
10	56.25	20.34	22.91	139.00	1.27	54.906	2.305	12.170	1.898	0.799	40.365	21.2
10	56.25	20.34	22.91	83.00	6.35	274.530	4.109	72.604	1.898	0.799	208.913	21.3
10	56.25	20.34	22.91	139.00	6.35	274.530	11.525	72.604	1.898	0.799	214.212	21.4
30	31.25	5.67	36.72	83.00	1.27	88.003	2.874	8.242	2.036	1.360	77.168	22.1
30	31.25	5.67	36.72	139.00	1.27	88.003	8.062	8.242	2.036	1.360	83.046	22.2
30	31.25	5.67	36.72	83.00	6.35	440.014	14.372	69.475	2.036	1.360	413.603	22.3
30	31.25	5.67	36.72	139.00	6.35	440.014	40.309	69.475	2.036	1.360	442.993	22.4
30	56.25	7.40	22.91	83.00	1.27	54.906	1.793	6.442	1.707	1.338	58.105	23.1
30	56.25	7.40	22.91	139.00	1.27	54.906	5.030	6.442	1.707	1.338	62.407	23.2
30	56.25	7.40	22.91	83.00	6.35	274.530	8.967	49.846	1.707	1.338	311.181	23.3
30	56.25	7.40	22.91	139.00	6.35	274.530	25.149	49.846	1.707	1.338	332.693	23.4
20	43.75	9.06	27.55	111.00	3.81	198.078	8.869	29.769	1.951	1.075	160.942	24.1
20	43.75	3.56	27.55	111.00	3.81	198.078	8.869	16.462	1.951	1.075	147.302	25.1
30	43.75	4.59	27.55	111.00	3.81	198.078	11.572	21.986	1.928	1.360	193.053	26.1
10	43.75	11.90	27.55	111.00	3.81	198.078	5.303	30.807	2.006	0.871	130.926	27.1
20	31.25	5.12	36.72	111.00	3.81	264.008	11.821	26.972	2.027	1.095	196.991	28.1
20	56.25	7.33	22.91	111.00	3.81	164.718	7.375	21.274	1.791	1.032	137.285	29.1
20	43.75	6.31	27.55	111.00	6.35	330.130	14.782	47.247	1.951	1.075	265.810	15.1*
20	43.75	6.31	27.55	111.00	1.27	66.026	2.956	5.961	1.951	1.075	49.586	15.2*
20	43.75	6.31	27.55	139.00	3.81	198.078	13.908	23.115	1.951	1.075	158.830	15.3*
20	43.75	6.31	27.55	83.00	3.81	198.078	4.959	23.115	1.951	1.075	150.469	15.4*
20	43.75	6.31	27.55	111.00	3.81	198.078	8.869	23.115	1.951	1.075	154.122	15.5*

APPENDIX C.7.4

Generated Draft and Pdraft Data For Varying Soil Depth

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
2	15	100	75	79.72	110.40	151.30	202.42	263.75	60.95	93.38	126.63	160.70	195.59
			90	83.37	114.06	154.96	206.07	267.40	61.21	94.31	128.24	163.00	198.57
			105	87.48	118.17	159.07	210.18	271.51	61.46	95.25	129.96	165.29	201.55
			120	92.05	122.74	163.64	214.75	276.09	61.71	96.18	131.47	167.59	204.53
			135	97.08	127.77	168.67	219.78	281.11	61.96	97.11	133.09	169.89	207.51
2	15	110	75	90.82	120.37	160.13	210.12	270.31	60.97	90.17	120.18	151.02	182.67
			90	94.47	124.02	163.79	213.77	273.96	61.06	90.93	121.62	153.13	185.47
			105	98.58	128.13	167.90	217.88	278.08	61.13	91.68	123.05	155.25	188.27
			120	103.15	132.70	172.47	222.45	282.65	61.20	92.43	124.49	157.37	191.07
			135	108.18	137.73	177.50	227.48	287.68	61.21	93.19	125.93	159.49	193.87
2	20	75	75	104.03	139.37	184.93	240.70	306.69	77.63	123.09	169.37	216.47	264.39
			90	107.68	143.02	188.58	244.36	310.34	79.08	125.21	172.17	219.96	268.56
			105	111.79	147.14	192.69	248.47	314.46	80.52	127.34	174.98	223.45	272.74
			120	116.36	151.71	197.26	253.04	319.03	81.96	129.47	177.79	226.94	276.91
			135	121.39	156.74	202.29	258.07	324.06	83.41	131.59	180.60	230.43	281.08
2	20	100	75	87.49	120.00	162.72	215.65	278.81	65.98	103.34	141.52	180.53	220.35
			90	91.15	123.65	166.37	219.31	282.46	66.97	105.01	143.88	183.57	224.08
			105	95.26	127.76	170.48	223.42	286.57	67.96	106.69	146.24	186.61	227.80
			120	99.83	132.33	175.05	227.99	291.14	68.96	108.36	148.59	189.65	231.52
			135	104.86	137.36	180.08	233.62	296.17	69.95	110.04	150.95	192.69	235.25

APPENDIX C.7.4

Generated Draft and Pdraft Data For Varying Soil Depth (cont.)

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
2	20	110	75	95.27	126.64	168.22	220.02	282.04	67.34	101.46	136.41	172.17	208.76
			90	98.92	130.29	171.87	223.67	285.69	68.15	102.96	138.58	175.03	212.31
			105	103.03	134.40	175.98	227.79	289.80	68.97	104.45	140.76	177.90	215.25
			120	107.60	138.97	180.56	232.56	294.37	69.78	105.95	142.94	180.76	219.39
			135	112.63	144.00	185.58	237.39	299.40	70.59	107.44	145.12	183.62	222.94
2	25	100	75	95.27	129.58	174.13	228.89	293.86	75.34	117.64	160.75	204.69	249.46
			90	98.92	133.25	177.79	232.54	297.51	77.08	120.05	163.85	208.48	253.92
			105	103.03	137.36	181.90	236.65	301.62	78.81	122.47	166.96	212.26	258.39
			120	107.60	141.93	186.47	241.22	306.20	80.55	124.89	170.06	216.04	262.85
			135	112.63	146.96	191.50	246.25	311.22	82.28	127.31	173.16	219.83	267.32
2	25	110	75	99.71	132.90	176.31	229.93	293.76	78.03	117.09	156.97	197.67	239.20
			90	103.37	136.55	179.96	233.58	297.42	79.59	119.33	159.89	201.28	243.48
			105	107.48	140.67	184.07	237.69	301.53	81.14	121.57	162.81	204.88	247.77
			120	112.05	145.24	188.64	242.26	306.10	82.70	123.80	165.73	208.48	252.05
			135	117.08	150.27	193.67	247.29	311.13	84.26	126.04	168.65	212.08	256.34
3	15	75	75	103.57	136.62	185.00	248.71	327.74	82.00	120.42	160.09	200.98	243.11
			90	108.63	141.69	190.07	253.77	332.80	82.53	121.64	161.98	203.56	246.37
			105	114.15	147.21	195.59	259.29	338.32	83.05	122.85	163.87	206.13	249.62
			120	120.13	153.19	201.57	265.27	344.30	83.58	124.06	165.76	208.71	252.88
			135	126.57	159.63	208.01	271.71	350.74	84.11	125.27	167.66	211.28	256.14

APPENDIX C.7.4

Generated Draft and Pdraft Data For Varying Soil Depth (cont.)

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
3	15	110	75	114.28	143.36	187.80	247.50	322.56	70.88	97.97	126.30	155.86	186.66
			90	119.34	148.43	192.83	252.57	327.62	70.78	98.55	127.56	157.81	189.28
			105	124.86	153.95	198.35	258.09	333.14	70.67	99.13	128.82	159.75	191.91
			120	130.84	159.93	204.34	264.07	339.12	70.57	99.71	130.09	161.70	194.54
			135	137.28	166.37	210.77	270.51	345.56	70.47	100.29	131.35	163.64	197.17
3	20	75	75	107.85	142.73	192.93	258.46	339.30	86.60	129.96	174.56	220.39	267.45
			90	112.92	147.79	197.99	263.52	344.37	87.87	131.92	177.19	223.71	271.45
			105	118.44	153.32	203.52	269.04	349.89	89.14	133.87	179.83	227.02	275.45
			120	124.42	159.30	209.50	275.02	355.87	90.41	135.82	182.46	230.34	279.45
			135	130.86	165.74	215.94	281.40	362.31	91.68	137.77	185.10	233.66	283.45
3	20	100	75	99.90	131.94	179.30	241.99	320.00	74.94	110.21	146.71	184.45	223.41
			90	104.96	137.00	184.36	247.05	325.06	75.77	111.71	148.90	187.31	226.97
			105	110.48	142.52	188.89	252.57	330.58	76.59	113.22	151.08	190.18	230.52
			120	116.46	148.50	195.87	258.55	336.56	77.41	114.72	153.27	193.05	234.07
			135	122.90	154.94	202.31	264.99	343.00	78.23	116.22	155.45	195.92	237.62
3	20	110	75	111.11	142.01	188.24	249.79	326.67	76.31	108.34	141.60	176.09	211.82
			90	116.17	147.07	193.30	254.85	331.73	76.95	109.66	143.60	178.78	215.20
			105	121.69	152.59	198.82	260.37	337.25	77.59	110.98	145.61	181.47	218.57
			120	127.67	158.57	204.80	266.35	343.23	78.22	112.30	147.61	184.16	221.94
			135	134.11	165.01	211.24	272.79	349.67	78.87	113.63	149.62	186.85	225.31

APPENDIX C.7.4

Generated Draft and Pdraft Data For Varying Soil Depth (cont.)

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
3	25	75	75	112.14	148.84	200.86	268.20	350.87	95.54	143.84	193.37	244.13	296.13
			90	117.21	153.90	205.92	273.27	355.94	97.55	146.53	196.75	248.19	300.88
			105	122.73	159.42	211.44	278.79	361.46	99.57	149.23	200.13	252.26	305.62
			120	128.71	165.40	217.42	284.77	367.44	101.58	151.93	203.50	256.32	310.36
			135	135.15	171.84	223.80	291.21	373.88	103.59	154.62	206.88	260.38	315.10
3	25	110	75	107.93	140.66	188.70	252.08	330.77	86.08	123.04	161.24	200.67	241.33
			90	112.99	145.72	193.77	257.14	335.83	87.46	125.18	163.98	204.10	245.45
			105	118.52	151.24	199.29	262.66	341.36	88.84	127.17	166.73	207.53	249.56
			120	124.50	157.22	205.27	268.64	347.34	90.22	129.24	169.48	210.96	253.67
			135	130.94	163.66	211.71	275.08	353.78	91.61	131.30	172.23	214.39	257.79
4	15	75	75	104.10	131.40	179.13	247.29	335.88	77.93	121.69	167.10	214.15	262.85
			90	111.14	138.44	186.16	254.35	342.92	78.69	123.13	169.22	216.95	266.33
			105	118.63	145.93	193.66	261.82	350.42	79.44	124.57	171.34	219.75	269.82
			120	126.59	153.89	201.61	269.78	358.37	80.20	126.00	173.46	222.56	273.30
			135	135.00	162.30	210.03	278.19	366.78	80.95	127.44	175.58	225.36	276.78
4	15	100	75	102.20	126.66	171.55	236.8	322.64	66.78	102.44	139.76	178.71	219.31
			90	109.24	133.70	178.59	243.92	329.67	67.08	103.43	141.42	181.06	222.35
			105	116.73	141.19	186.09	251.41	337.17	67.39	104.42	143.09	183.42	225.38
			120	124.69	149.15	194.04	259.37	345.12	67.69	105.41	144.76	185.77	228.42
			135	133.10	157.56	202.45	267.78	353.53	68.00	106.39	146.43	188.12	231.45

APPENDIX C.7.4

Generated Draft and Pdraft Data For Varying Soil Depth (cont.)

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
4	15	110	75	117.51	140.83	184.59	248.78	333.40	66.81	99.23	133.31	169.03	206.39
			90	124.54	147.87	191.62	255.81	340.43	66.94	100.05	134.80	171.20	209.25
			105	132.04	155.36	199.12	263.31	347.93	67.06	100.85	136.29	173.37	212.10
			120	139.99	163.32	207.07	271.26	355.88	67.18	101.66	137.78	175.55	214.96
			135	148.41	171.73	215.49	279.68	364.30	67.31	102.47	139.27	177.72	217.81
4	20	75	75	100.77	129.89	179.44	249.42	339.83	81.61	130.30	180.65	232.63	286.26
			90	107.81	136.92	186.47	256.45	346.87	83.11	132.48	183.51	236.18	240.49
			105	115.30	144.42	193.97	263.95	354.36	84.60	134.66	186.37	239.72	294.72
			120	123.26	152.37	201.92	271.90	362.32	86.10	136.84	189.23	243.26	298.94
			135	131.66	160.79	201.34	280.32	370.73	87.60	139.02	192.09	246.81	303.17
4	20	100	75	94.74	121.02	167.73	234.87	322.45	69.95	110.55	152.80	196.69	242.23
			90	101.77	128.05	174.77	241.92	329.49	71.00	112.28	155.21	199.79	246.00
			105	109.27	135.55	182.26	249.41	336.98	72.05	114.01	157.62	202.88	249.78
			120	117.22	143.50	190.22	257.36	344.94	73.09	115.74	160.04	205.97	253.56
			135	125.64	151.92	198.63	265.77	353.35	74.14	117.47	162.45	209.07	257.34
4	20	110	75	106.71	131.86	177.43	243.44	329.88	71.32	108.68	147.69	188.34	230.64
			90	113.75	138.89	184.47	250.48	336.92	72.18	110.23	149.92	191.25	234.23
			105	121.24	146.39	191.96	257.96	344.42	73.05	111.78	152.15	194.17	237.83
			120	129.20	154.34	199.92	265.93	352.37	73.92	113.33	154.38	197.08	241.43
			135	137.61	162.76	208.33	274.34	360.78	74.78	114.88	156.61	200.00	245.03

APPENDIX C.7.4

Generated Draft and Pdraft Data For Varying Soil Depth (cont.)

				DRAFT					PDRAFT				
				SOIL DEPTH(CM)					SOIL DEPTH(CM)				
H	θ	2Y	V	2	3	4	5	6	2	3	4	5	6
4	25	75	75	97.44	128.37	179.74	251.55	343.78	89.63	143.26	198.53	255.45	314.02
			90	104.47	135.41	186.78	258.58	350.82	91.87	146.18	202.14	259.74	318.99
			105	111.97	142.91	194.28	266.08	358.31	94.11	149.10	205.74	264.63	323.96
			20	119.92	150.86	202.23	274.03	366.67	96.35	152.02	209.35	268.32	328.93
			135	128.34	159.27	210.64	282.45	374.68	98.59	154.95	212.95	272.60	333.90
4	25	100	75	87.27	115.37	163.90	232.87	322.26	77.47	123.00	170.18	219.01	269.48
			90	94.31	122.41	170.94	239.91	329.30	79.26	125.48	173.34	222.85	274.00
			105	101.80	129.90	178.44	247.40	336.80	81.05	127.95	176.49	226.68	278.52
			120	109.76	137.86	186.39	255.36	344.75	82.84	130.42	179.65	230.52	283.04
			135	118.17	146.27	194.80	263.77	353.16	84.63	132.89	182.80	234.31	287.56
4	25	110	75	95.92	122.88	170.28	238.11	326.37	80.16	122.46	166.40	211.99	259.22
			90	102.96	129.92	177.32	245.15	333.41	81.77	124.75	169.37	215.65	263.56
			105	110.45	137.42	184.81	252.64	340.90	83.38	127.04	172.35	219.30	267.90
			120	118.41	145.37	192.77	260.60	348.86	84.99	129.33	175.32	222.96	272.24
			135	126.82	153.78	201.18	269.01	357.27	86.60	131.63	178.30	226.62	276.58

APPENDIX C.7.5

Generated Draft and Pdraft Data For Varying Slide Angles

				DRAFT					PDRAFT				
				Slide Angle					Slide Angle				
D	H	2Y	V	10	15	20	25	30	10	15	20	25	30
2	2	60	75	102.35	113.86	125.38	136.89	148.41	89.66	92.13	100.58	113.37	128.86
			90	106.00	117.52	129.03	140.55	152.06	89.89	93.10	102.29	115.83	132.06
			105	110.11	121.63	133.14	144.66	156.17	90.12	94.07	104.01	118.28	135.25
			120	114.68	126.20	137.71	149.23	160.74	90.35	95.04	105.72	120.74	138.45
			135	119.71	131.23	142.74	154.26	165.77	90.58	96.01	107.43	123.20	145.65
2	**2**	**75**	75	80.21	92.12	104.04	115.94	127.85	72.57	72.11	77.63	87.50	100.06
			90	83.87	95.77	107.68	119.59	131.50	72.53	72.81	79.08	89.69	102.99
			105	87.98	99.89	111.79	123.70	135.61	72.48	73.51	80.52	91.87	105.91
			120	92.55	104.46	116.36	128.27	140.18	72.44	74.21	81.96	94.06	108.84
			135	97.58	109.49	121.39	133.30	145.21	72.40	74.91	83.41	96.24	111.77
2	2	100	75	71.94	79.72	87.49	95.27	103.04	61.92	60.95	65.98	75.34	87.39
			90	75.60	83.37	91.15	98.92	106.70	61.43	61.21	66.97	77.08	89.87
			105	79.71	87.48	95.26	103.03	110.81	60.94	61.46	67.96	78.81	92.35
			120	84.28	92.05	99.83	107.60	115.38	60.44	61.71	68.96	80.55	94.83
			135	89.31	97.08	104.86	112.63	120.41	59.95	61.96	69.95	82.28	97.31
2	**3**	**60**	75	116.26	120.16	124.05	127.95	131.84	100.48	102.02	109.55	121.42	135.97
			90	121.33	125.22	129.12	133.01	136.91	100.53	102.82	111.09	123.70	139.00
			105	126.85	130.74	134.64	138.53	142.43	100.59	103.61	112.63	125.98	142.03
			120	132.83	136.72	140.62	144.51	148.41	100.64	104.41	114.17	128.26	145.05
			135	139.27	143.16	147.06	150.95	154.85	100.70	105.21	115.71	130.55	148.08

APPENDIX C.7.5

Generated Draft and Pdraft Data For Varying Slide Angles (cont.)

				DRAFT					PDRAFT				
				Slide Angle					Slide Angle				
D	H	2Y	V	10	15	20	25	30	10	15	20	25	30
2	3	75	75	99.28	103.57	107.85	112.14	116.43	83.39	82.00	86.00	95.54	107.18
			90	104.34	108.63	112.92	117.21	121.49	83.17	82.53	87.87	97.56	109.93
			105	109.86	114.15	118.44	122.73	127.01	82.96	83.05	89.14	99.57	112.69
			120	115.84	120.13	124.42	128.71	132.99	82.74	83.58	90.41	101.58	115.44
			135	122.28	126.57	130.86	135.15	139.43	82.53	84.11	91.68	103.59	118.20
2	3	100	75	99.59	99.74	99.90	100.05	100.21	72.74	70.85	74.54	83.38	94.57
			90	104.65	104.81	104.96	105.12	105.27	72.07	70.92	75.77	84.95	96.82
			105	110.17	110.33	110.48	110.64	110.79	71.41	71.00	76.59	86.51	99.12
			120	116.15	116.31	116.46	116.62	116.77	70.74	71.08	77.41	88.07	101.43
			135	122.59	122.75	122.90	123.06	123.21	70.08	71.16	78.23	89.64	103.73
3	3	60	75	149.20	154.92	160.63	166.35	172.06	138.83	145.30	157.77	174.57	194.06
			90	154.56	159.98	165.70	171.41	177.13	139.57	146.78	159.99	177.53	197.77
			105	159.79	165.50	171.22	176.93	182.65	140.30	148.26	162.21	180.50	201.48
			120	165.77	171.48	177.20	182.91	188.63	141.04	149.74	164.43	183.47	205.19
			135	172.21	177.92	183.64	189.35	195.07	141.78	151.22	166.66	186.43	208.90
3	3	75	75	130.52	136.62	142.73	148.84	154.95	116.88	120.42	129.96	143.84	160.41
			90	135.58	141.69	147.79	153.90	160.01	117.35	121.64	131.92	146.53	163.84
			105	141.10	147.21	153.32	159.42	165.53	117.81	122.85	133.87	149.23	167.28
			120	147.08	153.19	159.30	165.40	171.51	118.28	124.06	135.82	151.93	170.72
			135	153.52	159.63	165.74	171.84	177.95	118.75	125.27	137.77	154.62	174.16

APPENDIX C.7.5

Generated Draft and Pdraft Data For Varying Slide Angles (cont.)

				DRAFT					PDRAFT				
				Slide Angle					Slide Angle				
D	H	2Y	V	10	15	20	25	30	10	15	20	25	30
3	3	100	75	127.99	129.96	131.94	133.91	135.89	98.13	101.18	110.21	123.59	139.65
			90	133.05	135.03	137.00	138.98	140.95	98.15	101.94	111.71	125.83	142.64
			105	138.57	140.55	142.52	144.50	146.47	98.17	102.70	113.22	128.08	145.63
			120	144.55	146.53	148.50	150.48	152.45	98.19	103.46	114.72	130.32	148.61
			135	150.99	152.97	154.94	156.92	158.89	98.21	104.22	116.22	132.57	151.60

DYNAMICS OF UNDERCUTTERS

by

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ABSTRACT

Draft force on undercutters is influenced by the tool geometry, velocity of operation and soil properties. The extent to which the tool design factors influence draft force can best be studied by varying the geometric elements of the tool.

The use of a mathematical model to predict forces on tillage tools often aids in the design and application of such tool types. The inclusion of soil properties in such analytical study is always based on the assumption of soil homogeneity even though soils are rarely homogeneous and isotropic.

The objective of this dissertation, therefore, was to provide an analytical approach to the design and the prediction of draft forces on undercutters and to verify this model experimentally using artificial soil in the laboratory soil bin.

Twenty-nine model tools were designed and tested. The five factors under study were tool slide angle (θ), tool nose angle (2γ), tool lift height (H), tool velocity (v) and soil depth (D) . The resulting predicted and experimental draft forces were analyzed statistically to determine how these factors interacted to influence the draft force. The resulting model equations for the experimental data and the analytical data were referred to as Draft and Pdraft respectively. These equations were in turn used to generate data for plotting the resulting graphs which established comparisons between the two models.

The results show that the analytical model underpredicted draft forces on the model tools. This underprediction was quite noticeable at shallow depths.

From this investigation it was concluded that draft forces on undercutters can be predicted analytically and that better prediction is possible with further refinement of the model equations and uniform processing of the

artificial soil used.

Despite underprediction of draft force, the analytical model is quite versatile because it is not specific for any soil condition and because it shows good promise of improved prediction with further refinement of its parameters.